

# Analyse et Conception Formelles

## Lesson 7

### — Program verification methods

## Outline

- ① Testing
- ② Model-checking
- ③ Assisted proof
- ④ Static Analysis
- ⑤ A word about prototypes/models, accuracy, code generation

## Disclaimer

### Theorem 1 (Rice, 1953)

*Any nontrivial property about the language recognized by a Turing machine is undecidable.*

“The more you prove the less automation you have”

## The basics

### Definition 2 (Specification)

A complete description of the behavior of a software.

### Definition 3 (Oracle)

An oracle is a *mechanism* determining whether a test has passed or failed, w.r.t a specification.

### Definition 4 (Domain (of Definition))

The set of all possible inputs of a program, as defined by the specification.

## Notations

**Spec** the specification

**Mod** a formal model or formal prototype of the software

**Source** the source code of the software

**EXE** the binary executable code of the software

**D** the domain of definition of the software

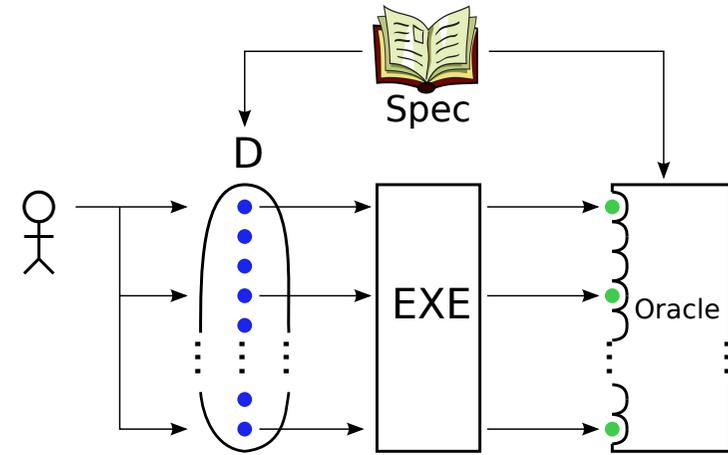
**Oracle** an oracle

**D<sup>#</sup>** an abstract definition domain

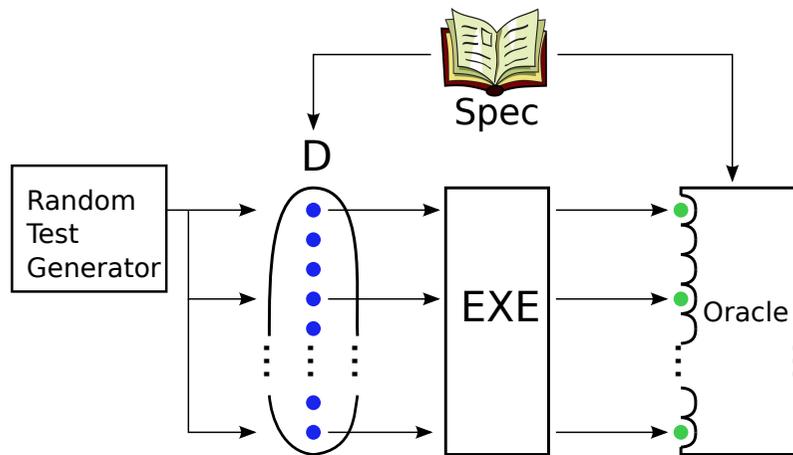
**Source<sup>#</sup>** an abstract source code

