

# Type-Based Verification of Electronic Voting Protocols

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Formal Methods Seminar

22<sup>nd</sup> May 2015

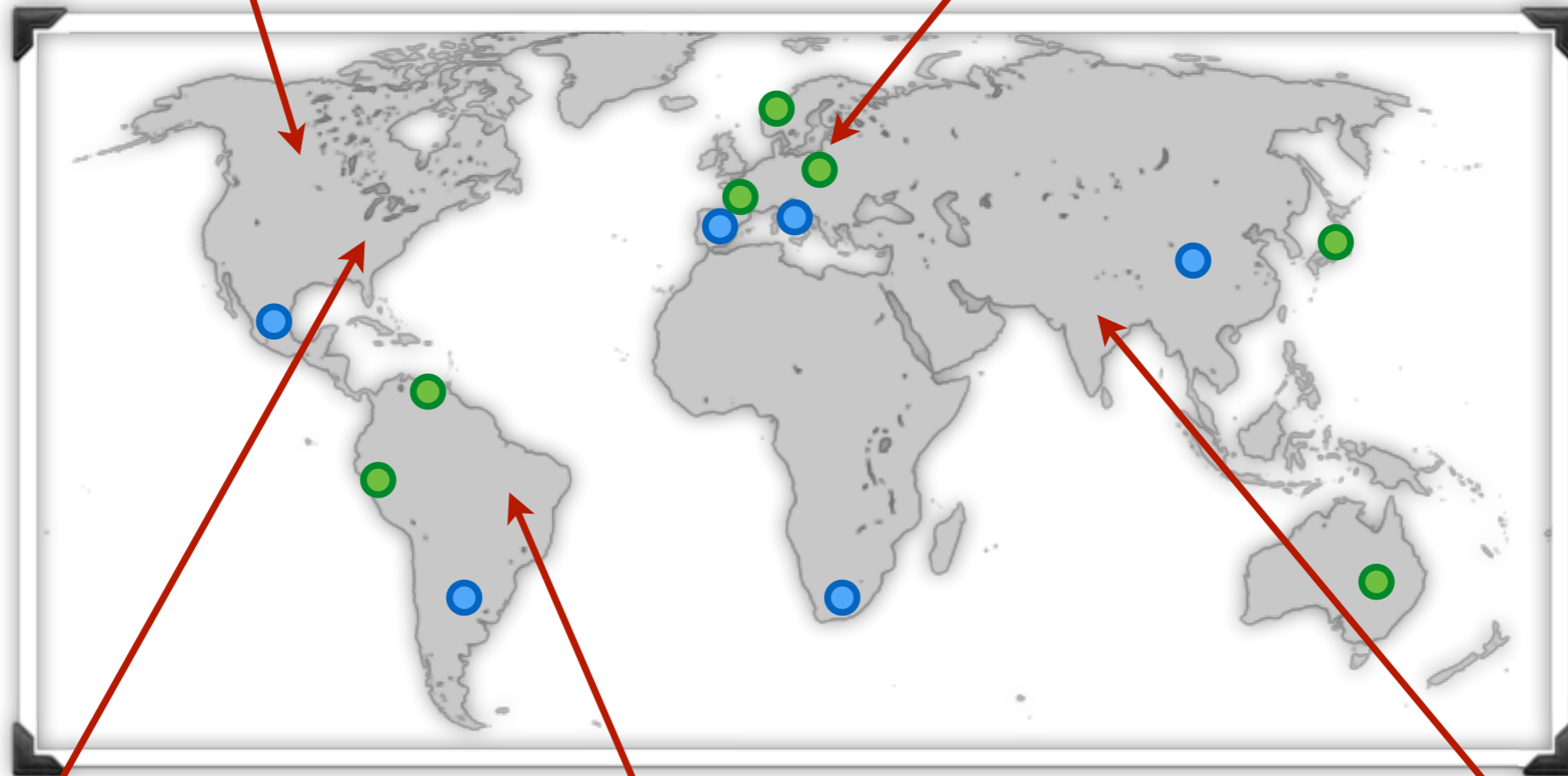
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# Introduction: E-voting evolution

**Canada** : Since 2004 at the Provincial level. (EVM and (later) Internet voting.)

**Estonia** : 2005, first legally binding vote using Internet.



But also :  
Norway  
France,  
Poland,  
...

