

# Formal verification of privacy

(for RFID protocols)

Stéphanie Delaune

Équipe EMSEC (IRISA), CNRS, France

Tuesday, September 13th, 2016

# Security protocols everywhere !



## Cryptographic protocols

- ▶ small programs designed to **secure** communication  
*e.g.* secrecy, authentication, anonymity, ...
- ▶ use **cryptographic primitives**  
*e.g.* encryption, signature, .....

# Security protocols everywhere !



## Cryptographic protocols

- ▶ small programs designed to **secure** communication  
*e.g.* secrecy, authentication, anonymity, ...
- ▶ use **cryptographic primitives**  
*e.g.* encryption, signature, .....

**The network is unsecure!**

Communications take place over a **public** network like the Internet.



# Security protocols everywhere !



## Cryptographic protocols

- ▶ small programs designed to **secure** communication  
*e.g.* secrecy, authentication, anonymity, ...
- ▶ use **cryptographic primitives**  
*e.g.* encryption, signature, .....

**It becomes more and more important to protect our privacy.**



# Electronic passport

An e-passport is a passport with an **RFID tag** embedded in it.



The **RFID tag** stores:

- ▶ the information printed on your passport;
- ▶ a JPEG copy of your picture;
- ▶ ...

# Electronic passport

An e-passport is a passport with an **RFID tag** embedded in it.



The **RFID tag** stores:

- ▶ the information printed on your passport;
- ▶ a JPEG copy of your picture;
- ▶ ...

The Basic Access Control (BAC) protocol is a key establishment protocol that has been designed to **protect our personal data**, and to ensure **unlinkability**.

**Unlinkability** aims to ensure *that a user may make multiple uses of a service or resource without others being able to link these uses together.*

[ISO/IEC standard 15408]

# BAC protocol

Passport  
( $K_E, K_M$ )

Reader  
( $K_E, K_M$ )

# BAC protocol

Passport  
( $K_E, K_M$ )

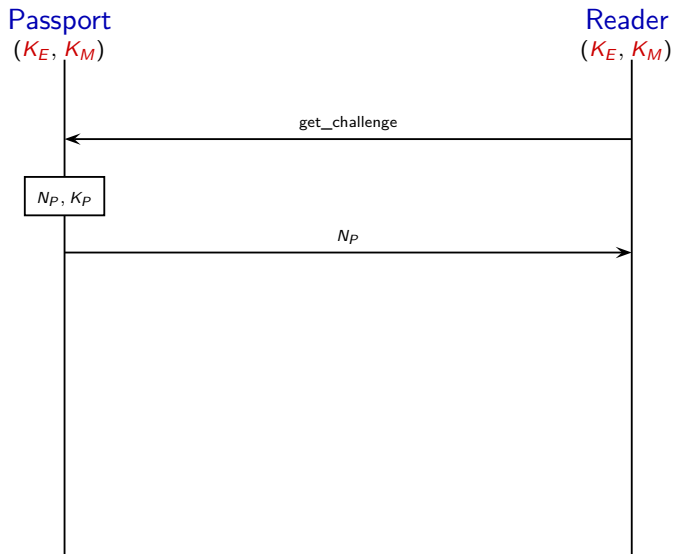
Reader  
( $K_E, K_M$ )

← get\_challenge

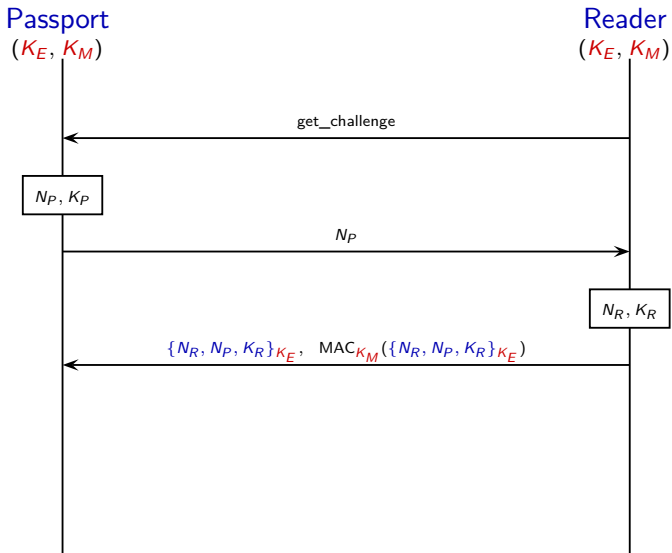
```
sequenceDiagram
    participant Passport as Passport (K_E, K_M)
    participant Reader as Reader (K_E, K_M)
    Reader->>Passport: get_challenge
```