**Oracle<sup>#</sup>** an abstract oracle

## Testing principles

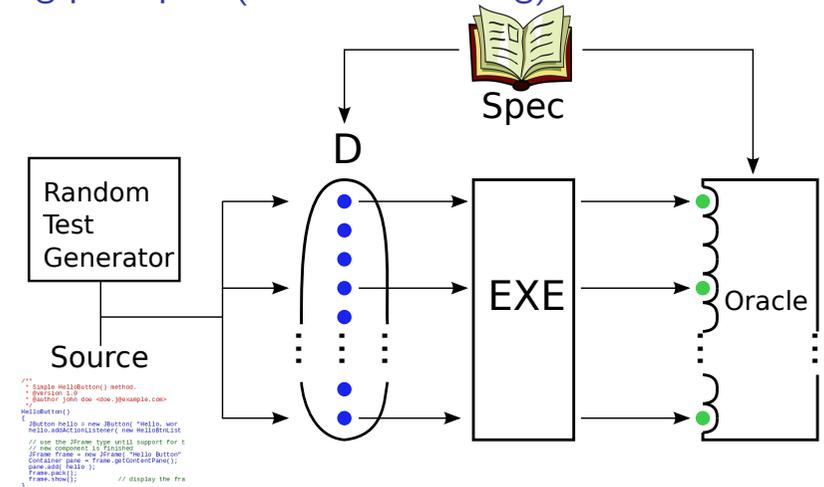


## Testing principles (random generators)



This is what Isabelle/HOL quickcheck does (and TP4Bis)

## Testing principles (white box testing)



```
/**
 * Sample HelloWorld() method.
 * @version 1.0 see www.gnu.org
 * @author Jimmie Dale Gosling
 */
HelloWorld() {
    HelloWorld() new HelloWorld("Hello, world!");
    HelloWorld() new HelloWorld("Hello, world!");
    // use the JFrame class until support for 1
    // new components is finished
    JFrame frame = new JFrame("Hello-World");
    getContentPane().add(new HelloWorld());
    setDefaultCloseOperation(WindowConstants.EXIT_ON_CLOSE);
    frame.pack(); // display the frame
    frame.setVisible(true);
}
```

### Definition 5 (Code coverage)

The degree to which the source code of a program has been tested, e.g. a *statement coverage* of 70% means that 70% of all the statements of the software have been tested at least once.

## Demo of white box testing in Evosuite

Objective: cover 100% of code (and raised exceptions)

### Example 6 (Program to test with Evosuite)

```
public static int Puzzle(int[] v, int i){
    if (v[i]>1) {
        if (v[i+2]==v[i]+v[i+1]) {
            if (v[i+3]==v[i]+18)
                throw new Error("hidden bug!");
            else return 1;}
        else return 2;}
    else return 3;
}
```

## Demo of white box testing in Evosuite

Generates tests for all branches (1, 2, 3, null array, hidden bug, etc)

One of the **generated** JUnit test cases:

```
@Test(timeout = 4000)
public void test5() throws Throwable {
    int[] intArray0 = new int[18];
    intArray0[1] = 3;
    intArray0[3] = 3;
    intArray0[4] = 21;    // an array raising hidden bug!

    try {
        Main.Puzzle(intArray0, 1);
        fail("Expecting exception: Error");
    } catch(Error e) {
        verifyException("temp.Main", e);
    }
}
```

## Testing, to sum up

### Strong and weak points

- + Done on the code → Finds real bugs!
- + Simple tests are easy to guess
- **Good** tests are not so easy to guess! (Recall TP0?)
- + Random and white box testing automate this task. May need an oracle: a formula or a reference implementation.
- Finds bugs but cannot prove a property
- + Test coverage provides (at least) a **metric** on software quality

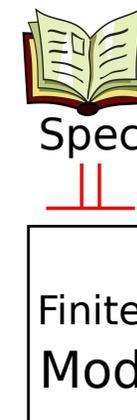
### Some tool names

Klee, SAGE (Microsoft), PathCrawler (CEA), Evosuite, many others ...

### One killer result

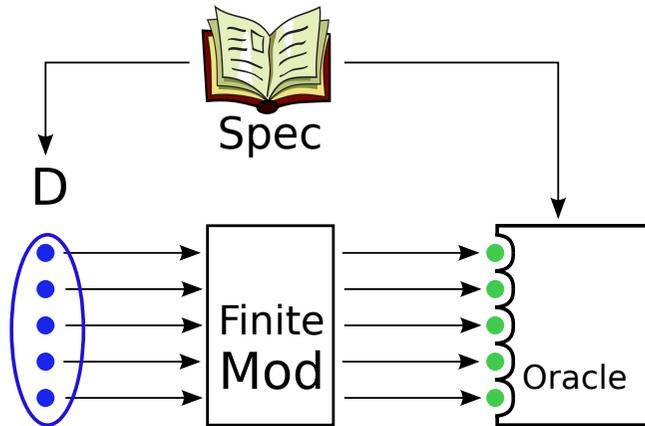
SAGE (running on 200 PCs/year) found 1/3 of security bugs in Windows 7  
<https://www.microsoft.com/en-us/security-risk-detection/>

## Model-checking principles



Where  $\models$  is the usual logical consequence. This property is **not** shown by doing a logical proof but by checking (by computation) that ...