Planned in :  
Mexico,  
China,  
Spain,  
...

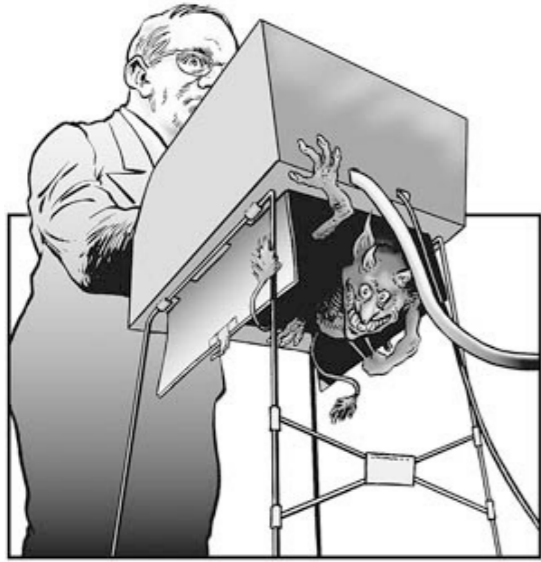
**USA** : EVM used for legally binding vote since 1996.

**India** : legally binding e-voting with EVM since 2002.

**Brazil** : legally binding e-vote with EVM since 2000.

# Introduction: E-voting, in theory

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**Electronic  
Voting Machines**



**Internet Voting**

Electronic Voting provides :

- **Conveniency**

Better accessibility, remote voting...

- **Efficiency**

Computers are tallying faster than humans.

- **Reliability**

Computers are more accurate than humans.

- **Trust**

Everything is ensured by cryptography.

# Introduction: E-voting, in theory



Coercion-Resistance

Verifiability



E-voting promises  
better security



Privacy

Eligibility



# Introduction: E-voting, in practice

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**But...**

Things can go wrong.



- Diebold Machines in the U.S.  
(Candice Hoke, 2008)
- Paperless EVM in India.  
(A. Halderman, R. Gonggrijp, 2010)

So, we need ~~proofs~~ !



automated  
proofs !



# Introduction: Tools can't make it !

Automated proofs often take place in the **symbolic approach**.

## Computational

More realistic  
model

**Strong  
guarantees**

Attacker modeled by probabilistic  
polynomial-time Turing Machine

**Tedious  
proofs**

cryptographic primitives as  
polynomial algorithms

## Symbolic

**Weaker  
guarantees**

Abstract  
model

Attacker modeled by  
deduction rules

cryptographic primitives  
as function symbols

**Easier proofs  
often automated**

There are **numerous tools** that can already perform automated proofs.

aKiSs

Tamarin

APTE

SPEC



AVISPA

Scyther

ProVerif



E-Voting protocols often include  
**too many** different  
cryptographic primitives !

# Introduction: A new tool ?

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**We needed something different !**

Something that could handle **equivalence-based properties**.

Then, the **rF\* type-checker** [Barthe et al. POPL'14] appears.  
(with the ability to verify equivalence-based properties)



We'll see that in details a bit later...

So we asked the question:

**Can type-checkers be used to verify  
(automatically) e-voting protocols**



# Introduction: Type-Systems

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But first, what are **type-systems** ?


- A **type** is a description that characterizes the expected form of the result of a computation.


If  $e$  is an expression, and we consider the following typing :


$e : \text{int}$

This is a **typing judgement** asserting that the value of  $e$  is of type int.

- **NB:** It will also checks consistency.

$2 + 1 : \text{int}$  

$\text{true} : \text{int}$  

$2 + \text{true} : \text{int}$  



# Introduction: Type-Systems

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- A **type-system** is a set of types and constructors used to describe the expected behavior of a program.
- The goal of the **type-checker** is to verify the different typing judgements and see whether they are true or not.

This is done by **using rules** from which it can derive the assertion.

- Basically, enforcing that  $e : \tau$  means that :
  - $e$  is well-typed, i.e. correctly derived of type  $\tau$  using the rules.
  - When  $e$  is evaluated, its value is described by  $\tau$ .

# Introduction: Type-Systems

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- What kind of rules ?

