

# Discovering habits with periodic patterns

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M2 SIF – DMV course

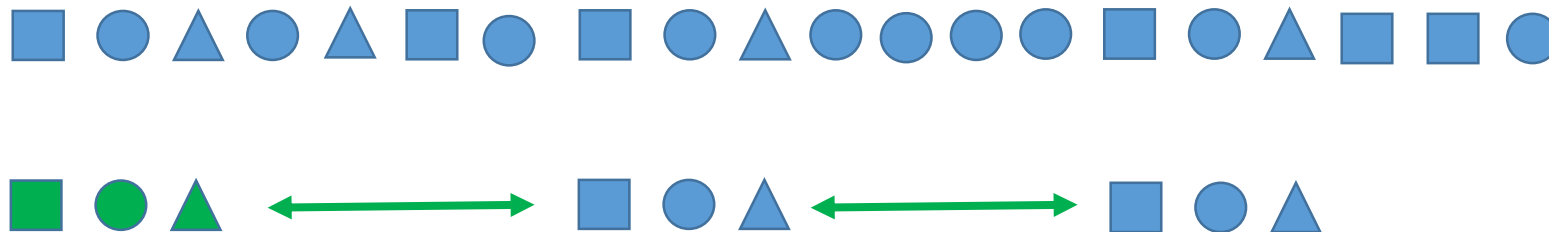
2022-2023

# Motivation

- Pattern mining : finding **regularities** in data
- « Habits »
  - Regularity in the actions performed
  - **Temporal regularity between occurrences**
- Different problem for pattern miner
  - WHAT is repeated => **HOW** is it repeated

# Periodicity

- Pattern P is repeated (as usual) => has occurrences
- Some temporal property between occurrences
  - Sequencing
  - Timestamps
- Periodicity (naïve version) : constant inter-occurrence delay



# Periodicity in DMV

- Today: exhaustive approach based on *periodic concepts*
- Later, if time allows: pattern set approach based on MDL
- End of course: Sequence segmentation approach
  - Usually during case study, by Peggy

# How periodic is your set-top box?

## Analyzing the execution of a video decoder

Patricia López Cueva, Aurélie Bertaux, Alexandre Termier, Jean-François Méhaut, Miguel Santana: *Debugging embedded multimedia application traces through periodic pattern mining*. EMSOFT 2012: 13-22

Patricia López Cueva, *Debugging Embedded Multimedia Application Execution Traces through Periodic Pattern Mining*, PhD, 2013.

Slides adapted from Patricia Lopez Cueva

# Context

- Data : execution traces of set-top boxes
  - System level info : interrupts, context switches,...
  - Applicative info : start/end of (some) high level functions
  - Application : video decoding
  
- Problem :
  - Understand complex periodic behavior of video decoding software
  - Determine when the periodicity is broken

# Data

Execution trace =  
Sequence of  
timestamped events

Cut into windows

Transform into  
sequence of itemsets  
(window -> itemset)