## Model-checking principles (II)



Where D, Mod and Oracle are finite.

## Model-checking principle explained in Isabelle/HOL

Automaton `digiCode.as` and Isabelle file `cm7.thy`

### Exercise 1

Define the lemma stating that whatever the initial state, typing `A,B,C` leads execution to Final state.

### Exercise 2

Define the lemma stating that the only possibility for arriving in the Final state by typing three letters is to have typed `A,B,C`.

## Model-checking, to sum-up

### Strong and weak points

- + Automatic and efficient
- + Can find bugs and prove the property
  - For finite models only (e.g not on source code!)
- + Can deal with **huge** finite models ( $10^{120}$  states)  
More than the number of atoms in the universe!
- + Can deal with finite abstractions of infinite models e.g. source code
  - Incomplete on abstractions (but can find real bugs!)

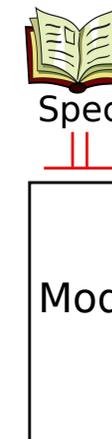
### Some tool names

SPIN, SMV, (bug finders) CBMC, SLAM, ESC-Java, Java path finder, ...

### One killer result

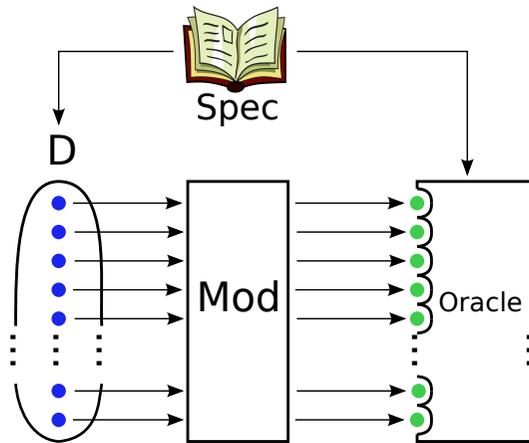
INTEL processors are commonly model-checked

## Assisted proof principles



Where  $\models$  is the usual logic consequence. This is proven directly on formulas Mod and Spec. This proof guarantees that...

## Assisted proof principles (II)



Where D, Mod, Oracle can be infinite.

## Assisted proof, to sum-up

### Strong and weak points

- + Can do the proof or find bugs (with counterexample finders)
- + Proofs can be **certified**
- Needs assistance
- For models/prototypes only (not on source nor on EXE)
- + Proof holds on the source code if it is generated from the prototype

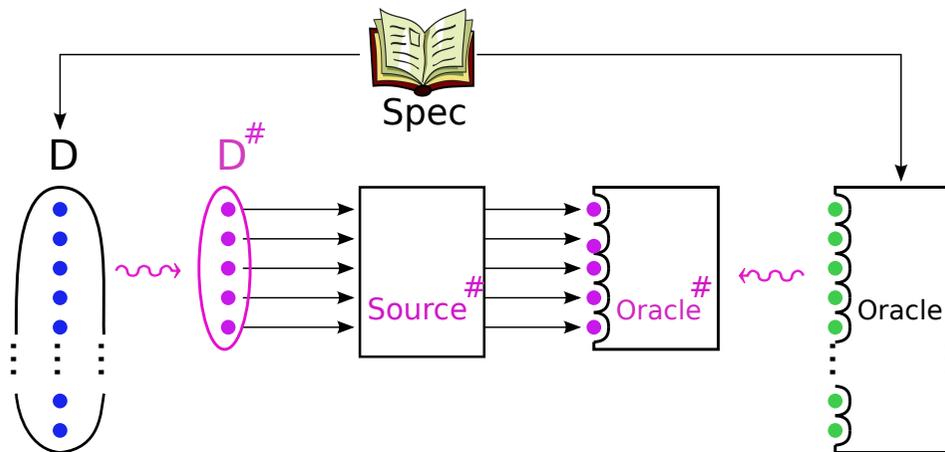
### Some tool names

B, Coq, Isabelle/HOL, ACL2, PVS, ... Why, Frama-C, ...