Function mapping  $\tau_1$  to  $\tau_2$  .

$$\frac{}{n : \text{int}}$$

$$\frac{\frac{e_1 : \tau_1 \rightarrow \tau_2}{e_1 e_2 : \tau_2} \quad e_2 : \tau_1}{e_1 e_2 : \tau_2}$$

- How does the type-checker to verify:  $2 + 1 : \text{int}$  ?

$$\frac{\frac{\frac{}{+ : \text{int} \rightarrow \text{int} \rightarrow \text{int}} \quad \frac{}{2 : \text{int}}}{+ 2 : \text{int} \rightarrow \text{int}} \quad \frac{}{1 : \text{int}}}{+ 2 1 : \text{int}}}$$



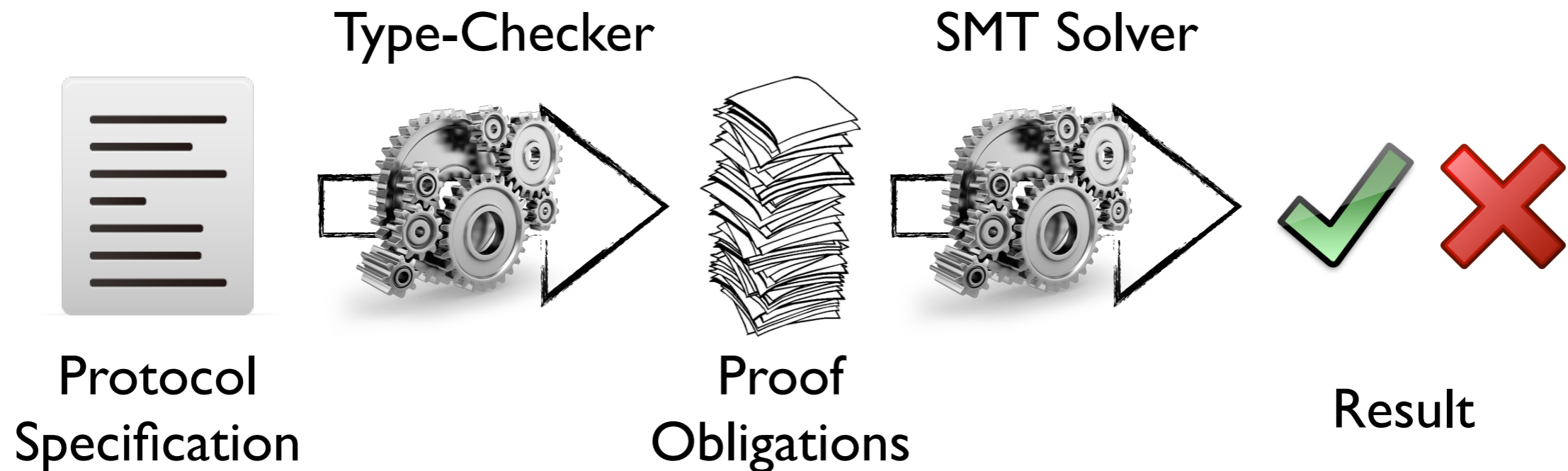
# Introduction: Type-Systems

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Of course, we need a type-system (a bit) more elaborated to be able to express electronic-voting protocols.

But this is not an issue...

How does it work ?



**Soundness result** : If a program type-checks, then it is safe.  
(In a presence of an arbitrary attacker.)

# Introduction: Type-Systems

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One interesting point :

SMT Solvers do not have any problem with AC-properties.

So...

Can type-checkers be used to verify  
(automatically) e-voting protocols



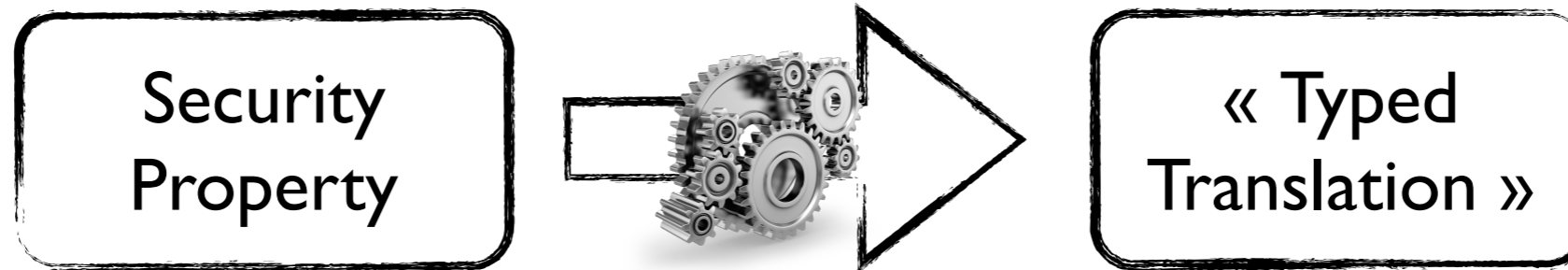
We decided to give it a go:

- Developing a **logical theory** to guide type-checker in proving interesting security properties like **privacy** and **verifiability**.
- Analyzing an **existing e-voting protocol** as an applied example.

# An Outline of what follows

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## I. Helios, our running example.



## II. Verifiability

1. Individual Verifiability
2. Universal Verifiability
3. End-to-end Verifiability

What's next, Doc ?



## III. Privacy

# Helios: Running example

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- Web-based electronic voting system

Try it at <https://vote.heliosvoting.org/> !

- Two existing versions : **homomorphic encryption** VS mixnets.
- Already used for several elections.

(Louvain-la-Neuve University, IACR\* Board, ...)

\*International Association for Cryptologic Research

# Helios (Simplified)

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Alice



$$\{v_A, r_A\}_{pk(E)}$$

Bob



Bulletin Board

$$\{v_B, r_B\}_{pk(E)}$$

Charlie



$$\{v_C, r_C\}_{pk(E)}$$

- $pk(E)$ : public key. The private one **is shared among trustees**.  
(All should collaborate to perform decryption of the tally.)
- The tally is computed using **homomorphic encryption** (El-Gamal).  
(The encrypted result is  $\{v_A + v_B + v_C, r_A + r_B + r_C\}_{pk(E)}$ .)
- Only the final result is encrypted, implying **vote privacy**.

# Helios (Simplified)

## A bit overly simplified...



$$\{v_A, r_A\}_{pk(E)} + \text{zkp}(v_A = 0 \text{ or } 1) \\ 0/1$$



Bulletin Board

$$\{v_B, r_B\}_{pk(E)} + \text{zkp}(v_B = 0 \text{ or } 1) \\ 0/1$$



$$\{v_C, r_C\}_{pk(E)} + \text{zkp}(v_C = 0 \text{ or } 1) \\ \text{100!}$$

- A **zero-knowledge proof** is attached to the ciphertext.

(It may also provide a proof to the correctness of the final tally.)

- Using ZKP, Helios satisfies **end-to-end verifiability**.



# Verifiability: Let's have an intuition of it !

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There are **three different** notions of **verifiability** :

- **Individual verifiability** :

Each voter can check that his ballot is on the bulletin board.

- **Universal verifiability** :

Any observer can verify that the announced result corresponds to the ballots published on the bulletin board.

- **End-to-end verifiability** :

The result matches with the votes intended by the voters.

# Individual Verifiability

How to prove individual verifiability using a type-system ?

$$\text{Voter}(id, v) = \begin{array}{ll} \text{assume } \text{Vote}(id, v); & \text{send}(net, b) \\ \text{let } r = \text{new}() \text{ in} & \text{let } bb = \text{recv}(net) \text{ in} \\ \text{let } b = \text{enc}(pk, v, r) \text{ in} & \text{if } b \in bb \text{ then} \\ \text{assume } \text{MyBallot}(id, v, b); & \text{assert } \text{VHappy}(id, v, bb) \end{array}$$

- We introduce three predicates : **Vote**, **MyBallot** and **VHappy**.
- We define when the predicate **VHappy** should be verified :

$$\text{assume } \text{VHappy}(id, v, b) \iff \text{Vote}(id, v) \wedge \exists b \in bb \text{ MyBallot}(id, v, b)$$

- We can prove that if such an annotated protocol type-checks...

**Then it guarantees individual verifiability !**

We used type-checker F\* [Swamy and al. ICFP'11]

# Universal Verifiability

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## How is made the tally ?

