

Master SIF - REP (2-3/20) Image acquisition and Projection Models

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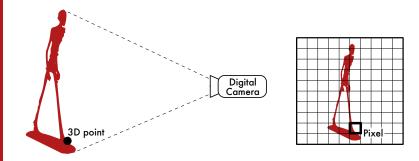
A Reference



What is a projection model?

Projection Model

Find the relationship between a point in the 3D world and the corresponding pixel in an image.





Photodetector

Acquisition and Projection

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Projection Model

Projection Mode Omnidirectional projection Sensor that converts a certain electromagnetic activity into a electrical current.

Usually a **semiconductor** that transforms a light photons into electrons only for a certain band of energy. The number of electrons collected is proportional to the quantity of light that is received.

One photodiode per Red/Green/Blue channel:

- CCD: charge-coupled device
- CMOS: complementary metal-oxide-semiconductor

One photodiode for all Red/Green/Blue channels:

Feoven





From photodiode to Pixel

Acquisition and Projection

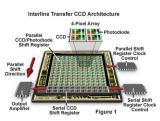
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A Pixel is a picture element

Active-Pixel Sensor (APS) associate to each pixel, one (or several) photodetector and an active amplifier.



APS based on CCD



How to capture the light?

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The issue is not only to capture the light intensity, but also the light direction

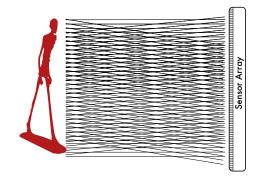




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Pinhole capture = Perspective projection

Acquisition an Projection

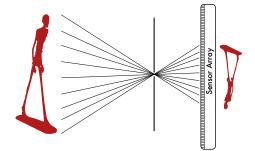
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Filter the light with a hole, in order to have, at most, one ray per 3D point in the scene.





An old idea

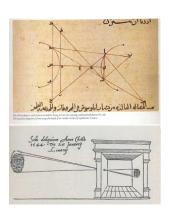
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- Ibn Al-Haytham (965-1039)
- Leonardo Da Vinci (1514)
- Johann Zahn (1685)





Aperture and focal length

Acquisition and Projection

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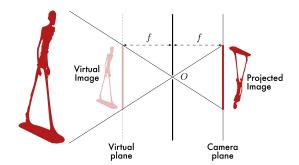
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- The **aperture** is the hole (pinhole) center *O* of the camera through which the rays are passing
- ullet The **focal length** f is the distance between the aperture and the camera plane





Aperture's size

Acquisition and Projection

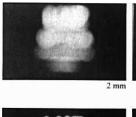
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It controls the trade-off between the *quantity of light* and the *uniqueness of the ray direction* per sensor.









[Wikipedia]

In the following, we consider that it is a point.



Focal length

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Projection Mode

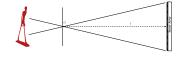
Perspective Projection Model

Omnidirectional projection

It controls the angle of view of the camera (and thus the zoom).







Camera objectives:

- Small f: wide angle
- High f: zoom



$$f=28\ \mathrm{mm}$$



$$f = 50 \text{ mm}$$



$$f = 70 \text{ mm}$$



$$f = 210 \text{ mm}$$

[Wikipedia]



Three coordinate systems

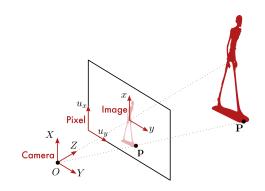
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3D point:

$$\mathbf{P} = \left[\begin{array}{c} X \\ Y \\ Z \end{array} \right]$$

Projected point:

$$\mathbf{p} = \left[\begin{array}{c} x \\ y \end{array} \right]$$

Pixel:

$$\mathbf{u} = \begin{bmatrix} u_x \\ u_y \end{bmatrix}$$



From Camera to Image coordinates

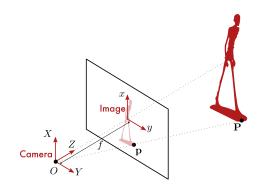
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The relationship between ${\bf P}$ and ${\bf p}$ is given by:

$$\begin{cases} x = ? \\ y = ? \end{cases}$$



From Camera to Image coordinates

Acquisition and Projection

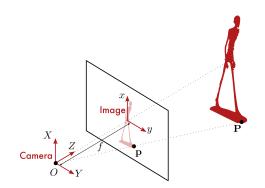
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The relationship between ${\bf P}$ and ${\bf p}$ is given by:

$$\begin{cases} x = f \frac{X}{Z} \\ y = f \frac{Y}{Z} \end{cases}$$



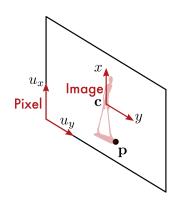
From Image to Pixel coordinates

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Camera center:

$$\mathbf{c} = \left[\begin{array}{c} x_0 \\ y_0 \end{array} \right]$$

Resolution (pixel.mm $^{-1}$):

$$\mathbf{k} = \left[egin{array}{c} k_x \ k_y \end{array}
ight]$$

Pixel coordinates:

$$\begin{cases} u_x = k_x(x+x_0) \\ u_y = k_y(y+y_0) \end{cases}$$



Homogeneous Coordinates

Acquisition an Projection Represent a n-dimensional coordinate with an n+1-dimension vector:

$$\left[\begin{array}{c} v_1 \\ \vdots \\ v_n \end{array}\right] \to \left[\begin{array}{c} v_1 \\ \vdots \\ v_n \\ 1 \end{array}\right]$$

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Homogeneous divide:

$$\begin{bmatrix} v_1 \\ \vdots \\ v_n \\ w \end{bmatrix} \to \begin{bmatrix} v_1/w \\ \vdots \\ v_n/w \\ 1 \end{bmatrix}$$

Two vectors are said **homogeneous** if their homogeneous divide is equal, e.g.,

$$\begin{bmatrix} 2\\3\\1 \end{bmatrix} \equiv \begin{bmatrix} 4\\6\\2 \end{bmatrix} \equiv \begin{bmatrix} 6\\9\\3 \end{bmatrix}$$



From Camera to Pixel coordinates

Acquisition and Projection

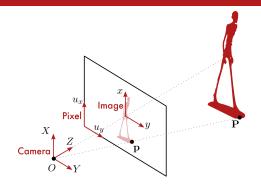
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$$\begin{bmatrix} u_x \\ u_y \\ 1 \end{bmatrix} \equiv \begin{bmatrix} k_x f X + k_x x_0 Z \\ k_y f Y + k_y y_0 Z \\ Z \end{bmatrix} = \begin{bmatrix} k_x f & 0 & k_x x_0 \\ 0 & k_y f & k_y y_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

Intrinsic Matrix \mathbf{K}



Intrinsic matrix

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The intrinsic matrix is given by:

$$\mathbf{K} = \begin{bmatrix} k_x f & s & k_x x_0 \\ 0 & k_y f & k_y y_0 \\ 0 & 0 & 1 \end{bmatrix}$$

with

- s: skew parameter (in pixels)
- (x_0, y_0) : principal point coordinates (in mm)
- f : focal length (in mm)
- k_x , k_y : vertical, horizontal resolution (in pixel.mm⁻¹)

Play with it:

http://ksimek.github.io/2013/08/13/intrinsic/



World coordinates

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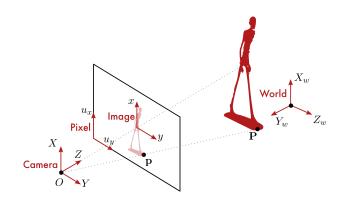
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The point P might be expressed in the world coordinate system:



Change of coordinate system

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$$\begin{array}{c|c} X & Z & R \\ \hline X & Z & World \\ \hline Y & Y_w & Z_w \end{array}$$

If (α,β,γ) are the euler angles of the rotation around respectively the (X_w,Y_w,Z_w) axis, the rotation matrix is given by:

$$\mathbf{R} = \left[\begin{array}{ccc} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{array} \right] \left[\begin{array}{ccc} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \gamma \end{array} \right] \left[\begin{array}{ccc} 1 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha \\ 0 & \sin \alpha & \cos \alpha \end{array} \right]$$

If the camera center O coordinates expressed in the world system are given by ${\bf t}$, the coordinate system change is expressed as:

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \mathbf{R} \left(\begin{bmatrix} X_w \\ Y_w \\ Z_w \end{bmatrix} - \mathbf{t} \right) = \underbrace{\begin{bmatrix} \mathbf{R} & -\mathbf{Rt} \end{bmatrix}}_{\text{Extrinsic Matrix } \mathbf{E}} \begin{bmatrix} X_w \\ Y_w \\ Z_w \\ 1 \end{bmatrix}$$