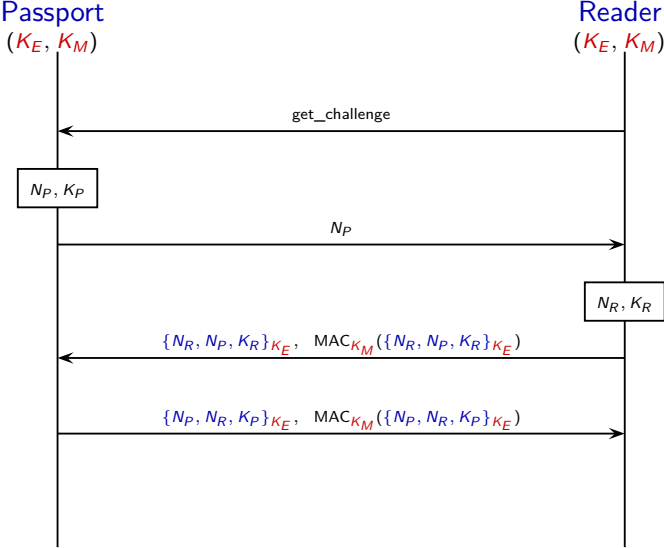
# BAC protocol



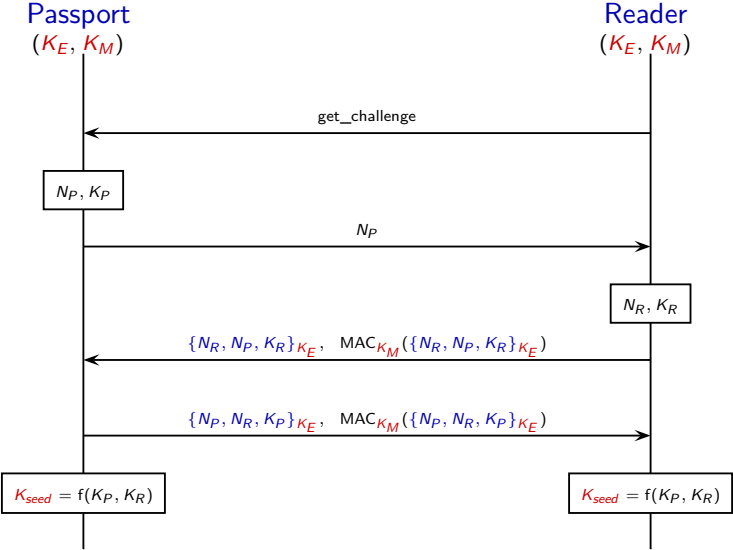
# BAC protocol



# BAC protocol



# BAC protocol



# Verifying security protocols: a difficult task

- ▶ **testing** their resilience against well-known attacks is **not sufficient**;
- ▶ **manual** security analysis is **error-prone**.



→ **Caution:** Do not underestimate your opponents!

# Verifying security protocols: a difficult task

- ▶ **testing** their resilience against well-known attacks is **not sufficient**;
- ▶ **manual** security analysis is **error-prone**.



→ **Caution:** Do not underestimate your opponents!



## Security

### Defects in e-passports allow real-time tracking

This threat brought to you by RFID [The register - Jan. 2010](#)

Lifestyle › Tech › News

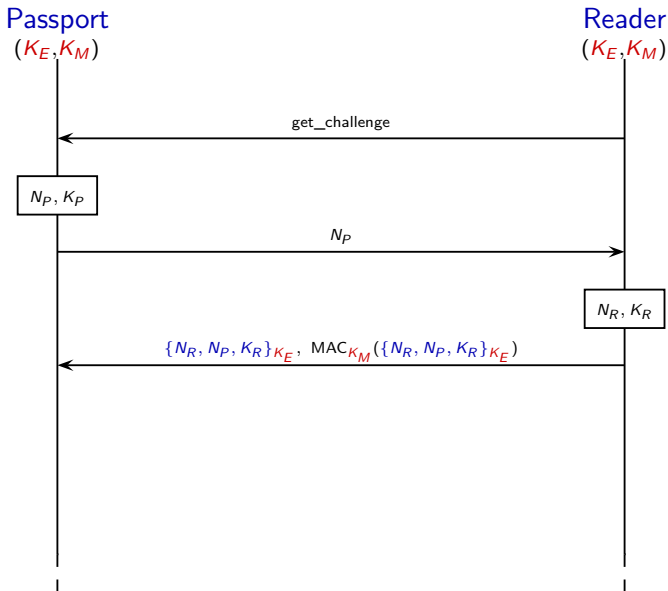
### Contactless card theft: Users warned to watch out for 'digital pickpockets'