- A step of **sanitization** where we remove duplicates and invalid ballots from the bulletin board. (  $bb \mapsto vbb$  )

(Don't remove the honest votes !)

- A step of **counting** where all the votes contained in ballots listed in  $vbb$  are counted.

## We need some predicates...

GoodCount( $vbb, r$ )

GoodSan( $bb, vbb$ )

assume JudgeHappy( $bb, r$ )  $\iff \exists vbb$  (GoodSan( $bb, vbb$ )  $\wedge$  GoodCount( $vbb, r$ ))

# Universal Verifiability

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We now use these predicates to encode a Judge...

$$\begin{aligned} \text{Judge}(bb, r) = & \text{ let } vbb = \text{recv}(net) \text{ in} \\ & \text{ let } zkp = \text{recv}(net) \text{ in} \\ & \text{ if } vbb = \text{remDuplicates}(bb) \wedge \text{check\_zkp}(zkp, vbb, r) \text{ then} \\ & \text{ assert JudgeHappy}(bb, r) \end{aligned}$$

- We can prove that if such an annotated protocol type-checks...

**Then it guarantees universal verifiability !**

We used type-checker F\* [Swamy and al. ICFP'11]

# End-To-End Verifiability

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We repeat the same scheme we used for individual or universal verifiability.

**New predicate :**

assume  $\text{EndToEnd} \iff \exists bb, r, id_1, \dots, id_n, v_1, \dots, v_n.$

$(\text{JudgeHappy}(bb, r) \wedge \forall \text{Happy}(id_1, v_1, bb) \wedge \dots \wedge \forall \text{Happy}(id_n, v_n, bb))$

$\implies \exists rlist . r = \rho(rlist) \wedge \{|v_1, \dots, v_n|\} \subseteq_m rlist$

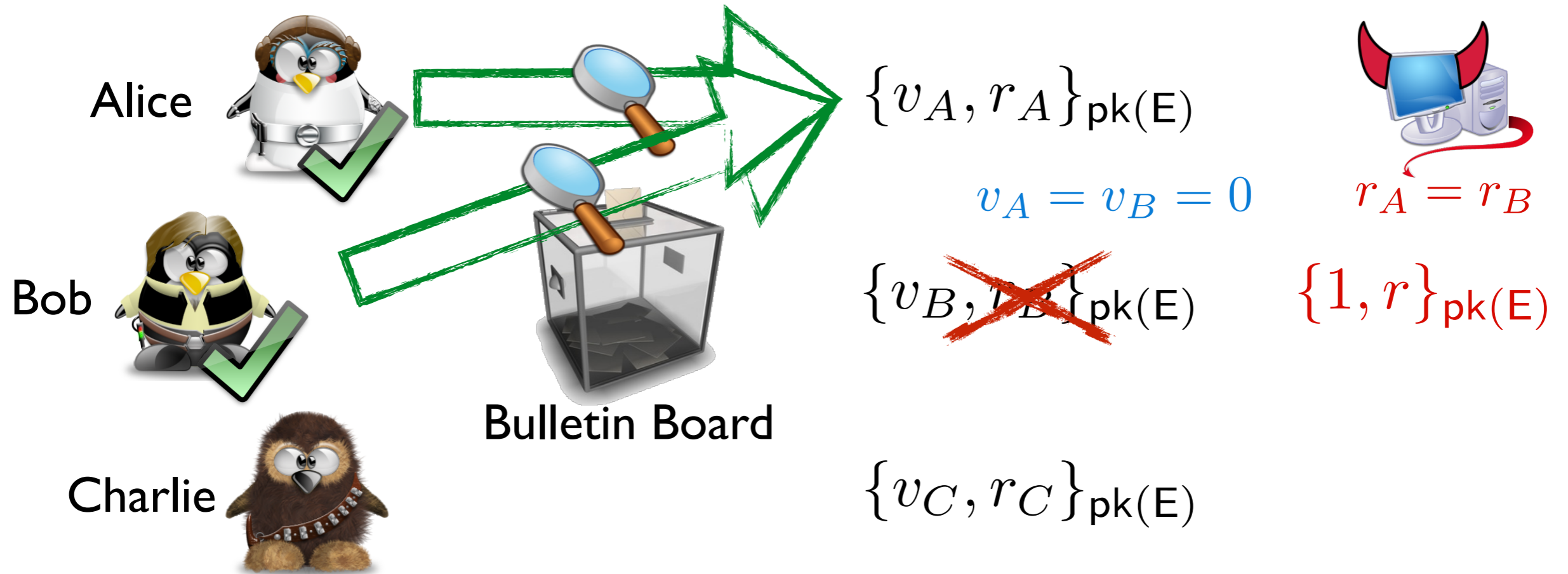
However this is **difficult to enforce** using a type-system.