### One killer result

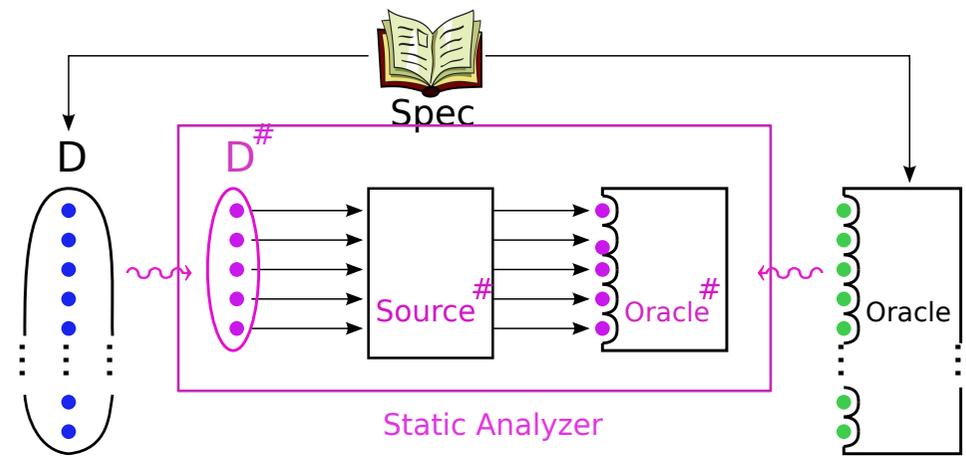
CompCert certified C compiler

## Static Analysis principles



Where abstraction  $\rightsquigarrow$  is a **correct** abstraction

## Static Analysis principles (II)



Where abstraction  $\rightsquigarrow$  is a **correct** abstraction

## Static Analysis principles – Abstract Interpretation (III)

The abstraction ' $\rightsquigarrow$ ' is based on the abstraction function  $\text{abs}:: D \Rightarrow D^\#$

Depending on the verification objective, precision of  $\text{abs}$  can be adapted

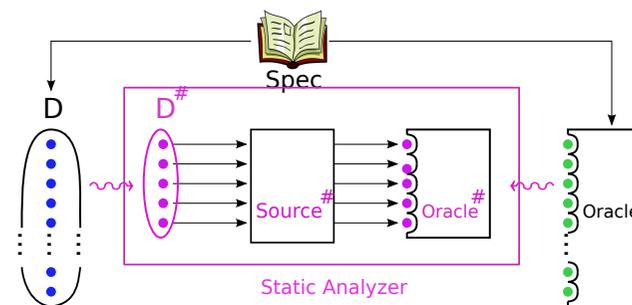
### Example 7 (Some abstractions of program variables for $D=\text{int}$ )

- (1)  $\text{abs}:: \text{int} \Rightarrow \{\perp, T\}$  where  $\perp \equiv$  "undefined" and  $T \equiv$  "any int"
- (2)  $\text{abs}:: \text{int} \Rightarrow \{\perp, \text{Neg}, \text{Pos}, \text{Zero}, \text{NegOrZero}, \text{PosOrZero}, T\}$
- (3)  $\text{abs}:: \text{int} \Rightarrow \{\perp\} \cup \text{Intervals on } \mathbb{Z}$

### Example 8 (Program abstraction with $\text{abs}$ (1), (2) and (3))

	(1)	(2)	(3)
$x := y+1;$	$x = \perp$	$x = \perp$	$x = \perp$
$\text{read}(x);$	$x = T$	$x = T$	$x = ]-\infty; +\infty[$
$y := x+10$	$y = T$	$y = T$	$y = ]-\infty; +\infty[$
$u := 15;$	$u = T$	$u = \text{Pos}$	$u = [15; 15]$
$x :=  x $	$x = T$	$x = \text{PosOrZero}$	$x = [0; +\infty[$
$u := x+u;$	$u = T$	$u = \text{Pos}$	$u = [15; +\infty[$