[Independent - Feb. 2016](#)



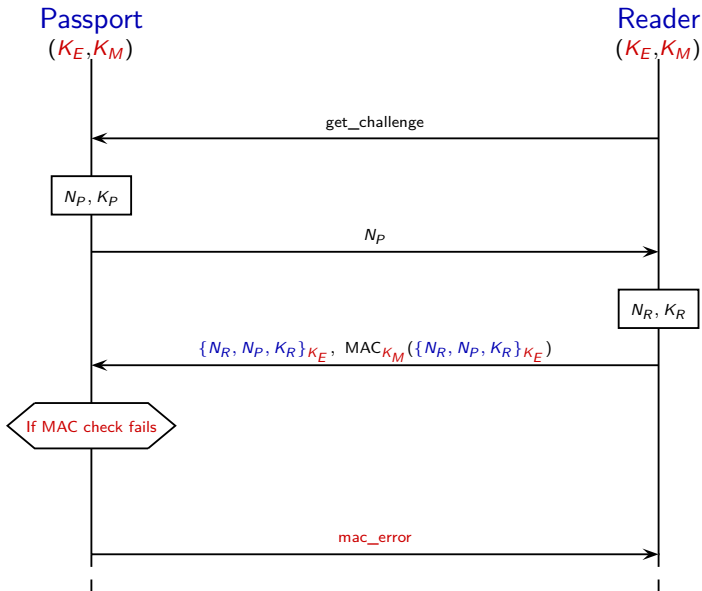
# French electronic passport

→ the passport must reply to all received messages.



# French electronic passport

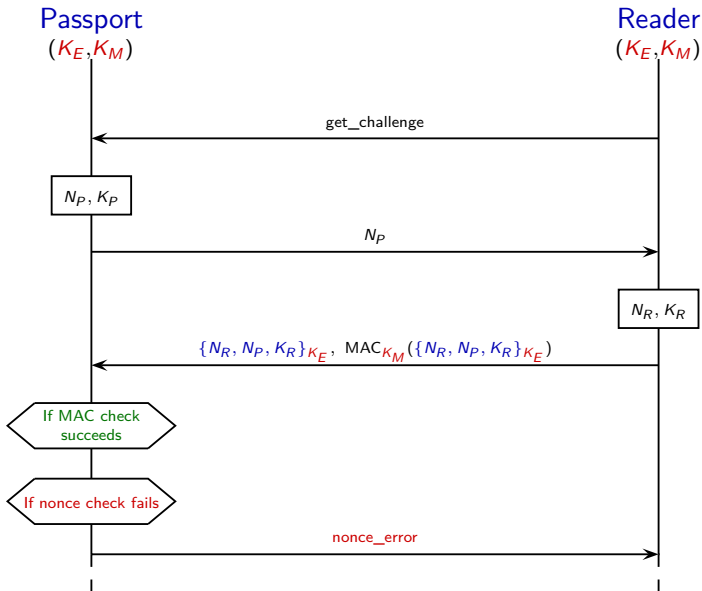
→ the passport must reply to all received messages.





# French electronic passport

→ the passport must reply to all received messages.



## An attack on the French passport [Chothia & Smirnov, 10]

**An attacker can track a French passport**, provided he has once witnessed a successful authentication.

# An attack on the French passport [Chothia & Smirnov, 10]

**An attacker can track a French passport**, provided he has once witnessed a successful authentication.

Part 1 of the attack.

The attacker eavesdropes on Alice using her passport and records message  $M$ .

$$M = \{N_R, N_P, K_R\}_{K_E}, \text{MAC}_{K_M}(\{N_R, N_P, K_R\}_{K_E})$$

# An attack on the French passport [Chothia & Smirnov, 10]

**An attacker can track a French passport**, provided he has once witnessed a successful authentication.

Part 1 of the attack.