## Execution Trace (s.μs)

0.1 ms {

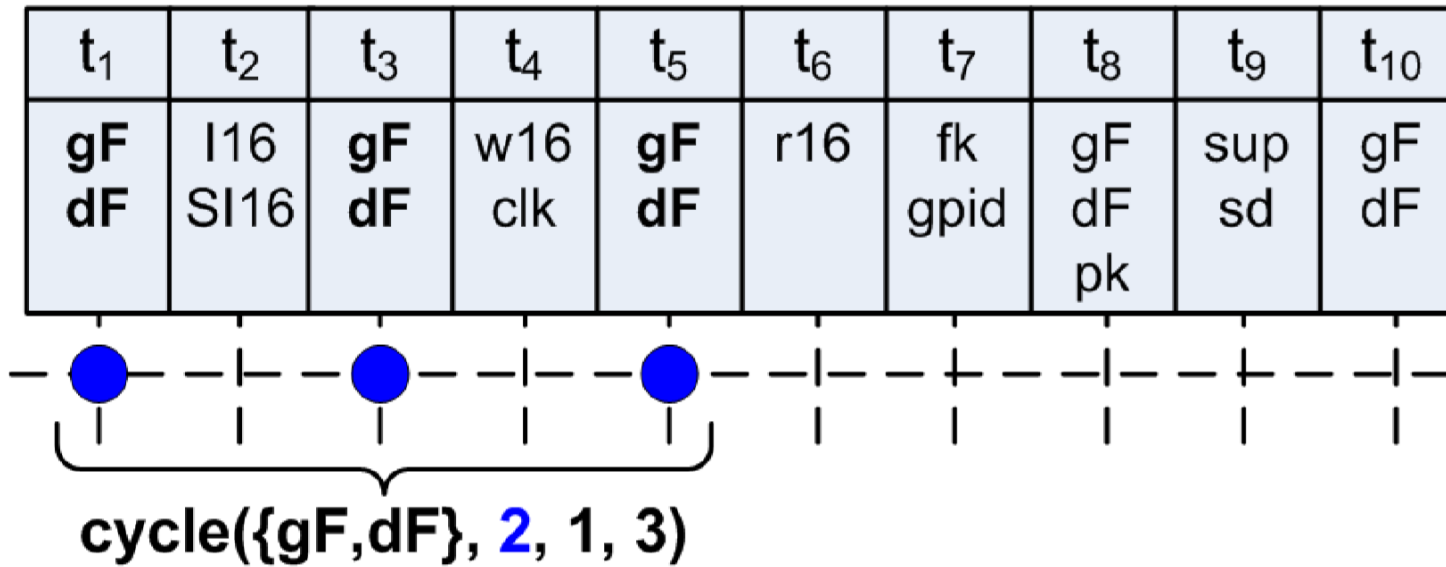
68.770630	getFrame
68.770697	displayFrame
68.770741	int16
68.770768	swint16
68.770869	displayFrame
68.770913	getFrame
68.770959	write16
68.770982	cpu_clock
68.771032	getFrame
68.771099	displayFrame
68.771150	read16
68.771235	fork
68.771324	get_pid
68.771346	getFrame
68.771372	displayFrame
68.771402	printk
68.771456	sem_up
68.771487	sem_down
68.771540	getFrame
68.771586	displayFrame

Preprocessing

## Transactional Database

t <sub>1</sub>	getFrame, displayFrame
t <sub>2</sub>	int16, swint16
t <sub>3</sub>	displayFrame, getFrame
t <sub>4</sub>	write16, cpu_clock
t <sub>5</sub>	getFrame, displayFrame
t <sub>6</sub>	read16
t <sub>7</sub>	fork, get_pid
t <sub>8</sub>	getFrame, displayFrame, printk
t <sub>9</sub>	sem_up, sem_down
t <sub>10</sub>	getFrame, displayFrame

# Pattern building block : the **cycle**



Repeated events

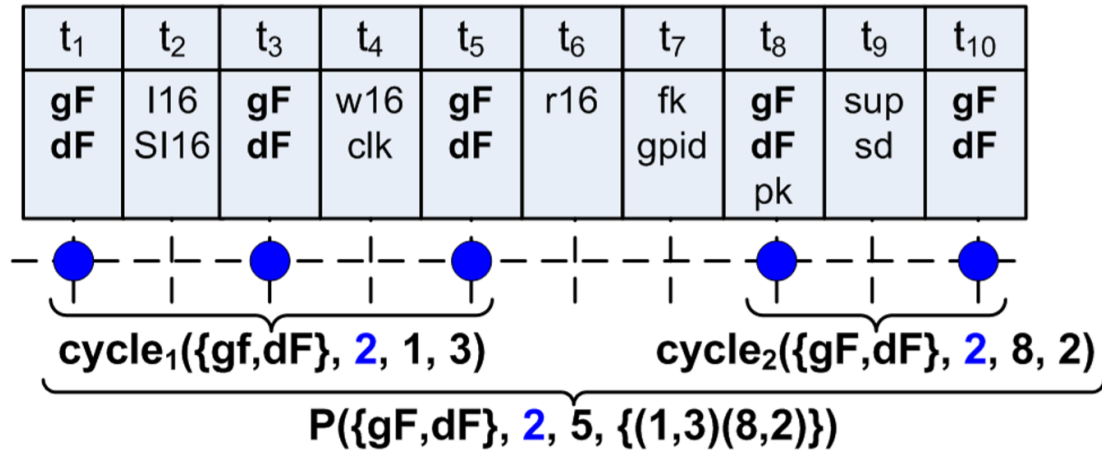
Period

Start offset

#repetition



# Periodic pattern



## Periodic Pattern

[Ma & Hellerstein, 2001]

A group of cycles forms a periodic pattern if:

- 1 Same period for all cycles.
- 2 All cycles are consecutive.
- 3 Cycles do not overlap.