## Static Analysis: proving the correctness of the analyzer

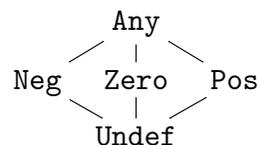


- Formalize semantics of Source language, *i.e.* formalize an  $\text{eval}$
- Formalize the oracle: BAD predicate on program states
- Formalize the abstract domain  $D^\#$
- Formalize the static analyser  $\text{SAn}:: \text{program} \Rightarrow \text{bool}$
- Prove correctness of  $\text{SAn}$ :  $\forall \mathbf{P}. \text{SAn}(\mathbf{P}) \longrightarrow (\neg \text{BAD}(\text{eval}(\mathbf{P})))$
- ... Relies on the proof that  $\rightsquigarrow$  is a correct abstraction

## Static Analysis principle explained in Isabelle/HOL

To abstract  $\text{int}$ , we define  $\text{absInt}$  as the abstract domain ( $D^\#$ ):

`datatype absInt = Neg | Zero | Pos | Undef | Any`



### Remark 1

Have a look at the concretization function (called *concrete*) defining sets of integers represented by abstract elements *Neg*, *Zero*, etc.

### Exercise 3

Define the function  $\text{absPlus}:: \text{absInt} \Rightarrow \text{absInt} \Rightarrow \text{absInt}$  (noted  $+\#$ )

### Exercise 4 (Prove that $+\#$ is a correct abstraction of $+$ )

$x \in \text{concrete}(x^a) \wedge y \in \text{concrete}(y^a) \longrightarrow (x + y) \in \text{concrete}(x^a +\# y^a)$

## Static Analysis, to sum-up

### Strong and weak points

- + Can prove the property
- + Automatic
- + On the source code
- Not designed to find bugs

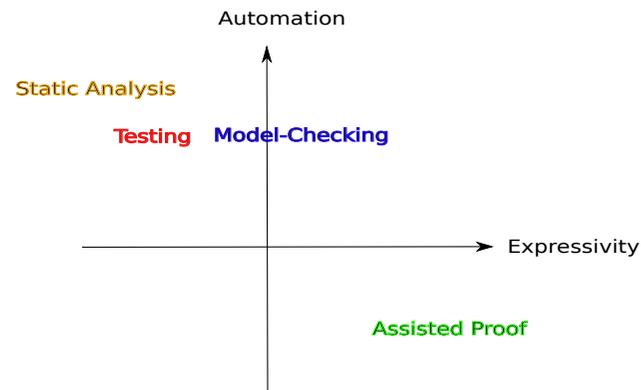
### Some tool names

Astree (Airbus), Polyspace, Sawja, Infer (Facebook)...

### One killer result

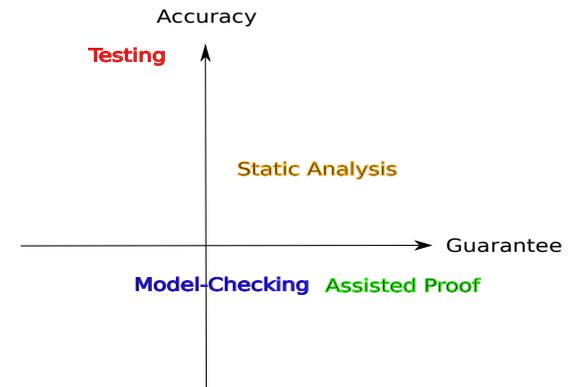
Astree was used to successfully analyze  $10^6$  lines of code of the Airbus A380 flight control system

## To sum-up on all presented techniques



- Some properties are too complex to be verified using a static analyzer
- Testing can only be used to check **finite** properties
- Model-checking deals only with finite models (to be built by hand)
- Static analysis is always fully automatic