The attacker eavesdrops on Alice using her passport and records message  $M$ .

$$M = \{N_R, N_P, K_R\}_{K_E}, \text{MAC}_{K_M}(\{N_R, N_P, K_R\}_{K_E})$$

Part 2 of the attack.

In presence of an unknown passport ( $K'_E, K'_M$ ), the attacker replays the message  $M$  and checks the error code he receives.

1. MAC check failed:  $K'_M \neq K_M \implies \text{???? is not Alice}$
2. MAC check succeeded:  $K'_M = K_M \implies \text{???? is Alice}$

# A successful approach: formal symbolic verification

—→ provides a **rigorous** framework and **automatic tools** to analyse security protocols and find their flaws.

**Example:** Authentication flaw in the Single Sign-On protocol used e.g. in Gmail

[Armando *et al.* (2011)] using SATMC  
(Avantssar verification platform)

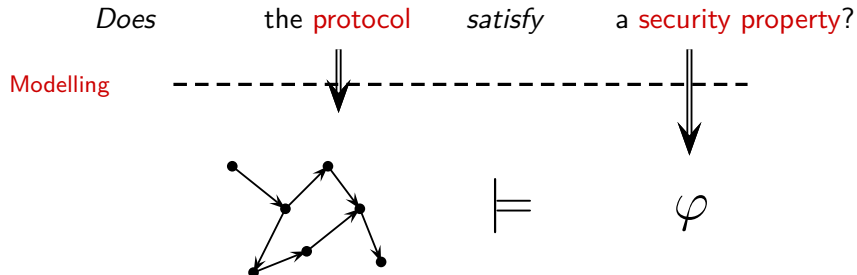


# A successful approach: formal symbolic verification

→ provides a **rigorous** framework and **automatic tools** to analyse security protocols and find their flaws.

**Example:** Authentication flaw in the Single Sign-On protocol used e.g. in Gmail

[Armando *et al.* (2011)] using SATMC  
(Avantssar verification platform)



# A successful approach: formal symbolic verification

→ provides a **rigorous** framework and **automatic tools** to analyse security protocols and find their flaws.

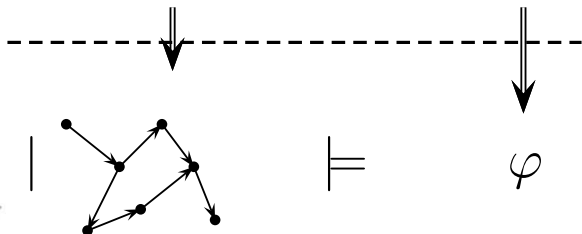
**Example:** Authentication flaw in the Single Sign-On protocol used e.g. in Gmail

[Armando *et al.* (2011)] using SATMC  
(Avantssar verification platform)



Does the **protocol** satisfy a **security property**?

Modelling



# State of the art (in a nutshell)

## for analysing confidentiality/authentication properties

### Unbounded number of sessions

- ▶ **undecidable** in general [Even & Goldreich, 83; Durgin *et al*, 99]
- ▶ decidable for **restricted** classes [Lowe, 99; Rammanujam & Suresh, 03]

### Bounded number of sessions

- ▶ a **decidability** result (NP-complete)  
[Rusinowitch & Turuani, 01; Millen & Shmatikov, 01]



**ProVerif**





# Main limitations of existing verification tools

- ▶ They are **not** suitable to analyse **privacy-type properties**.  
—→ unlinkability, anonymity, vote-privacy . . .
- ▶ They do **not** allow one to reason modulo the algebraic properties of some primitives.  
—→ exclusive or, homomorphic encryption, . . .
- ▶ They do **not** allow to take **physical properties** into account.  
—→ transmission delay, location of participants, network topology

# Main limitations of existing verification tools

- ▶ They are **not** suitable to analyse **privacy-type properties**.  
→ unlinkability, anonymity, vote-privacy ...
- ▶ They do **not** allow one to reason modulo the algebraic properties of some primitives.  
→ exclusive or, homomorphic encryption, ...
- ▶ They do **not** allow to take **physical properties** into account.  
→ transmission delay, location of participants, network topology

These features are important for analysing **contactless systems!**



POPSTAR

(janv. 2017- déc. 2021)

Reasoning about **Physical properties**  
Of **security Protocols**  
with an Application To **contactless Systems**

# Main limitations of existing verification tools

- ▶ They are **not** suitable to analyse **privacy-type properties**.  
→ unlinkability, anonymity, vote-privacy ...
- ▶ They do **not** allow one to reason modulo the algebraic properties of some primitives.  
→ exclusive or, homomorphic encryption, ...
- ▶ They do **not** allow to take **physical properties** into account.  
→ transmission delay, location of participants, network topology

These features are important for analysing **contactless systems**!