**Nevertheless, does this definition ring any bell ?**

**Idea:** individual + universal = end-to-end

**But...**

# Clash-Attacks [Küsters et al. S&P'12]



- Alice and Bob will vote the same way.
- Machines of Alice and Bob are corrupted by Charlie.
- One vote can be discarded and replaced by another one...

**without Alice nor Bob noticing it !**

# NoClash Property

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Yes, another predicate !

$$\begin{aligned} \text{assume NoClash} &\iff \forall id_1, id_2, v_1, v_2, b . \\ &\quad \text{MyBallot}(id_1, v_1, b) \wedge \text{MyBallot}(id_2, v_2, b) \\ &\implies id_1 = id_2 \wedge v_1 = v_2 \end{aligned}$$

Two distinct honest voters will never consider the same ballot to contain their vote.

- We can prove that if such an annotated protocol type-checks...

**Then it guarantees that there are no clashes !**

We used type-checker F\* [Swamy and al. ICFP'11]

- Then, we have an interesting result :

**Individual Verif. + Universal Verif. + NoClash = End-to-End Verif.**

# Verifiability: Conclusion

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- We defined a way to **prove individual and universal verifiability** using type-systems ( $F^*$ ).
- We applied this methodology to Helios and verified that it holds.
- Using the NoClash predicate, we have a way to **prove end-to-end verifiability** using type-systems.
- Thanks to previous results, **it also holds for Helios**.



# Privacy: Definition

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What is **privacy** in an electronic-voting protocol ?

Idea 1: Should my vote remain secret ?



Well... We need to reveal votes in order to get the result...

Idea 2: Should no one see the difference if I change my vote ?



indistinguishable from



In the case of unanimity, the difference is kinda... obvious.

# Privacy: Definition

## Idea 3:

Should no one see the difference if **two honest voters** swap their votes ? 

Definition (S. Delaune, S. Kremer, M. Ryan, 2009)



Observational  
Equivalence

# Privacy: Using $rF^*$ to prove it

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- $rF^*$  can be used to enforce **observational equivalence**.
- To do so, it implements **relational refinements** which allows to reason about two protocol runs:

$$x : T\{|F|\}$$

- To specify that a value is the same in both runs, we use **eq-types**:

$$\text{eq } T \triangleq x : T\{|Lx = Rx|\}$$

Value of  $x$  in the first execution.

- All inputs/outputs should be typed with eq types.

# Privacy: Typing it ! (with rF\*)

$x : \text{bytes}\{|Lx = v_1 \wedge Rx = v_2|\}$

Alice  $v_A =$   
let  $b_A = \text{create\_Ballot}_A(v_A)$  in  
send( $c_A, b_A$ )

$x : \text{bytes}\{|Lx = v_2 \wedge Rx = v_1|\}$

Bob  $v_B =$   
let  $b_B = \text{create\_Ballot}_B(v_B)$  in  
send( $c_B, b_B$ )

- We add a corrupted voter, who also submits a ballot :  $b_C = \{v_C, r_C\}_{\text{pk}(E)}$
- The corrupted voter submits the same thing at each execution, thus :

$v_C$  is of type  $x : \text{eq bytes}$

- Finally, the result, after decryption, is :  $v_A + v_B + v_C$

Result is an eq bytes,  
we can publish it !

$v_1 + v_2 + v_C \approx v_2 + v_1 + v_C$

# Conclusion

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## Finally...

- New definitions for **individual, universal, end-to-end verifiability** and **privacy** that are enforceable by **mechanized type-based analysis**.
- A theorem proving that **end-to-end verifiability is enforced** by both individual and universal verifiability and no-clash property.
- Using  $F^*$  and  $rF^*$ , we proved the security properties of Helios.
- Can we apply it to other protocols ?

*That's all folks!*



*Questions?*