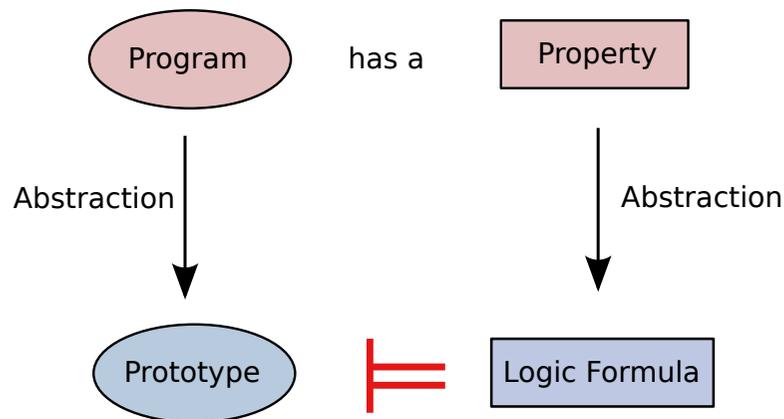
## To sum-up on all presented techniques



- Testing works on EXE, Static analysis on source code, others on models/prototypes
- Model-checking, assisted proof and static analysis have a similar guarantee level except that assisted proofs can be certified

## A word about models/prototypes

Program verification using “formal methods” relies on:



This is the case for model-checking and assisted proof.

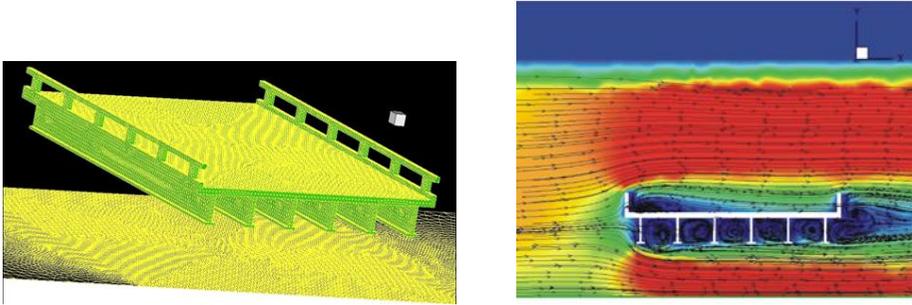
## Testing prototypes is a common practice in engineering



It is crucial for early detection of problems! Do you know Tacoma bridge?

## Testing prototypes is an engineering common practice (II)

More and more, prototypes are mathematical/numerical models



If the prototype is accurate: any detected problem is a **real** problem!

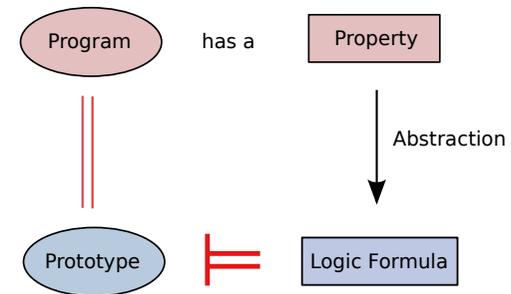
Problem on the prototype  $\rightarrow$  Problem on the real system

But in general, we do not have the opposite:

**No problem** on the prototype  $\nrightarrow$  **No problem** on the real system

## Why code exportation is a great plus?

Code exportation produces the program from the model itself!



Thus, we here have a **great bonus**: [TP5, TP67, TP89, CompCert]

**No problem** on the prototype  $\rightarrow$  **No problem** on the real system

If the exported program is not efficient enough it can, at least, be used as a reference implementation (an oracle) for testing the optimized one.

## About "Property $\xrightarrow{\text{Abstraction}}$ Logic formula"

This is the only remaining difficulty, and this step is **necessary**!

Back to TP0, it is very difficult for two reasons:

- 1 The "what to do" is not as simple as it seems
  - Many tests to write and what exactly to test?
  - How to be sure that no test was missing?
  - Lack of a **concise** and **precise** way to state the property  
Defining the property with a french text is too ambiguous!
- 2 The "how to do" was not that easy

Logic Formula = factorization of tests

- guessing **1** formula is harder than guessing **1** test
- guessing **1** formula is harder than guessing **10** tests
- guessing **1** formula is **not harder** than guessing **100** tests
- guessing **1** formula is **faster** than writing **100** tests (TP0 in Isabelle)
- proving **1** formula is **stronger** than writing **infinitely** many tests

## About formal methods and security

You **have to use formal methods** to secure your software  
... because hackers will use them to find new attacks!

Be serious, do hackers read scientific papers?  
or use academic stuff?