POPSTAR

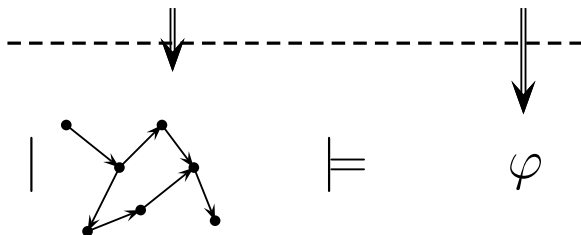
(janv. 2017- déc. 2021)

Reasoning about **Physical properties**  
Of **security Protocols**  
with an Application To **contactless Systems**

# Outline

Does the **protocol** satisfy a **security property**?

Modelling



## Outline of the remaining of this talk

1. Modelling: protocols, security properties, and the attacker !
2. Designing verification algorithms

→ we focus here on **privacy-type** security properties

## Part I

Modelling: protocols, security properties,  
and the attacker

# Protocols as processes

Applied pi calculus: basic programming language with constructs for **concurrency** and **communication** [Abadi & Fournet, 01]

→ based on the  $\pi$ -calculus [Milner *et al.*, 92] ...

$P, Q$	$:=$	$0$	null process
		$\text{in}(c, x).P$	input
		$\text{out}(c, u).P$	output
		$\text{if } u = v \text{ then } P \text{ else } Q$	conditional
		$P \mid Q$	parallel composition
		$!P$	replication
		$\text{new } n.P$	fresh name generation

# Protocols as processes

Applied pi calculus: basic programming language with constructs for concurrency and communication [Abadi & Fournet, 01]

→ based on the  $\pi$ -calculus [Milner *et al.*, 92] ...

$P, Q$	$:=$	$0$	null process
		$\text{in}(c, x).P$	input
		$\text{out}(c, u).P$	output
		$\text{if } u = v \text{ then } P \text{ else } Q$	conditional
		$P \mid Q$	parallel composition
		$!P$	replication
		$\text{new } n.P$	fresh name generation

... but messages that are exchanged are not necessarily atomic !

# Messages as terms

Messages are abstracted by terms built over a set of **names**  $\mathcal{N}$ , and a **signature**  $\mathcal{F}$ .

$$\begin{array}{ll} t ::= n & \text{name } n \\ \quad | f(t_1, \dots, t_k) & \text{application of symbol } f \in \mathcal{F} \end{array}$$



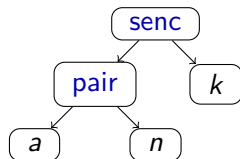
# Messages as terms

Messages are abstracted by terms built over a set of **names**  $\mathcal{N}$ , and a **signature**  $\mathcal{F}$ .

$$\begin{array}{ll} t ::= n & \text{name } n \\ \quad | f(t_1, \dots, t_k) & \text{application of symbol } f \in \mathcal{F} \end{array}$$

**Example:** representation of  $\{a, n\}_k$

- ▶ names:  $n, k, a$
- ▶ constructors: `senc`, `pair`,



# Messages as terms

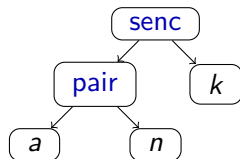
Messages are abstracted by terms built over a set of **names**  $\mathcal{N}$ , and a **signature**  $\mathcal{F}$ .

$$\begin{array}{ll} t ::= n & \text{name } n \\ \quad | f(t_1, \dots, t_k) & \text{application of symbol } f \in \mathcal{F} \end{array}$$

→ The term algebra is equipped with an **equational theory**  $E$ .