Play with it: http://ksimek.github.io/2012/08/22/extrinsic/



From World to Pixel coordinates

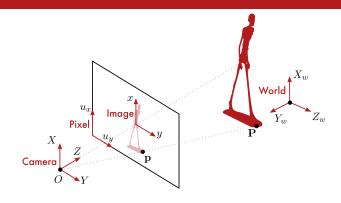
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$$\left[\begin{array}{c} u_x \\ u_y \\ 1 \end{array}\right] \equiv \left[\begin{array}{ccc} k_x f & 0 & k_x x_0 \\ 0 & k_y f & k_y y_0 \\ 0 & 0 & 1 \end{array}\right] \left[\begin{array}{c} \mathbf{R} & -\mathbf{Rt} \end{array}\right] \left[\begin{array}{c} X_w \\ Y_w \\ Z_w \\ 1 \end{array}\right] = \mathbf{KE} \left[\begin{array}{c} X_w \\ Y_w \\ Z_w \\ 1 \end{array}\right]$$



Perspective projection's properties

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- Distant objects look smaller (exercice)
- Lines project to lines (exercice)
- Parallel lines are in general no longer parallel (exercice)
- Parallel lines meet at a vanishing point
- Angles are not preserved
- 3D points can be retrieved from camera motion (cf. Epipolar Geometry)



Pose estimation

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Unknown rotations and positions estimated thanks to known world coordinate positions and their associated pixel positions

$$\begin{bmatrix} u_x \\ u_y \\ 1 \end{bmatrix} \equiv \begin{bmatrix} k_x f & 0 & k_x x_0 \\ 0 & k_y f & k_y y_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{R} & -\mathbf{Rt} \end{bmatrix} \begin{bmatrix} X_w \\ Y_w \\ Z_w \\ 1 \end{bmatrix}$$

Algorithms

- Find many matches
- And minimize $\min_{(\mathbf{K},\mathbf{R},\mathbf{t})} \sum_i r_i(\mathbf{K},\mathbf{R},\mathbf{t})^2 = \min_{(\mathbf{K},\mathbf{R},\mathbf{t})} \sum_i ||p_i^{obs} p_i^{est}(\mathbf{K},\mathbf{R},\mathbf{t})||_2^2$
- Gauss-Newton Solver
 - \bullet By first finding inital values $(\mathbf{K}_0,\mathbf{R}_0,\mathbf{t}_0)$
 - Then iteratively refine $(\mathbf{K}_{s+1}, \mathbf{R}_{s+1}, \mathbf{t}_{s+1}) = (\mathbf{K}_{s}, \mathbf{R}_{s}, \mathbf{t}_{s}) + \delta(\mathbf{K}, \mathbf{R}, \mathbf{t})$
 - where $\delta(\mathbf{K}, \mathbf{R}, \mathbf{t}) = -(\mathbf{J}_r^T \mathbf{J}_r)^{-1} \mathbf{J}_r^\top r$
- Levenberg-Marquardt



Pose estimation applications

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- Calibration
- Augmented reality
- Video summary



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What is an omnidirectional image?

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Definition

An image that represents the light activity arriving at a point (the image center) from every direction (360° field of view).

Applications:

 Virtual reality Head-Mounted Display (HDM)





- Free viewpoint Television
 More than 1 million videos uploaded
 on Youtube in 1 year
- Robotics





Omnidirectional capture?

Omnidirectional projection

The main issue is to cover a wide angle of view (360°)

Multiple perspective projections by several small degree of view cameras (180° or 360° field of view)





- A curved mirror + one single perspective camera (180° field of view)
- Fish-eye lenses (180° field of view)

In the following, we present the two last ones.

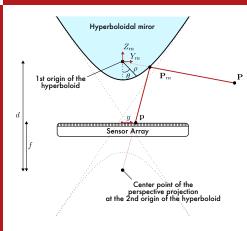


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Projection on the mirror of equation $\rho = \frac{a}{1 + e \cos \theta}$:

Perspective projection on the sensor array:

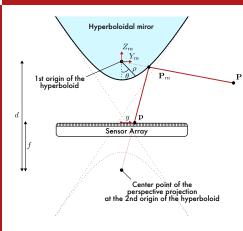


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Projection on the mirror of equation $\rho = \frac{a}{1 + e \cos \theta}$:

$$\mathbf{P}_{m} = \frac{\mathbf{P}}{||\mathbf{P}||} \cdot \rho$$

$$\begin{bmatrix} X_{m} \\ Y_{m} \\ Z_{m} \end{bmatrix} = \frac{\rho}{\sqrt{X^{2} + Y^{2} + Z^{2}}} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}.$$