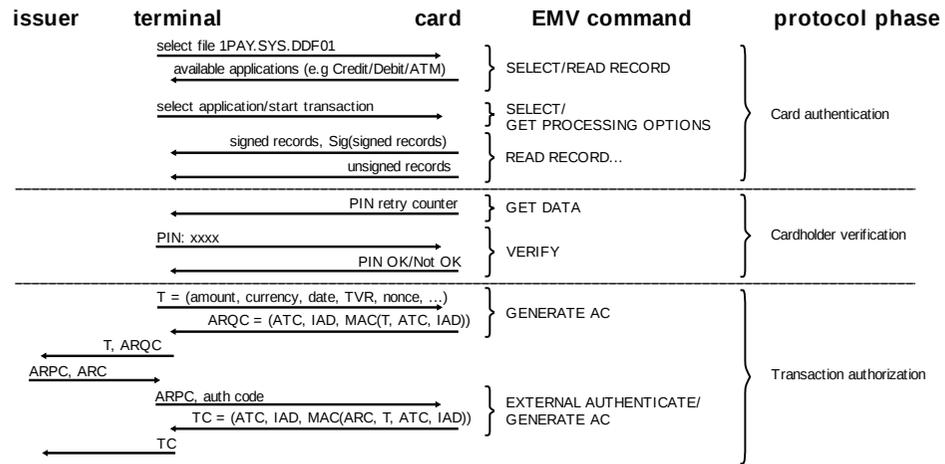
**Yes, they do!**

# Hackers do read scientific papers!

## Chip and PIN is Broken

Steven J. Murdoch, Saar Drimer, Ross Anderson, Mike Bond  
 University of Cambridge  
 Computer Laboratory  
 Cambridge, UK

Conference  
 Security and Privacy  
 2010  
 13 pages



# Hackers do read scientific papers!

## Chip and PIN is Broken

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They **revealed a weakness** in the payment protocol of EMV

They showed how to make a payment with a card without knowing the PIN



# Hackers do read scientific papers!

## When Organized Crime Applies Academic Results A Forensic Analysis of an In-Card Listening Device

Houda Ferradi, Rémi Géraud, David Naccache, and Assia Tria

<sup>1</sup> École normale supérieure  
 Computer Science Department  
 45 rue d'Ulm, F-75230 Paris CEDEX 05, France

Journal of  
 Cryptographic Engineering  
 2015



# Hackers do read scientific papers!

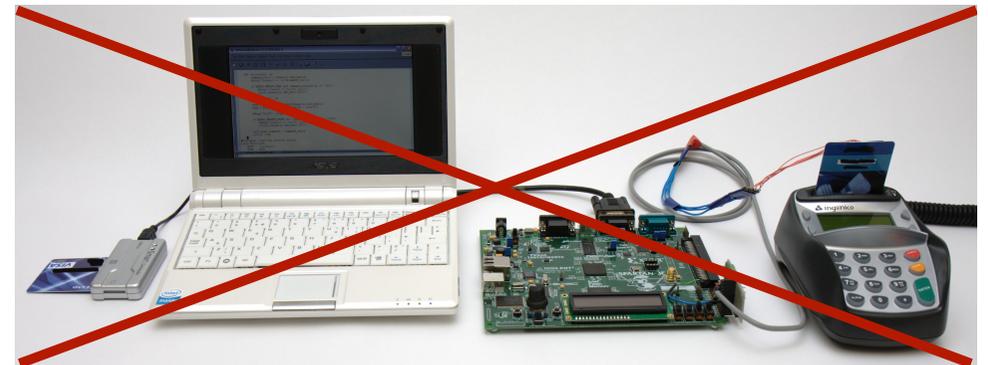
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Criminals used the attack of Murdoch & al. but not:



## About formal methods and security

You **have to use formal methods** to secure your software  
... because hackers will use them to find new attacks!

(1 formula) + (counter-example generator)  $\rightarrow$  attack!

- Fuzzing of implementations using model-checking
- Finding bugs (to exploit) using white-box testing
- Finding errors in protocols using counter-example gen. (e.g. TP89)

$\Rightarrow$  You **will have to formally prove security** of your software!