**Example:** representation of  $\{a, n\}_k$

- ▶ names:  $n, k, a$
- ▶ constructors: **senc**, **pair**,
- ▶ destructors: **sdec**, **proj<sub>1</sub>**, **proj<sub>2</sub>**.



→ **proj<sub>1</sub>**(**pair**( $x, y$ )) =  $x$ , **proj<sub>2</sub>**(**pair**( $x, y$ )) =  $y$ ,  
**sdec**(**senc**( $x, y$ ),  $y$ ) =  $x$ .

# Semantics of the applied pi

How processes can evolve?

Basically, we have the following rules:

**REPL**  $!P \rightarrow P \mid !P$

**NEW**  $\text{new } n.P \rightarrow P\{n'/n\}$  where  $n'$  is a fresh name

**COMM**  $\text{out}(c, u).P \mid \text{in}(c, x).Q \rightarrow P \mid Q\{u/x\}$

**THEN** if  $u = v$  then  $P$  else  $Q \rightarrow P$  when  $u =_{\mathbf{E}} v$

**ELSE** if  $u = v$  then  $P$  else  $Q \rightarrow Q$  when  $u \neq_{\mathbf{E}} v$

# Going back to the e-passport

Cryptographic primitives are modelled using **function symbols**

- ▶ encryption/decryption:  $\text{senc}/2$ ,  $\text{sdec}/2$
- ▶ concatenation/projections:  $\langle \cdot, \cdot \rangle/2$ ,  $\text{proj}_1/1$ ,  $\text{proj}_2/1$
- ▶ mac construction:  $\text{mac}/2$



→  $\text{sdec}(\text{senc}(x, y), y) = x$ ,  $\text{proj}_1(\langle x, y \rangle) = x$ ,  $\text{proj}_2(\langle x, y \rangle) = y$ .

**Nonces**  $n_r$ ,  $n_p$ , and **keys**  $k_r$ ,  $k_p$ ,  $k_e$ ,  $k_m$  are modelled using **names**

# Going back to the e-passport

Cryptographic primitives are modelled using **function symbols**

- ▶ encryption/decryption:  $\text{senc}/2$ ,  $\text{sdec}/2$
- ▶ concatenation/projections:  $\langle \_, \_ \rangle/2$ ,  $\text{proj}_1/1$ ,  $\text{proj}_2/1$
- ▶ mac construction:  $\text{mac}/2$



→  $\text{sdec}(\text{senc}(x, y), y) = x$ ,  $\text{proj}_1(\langle x, y \rangle) = x$ ,  $\text{proj}_2(\langle x, y \rangle) = y$ .

**Nonces**  $n_r$ ,  $n_p$ , and **keys**  $k_r$ ,  $k_p$ ,  $k_e$ ,  $k_m$  are modelled using **names**

## Modelling Passport's role

$$P_{\text{BAC}}(k_E, k_M) = \text{new } n_P. \text{new } k_P. \text{out}(n_P). \text{in}(\langle z_E, z_M \rangle).$$
$$\text{if } z_M = \text{mac}(z_E, k_M) \text{ then if } n_P = \text{proj}_1(\text{proj}_2(\text{sdec}(z_E, k_E)))$$
$$\text{then out}(\langle m, \text{mac}(m, k_M) \rangle)$$
$$\text{else out}(\textit{nonce\_error})$$
$$\text{else out}(\textit{mac\_error})$$

where  $m = \text{senc}(\langle n_P, \langle \text{proj}_1(z_E), k_P \rangle \rangle, k_E)$ .

# Privacy-type security properties

→ they are modelled as **equivalence-based properties**

Testing equivalence  $P \approx Q$

For **all processes**  $A$ , we have that:

$(A \mid P) \Downarrow_c$  if, and only if,  $(A \mid Q) \Downarrow_c$

$R \Downarrow_c$  means that  $R$  can evolve and emits on public channel  $c$ .

# Privacy-type security properties

→ they are modelled as **equivalence-based properties**

Testing equivalence  $P \approx Q$

For **all processes**  $A$ , we have that:

$$(A \mid P) \Downarrow_c \text{ if, and only if, } (A \mid Q) \Downarrow_c$$

$R \Downarrow_c$  means that  $R$  can evolve and emits on public channel  $c$ .