Perspective projection on the sensor array:



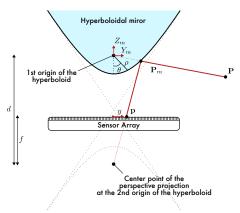
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Projection on the mirror of equation $\rho = \frac{a}{1 + e \cos \theta}$:

$$\mathbf{P}_{m} = \frac{\mathbf{P}}{||\mathbf{P}||} \cdot \rho$$

$$\begin{bmatrix} X_{m} \\ Y_{m} \\ Z_{m} \end{bmatrix} = \frac{\rho}{\sqrt{X^{2} + Y^{2} + Z^{2}}} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}.$$

Perspective projection on the sensor array:

$$\begin{cases} x = f \frac{X_m}{Z_m + d} \\ y = f \frac{Y_m}{Z_m + d} \end{cases}$$



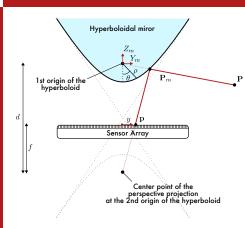
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Projection on the mirror of equation $\rho = \frac{a}{1 + e \cos \theta}$:

$$\mathbf{P}_{m} = \frac{\mathbf{P}}{||\mathbf{P}||} \cdot \rho$$

$$\begin{bmatrix} X_{m} \\ Y_{m} \\ Z_{mn} \end{bmatrix} = \frac{\rho}{\sqrt{X^{2} + Y^{2} + Z^{2}}} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}.$$

Perspective projection on the sensor array:

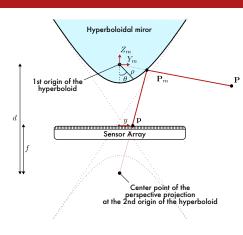
$$\begin{cases} x = f \frac{X_m}{Z_m + d} \\ y = f \frac{Y_m}{Z_m + d} \end{cases}$$

And:

$$d = \frac{2ae}{1-e^2}$$
 and $\cos(\theta) = \frac{Z}{||\mathbf{P}||}$,



Omnidirectional projection



Projection on the mirror of equation $\rho = \frac{a}{1+e\cos\theta}$:

$$\mathbf{P}_{m} = \frac{\mathbf{P}}{||\mathbf{P}||} \cdot \rho$$

$$\begin{bmatrix} X_{m} \\ Y_{m} \\ Z \end{bmatrix} = \frac{\rho}{\sqrt{X^{2} + Y^{2} + Z^{2}}} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}.$$

Perspective projection on the sensor array:

$$\begin{cases} x = f \frac{X_m}{Z_m + d} \\ y = f \frac{Y_m}{Z_m + d} \end{cases}$$

And:

And:
$$d = \frac{2ae}{1-e^2}$$
 and $\cos(\theta) = \frac{Z}{||\mathbf{P}||}$,

$$\mathbf{p} = \left[\frac{\frac{1 - e^2}{1 + e^2} fX}{\frac{2e}{1 + e^2} \sqrt{X^2 + Y^2 + Z^2} + Z}, \frac{\frac{1 - e^2}{1 + e^2} fY}{\frac{2e}{1 + e^2} \sqrt{X^2 + Y^2 + Z^2} + Z} \right]^{\top}$$



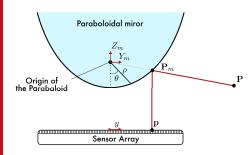
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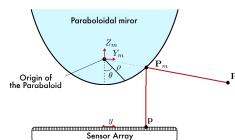


Projection on the mirror of equation $\rho = \frac{a}{1+\cos\theta}$:

Orthogonal projection on the sensor array:



Omnidirectional projection



Projection on the mirror of equation $\rho = \frac{a}{1 + \cos \theta}$:

$$\mathbf{P}_{m} = \frac{\mathbf{P}}{||\mathbf{P}||} \cdot \rho$$

$$\begin{bmatrix} X_{m} \\ Y \end{bmatrix} = \rho \begin{bmatrix} X \\ Y \end{bmatrix}$$

$$\begin{bmatrix} X_m \\ Y_m \\ Z_m \end{bmatrix} = \frac{\rho}{\sqrt{X^2 + Y^2 + Z^2}} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}.$$

Orthogonal projection on the sensor array:



Catadioptric cameras: Para-catadioptric

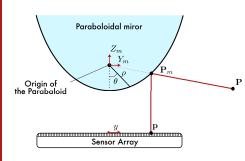
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Projection on the mirror of equation $\rho = \frac{a}{1+\cos\theta}$:

$$\mathbf{P}_{m} = \frac{\mathbf{P}}{||\mathbf{P}||} \cdot \rho$$

$$\begin{bmatrix} X_{m} \\ Y_{m} \\ Z_{m} \end{bmatrix} = \frac{\rho}{\sqrt{X^{2} + Y^{2} + Z^{2}}} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}.$$

Orthogonal projection on the sensor array:

$$\left\{ \begin{array}{l} x = X_m \\ y = Y_m \end{array} \right.$$
 And $\cos(\theta) = \frac{Z}{||\mathbf{P}||}$,

In the image coordinate:



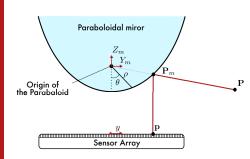
Catadioptric cameras: Para-catadioptric

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Projection on the mirror of equation $\rho = \frac{a}{1 + \cos \theta}$:

$$\mathbf{P}_{m} = \frac{\mathbf{P}}{||\mathbf{P}||} \cdot \rho$$

$$\begin{bmatrix} X_{m} \\ Y_{m} \\ Z_{m} \end{bmatrix} = \frac{\rho}{\sqrt{X^{2} + Y^{2} + Z^{2}}} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}.$$

Orthogonal projection on the

sensor array:
$$\left\{ \begin{array}{l} x = X_m \\ y = Y_m \end{array} \right.$$
 And $\cos(\theta) = \frac{Z}{||\mathbf{P}||}$,

In the image coordinate:

$$\mathbf{p} = \left[\frac{aX}{\sqrt{X^2 + Y^2 + Z^2} + Z}, \frac{aY}{\sqrt{X^2 + Y^2 + Z^2} + Z} \right]^{\top}$$



Fisheye lens

Projection

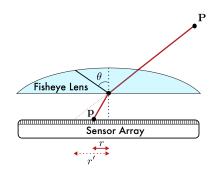
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Radial distortion of the lens:

$$r \neq r'$$

Example of radial distortion

[F01]:

$$r' = \frac{k_1 r}{1 - k_2 r^2}$$

Usually, this distortion reads [C07]:

$$r = f(\theta)$$

[F01] A. W. Fitzgibbon. Simultaneous linear estimation of multiple view geometry and lens distortion. In CVPR (1), pages 125-132, 2001.

[CO7] J. Courbon, Y. Mezouar, L. Eck, and P. Martinet. A generic fisheye camera model for robotic applications. In IROS, pages 16838ħ1688, 2007



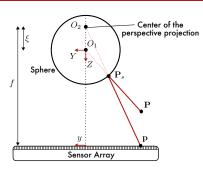
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Projection on the sphere of center O_1 :

Perspective projection of center O_2 on the sensor array:

In the image coordinates:





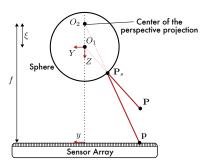
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Projection on the sphere of center O_1 :

$$egin{aligned} \mathbf{P}_s &= rac{\mathbf{P}}{||\mathbf{P}||} \ egin{aligned} X_s \ Y_s \ Z_o \end{aligned} &= rac{1}{\sqrt{X^2 + Y^2 + Z^2}} \left[egin{array}{c} X \ Y \ Z \end{array}
ight]. \end{aligned}$$

Perspective projection of center O_2 on the sensor array:

In the image coordinates:



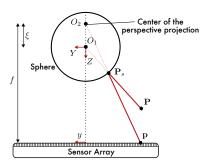
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Projection on the sphere of center O_1 :

$$egin{align*} \mathbf{P}_s &= rac{\mathbf{P}}{||\mathbf{P}||} \ egin{align*} X_s \ Y_s \ Z_c \ \end{bmatrix} &= rac{1}{\sqrt{X^2 + Y^2 + Z^2}} egin{bmatrix} X \ Y \ Z \ \end{bmatrix}.$$

Perspective projection of center O_2 on the sensor array:

$$\begin{cases} x = f \frac{X_s}{Z_s + \xi} \\ y = f \frac{Y_s}{Z_s + \xi} \end{cases}$$

In the image coordinates:



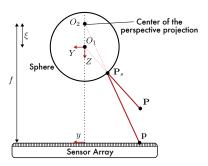
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Projection on the sphere of center O_1 :

$$\begin{array}{c|c} \mathbf{P}_s = \frac{\mathbf{P}}{||\mathbf{P}||} \\ \begin{bmatrix} X_s \\ Y_s \\ Z \end{bmatrix} = \frac{1}{\sqrt{X^2 + Y^2 + Z^2}} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}.$$

Perspective projection of center O_2 on the sensor array:

$$\begin{cases} x = f \frac{X_s}{Z_s + \xi} \\ y = f \frac{Y_s}{Z_s + \xi} \end{cases}$$

In the image coordinates:

$$\mathbf{p} = \left[\frac{fX}{\xi \sqrt{X^2 + Y^2 + Z^2} + Z}, \frac{fY}{\xi \sqrt{X^2 + Y^2 + Z^2} + Z} \right]^{\top}$$



Example of Captured 360° image

Acquisition and Projection

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Omnidirectional projection

Reference

Catadioptric Cameras





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[S.K. Nayar and V.N. Peri, "Folded Catadioptric Cameras," Panoramic Vision, pp. 103-119, R.,
Springer-Verlag, Apr. 2001.]

[S. Baker and S.K. Nayar, ,"Single Viewpoint Catadioptric Cameras," Panoramic Vision, pp. 39-71, R.,
Springer-Verlag, Apr. 2001.]

[S. Baker and S.K. Nayar, "A Theory of Single-Viewpoint Catadioptric Image Formation," International Journal
on Computer Vision, Vol. 35, No. 2, pp. 175-126, Nov. 1999.]
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Example of Captured 360° image

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Line projections

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Let us take a line of equation

$$\begin{cases} X = a_x t + X_0 \\ Y = a_y t + Y_0 \\ Z = a_z t + Z_0 \end{cases}$$

If
$$k_x = k_y = f = 1$$
 and $x_0 = y_0 = 0$. We can write

$$\left[\begin{array}{c} u_x \\ u_y \end{array} \right] = \left[\begin{array}{c} \frac{a_x t + X_0}{\xi \sqrt{(a_x t + X_0)^2 + (a_y t + Y_0)^2 + (a_z t + Z_0)^2 + a_z t + Z_0}} \\ \frac{a_y t + Y_0}{\xi \sqrt{(a_x t + X_0)^2 + (a_y t + Y_0)^2 + (a_z t + Z_0)^2} + a_z t + Z_0} \end{array} \right]$$

The projection of lines are curves in the spherical image.



Parallel lines projections

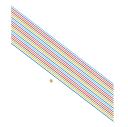
Acquisition and Projection

Projection Mode

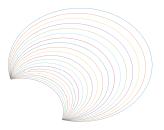
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Parallel lines in the 3D space



Projection in the spherical camera

The vanishing points are visible in the scene.



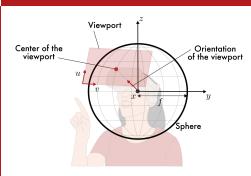
Viewport rendering

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The projection of \mathbf{P}_s on the viewport is:

The pixels of the spherical image are placed on the sphere $\mathbf{P}_s = [x,y,z]^\top$

The viewport is oriented towards a direction whose rotation matrix is given by ${\bf R}.$

The center of the viewport is at (c_u,c_v) , with corresponding resolutions (k_u,k_v) .

[De Simone, Francesca et al. "Geometry-driven quantization for omnidirectional image coding." PCS (2016).]



Viewport rendering

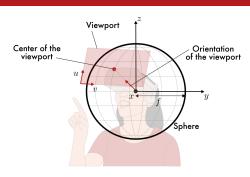
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The pixels of the spherical image are placed on the sphere $\mathbf{P}_s = [x,y,z]^{\top}$

The viewport is oriented towards a direction whose rotation matrix is given by ${\bf R}$.

The center of the viewport is at (c_u, c_v) , with corresponding resolutions (k_u, k_v) .

The projection of P_s on the viewport is:

$$\begin{bmatrix} u \\ v \\ 1 \end{bmatrix} \equiv \begin{bmatrix} k_u c_u & 0 & k_u f \\ k_v c_v & k_v f & 0 \\ 1 & 0 & 0 \end{bmatrix} \mathbf{R} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

[De Simone, Francesca et al. "Geometry-driven quantization for omnidirectional image coding." PCS (2016).]



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