**Example 1:**  $\text{out}(a, \text{yes}) \stackrel{?}{\approx} \text{out}(a, \text{no})$

# Privacy-type security properties

→ they are modelled as **equivalence-based properties**

Testing equivalence  $P \approx Q$

For **all processes**  $A$ , we have that:

$$(A \mid P) \Downarrow_c \text{ if, and only if, } (A \mid Q) \Downarrow_c$$

$R \Downarrow_c$  means that  $R$  can evolve and emits on public channel  $c$ .

**Example 1:**

$$\text{out}(a, \text{yes}) \not\approx \text{out}(a, \text{no})$$

$$\longrightarrow A = \text{in}(a, x).\text{if } x = \text{yes then out}(c, \text{ok})$$





# Privacy-type security properties

→ they are modelled as **equivalence-based properties**

## Testing equivalence $P \approx Q$

For **all processes**  $A$ , we have that:

$$(A \mid P) \Downarrow_c \text{ if, and only if, } (A \mid Q) \Downarrow_c$$

$R \Downarrow_c$  means that  $R$  can evolve and emits on public channel  $c$ .

**Example 2:**  $k$  and  $k'$  are known to the attacker

$$\begin{aligned} & \text{new } s. \text{out}(a, \text{senc}(s, k)). \text{out}(a, \text{senc}(s, k')) \\ & \quad \neq \\ & \text{new } s, s'. \text{out}(a, \text{senc}(s, k)). \text{out}(a, \text{senc}(s', k')) \end{aligned}$$

→  $A = \text{in}(a, x). \text{in}(a, y). \text{if } (\text{sdec}(x, k) = \text{sdec}(y, k')) \text{ then out}(c, \text{ok})$

# Privacy-type security properties

→ they are modelled as **equivalence-based properties**

Testing equivalence  $P \approx Q$

For **all processes**  $A$ , we have that:

$$(A \mid P) \Downarrow_c \text{ if, and only if, } (A \mid Q) \Downarrow_c$$

$R \Downarrow_c$  means that  $R$  can evolve and emits on public channel  $c$ .

**Example 3:**

$$\text{new } s.\text{out}(a, s) \approx \text{new } s.\text{new } k.\text{out}(a, \text{senc}(s, k))$$

# Some privacy-type properties

Unlinkability

[Arapinis et al, 2010]

$$!new\ ke.new\ km.(!P_{BAC} \mid !R_{BAC}) \approx !new\ ke.new\ km.(P_{BAC} \mid !R_{BAC})$$

↑  
many sessions  
for each passport

↑  
only one session  
for each passport

# Some privacy-type properties

## Unlinkability

[Arapinis et al, 2010]

$$!new\ ke.new\ km.(!P_{BAC} \mid !R_{BAC}) \approx !new\ ke.new\ km.(P_{BAC} \mid !R_{BAC})$$

↑  
many sessions  
for each passport

↑  
only one session  
for each passport

## Vote privacy

[Kremer and Ryan, 2005]

$$S[V_A(\text{yes}) \mid V_B(\text{no})] \approx S[V_A(\text{no}) \mid V_B(\text{yes})]$$

↑  
A votes yes  
B votes no

↑  
A votes no  
B votes yes

## Part II

How can we check testing equivalence?

## Some recent theoretical results

→ [Chrétien PhD thesis, 16]

- ▶ **undecidable** in general (and even under quite severe restriction)
- ▶ a **first decidability result** through a characterization of equivalence of protocols in terms of equality of languages of deterministic pushdown automata. [ICALP'13, TOCL'15]
- ▶ decidable for an interesting subclass of tagged protocols (with nonces) [CSF'15]

# Some recent theoretical results

→ [Chrétien PhD thesis, 16]

- ▶ **undecidable** in general (and even under quite severe restriction)
- ▶ a **first decidability result** through a characterization of equivalence of protocols in terms of equality of languages of deterministic pushdown automata. [ICALP'13, TOCL'15]
- ▶ decidable for an interesting subclass of tagged protocols (with nonces) [CSF'15]

## Main limitations:

- ▶ a **restricted set of primitives**: symmetric encryption, and concatenation only;
- ▶ not really practical (**no verification tool**).



## A more pragmatic approach

→ [Blanchet *et al.*, LICS'05]

ProVerif tool: <http://www.proverif.ens.fr>

- ▶ processes **with replication**;
- ▶ **various** cryptographic primitives modeled using equations;
- ▶ various security properties: secrecy, authentication, and equivalence-based properties (namely **diff-equivalence**);

The tool may not terminate or give false attacks.

## A more pragmatic approach

→ [Blanchet *et al.*, LICS'05]

ProVerif tool: <http://www.proverif.ens.fr>

- ▶ processes **with replication**;
- ▶ **various** cryptographic primitives modeled using equations;
- ▶ various security properties: secrecy, authentication, and equivalence-based properties (namely **diff-equivalence**);

The tool may not terminate or give false attacks.

**Main issue:** diff-equivalence is **too strong** in many situations.

→ ProVerif is not suitable to analyse vote-privacy, or unlinkability of the BAC protocol.

Some extensions have been recently developed to go beyond diff-equivalence, e.g. vote-privacy [Blanchet & Smyth, 16], unlinkability [Hirschi *et al.*, 16].

# Another decidability result (bounded number of sessions)

→ [Cheval PhD thesis, 12]

## Main result

A procedure for deciding **testing equivalence** for a large class of processes implemented in a **tool** called APTE

## The class of processes:

- ▶ + non-trivial else branches, private channels, and non-deterministic choice;
- ▶ – but no replication, and a fixed set of cryptographic primitives (signature, symmetric and asymmetric encryptions, hash function, mac, pairs).

# Another decidability result (bounded number of sessions)

→ [Cheval PhD thesis, 12]

## Main result

A procedure for deciding **testing equivalence** for a large class of processes implemented in a **tool** called APTE

## The class of processes:

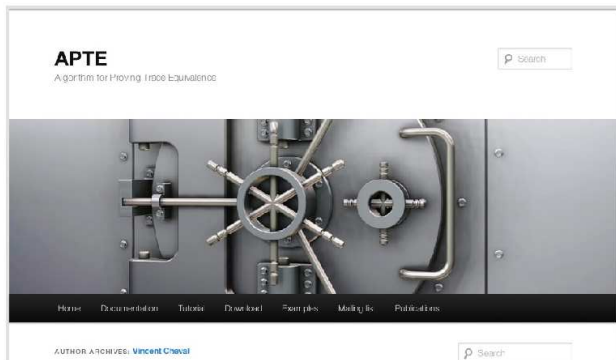
- ▶ + non-trivial else branches, private channels, and non-deterministic choice;
- ▶ – but no replication, and a fixed set of cryptographic primitives (signature, symmetric and asymmetric encryptions, hash function, mac, pairs).

Similar results for restricted class of processes have been obtained in [Baudet, 05], [Dawson & Tiu, 10], [Chevalier & Rusinowitch, 10], [Chadha *et al.*, 12], ...

# APTE- Algorithm for Proving Trace Equivalence

<http://projects.lsv.ens-cachan.fr/APTE> (Ocaml - 12 KLocs)

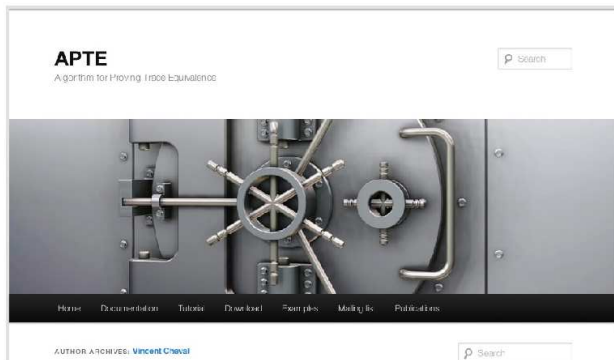
→ developed by Vincent CHEVAL [Cheval, TACAS'14]



# APTE- Algorithm for Proving Trace Equivalence

<http://projects.lsv.ens-cachan.fr/APTE> (Ocaml - 12 KLocs)

→ developed by Vincent CHEVAL [Cheval, TACAS'14]



→ but a limited practical impact because it scales badly

# Conclusion



Reasoning about **Physical properties** Of  
**security Protocols**  
with an Application To **contactless Systems**

## Main issues:

- ▶ **specificities** of contactless systems are not well understood;
- ▶ a lack of **formal model** to reason about these systems.

## Main outcomes:

- ▶ solid **foundations** to reason about **physical properties**;
- ▶ new **algorithms** and **tools** to analyse the security and **privacy** of modern protocols;
- ▶ make the upcoming generation of **nomadic contactless devices** more secure.