## Support

Sum of all *cycles* lengths:

$\text{cycles} = \{(o_1, l_1), \dots, (o_k, l_k)\}$

$$\text{support} = \sum_{i=1}^k l_i$$

## Many redundancies

### Frequent Periodic Pattern

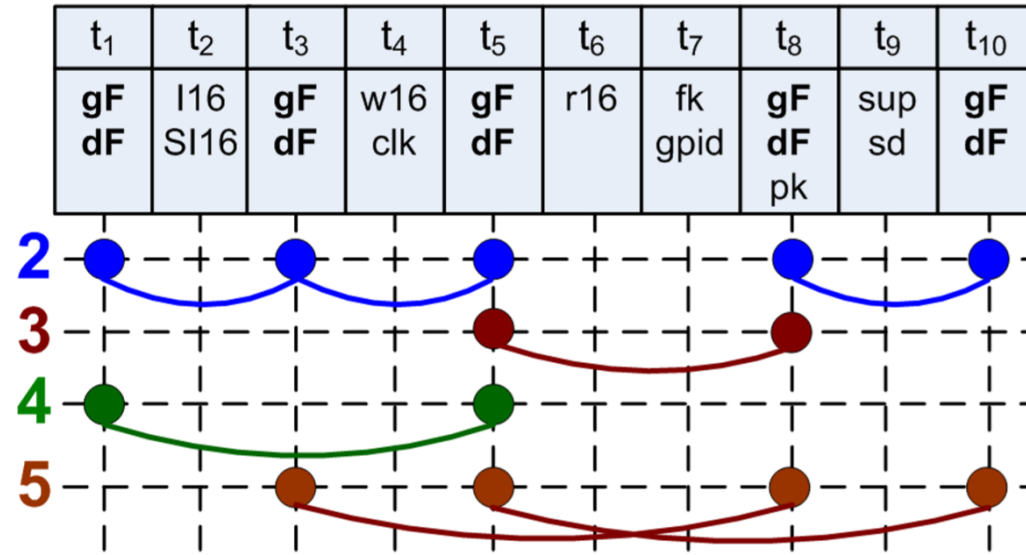
Given a minimum support threshold ( $\text{min\_sup}$ ), a pattern is frequent if

$$\text{support} \geq \text{min\_sup}$$

# Towards a condensed representation

- Too many redundant patterns -> condensed representation
  - Closed periodic patterns ?
- Pb : cannot compute classic closure with (Itemset, Period, Transactions)
- Solution : move from diadic to triadic !

# Triadic representation



Itemsets	Periods	2										3									
	Transactions	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
gF		X		X		X			X		X					X			X		
dF		X		X		X			X		X					X			X		
...																					
Itemsets	Periods	4										5									
	Transactions	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
gF		X				X								X		X			X		X
dF		X				X								X		X			X		X
...																					

Itemsets	Periods	2										3									
	Transactions	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
gF		X		X		X			X		X					X			X		
dF		X		X		X			X		X					X			X		
...																					
Itemsets	Periods	4										5									
	Transactions	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
gF		X				X								X		X			X		X
dF		X				X								X		X			X		X
...																					

Triples
$(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5\})$

		2										3									
Itemsets	Periods	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
	gF		X		X		X			X		X					X			X	
dF		X		X		X			X		X					X			X		
...																					
		4										5									
Itemsets	Periods	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
	gF	X				X								X		X			X		X
dF		X				X								X		X			X		X
...																					

**Periodic Concepts**  
 $T_1(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$

Itemsets	Periods	2										3									
	Transactions	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
gF		X		X		X			X		X					X			X		
dF		X		X		X			X		X					X			X		
...																					
Itemsets	Periods	4										5									
	Transactions	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
gF		X				X								X		X			X		X
dF		X				X								X		X			X		X
...																					

**Periodic Concepts**

$T_1(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$

$T_2(\{gF, dF\}, \{2, 4\}, \{t_1, t_5\})$

Itemsets	Periods	2										3									
	Transactions	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
gF		X	X	X		X		X	X					X			X				
dF		X	X	X		X		X	X					X			X				
...																					
Itemsets	Periods	4										5									
	Transactions	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
gF		X				X								X	X			X		X	
dF		X				X								X	X			X		X	
...																					

### Periodic Concepts

$$T_1(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$$

$$T_2(\{gF, dF\}, \{2, 4\}, \{t_1, t_5\})$$

$$T_3(\{gF, dF\}, \{2, 5\}, \{t_3, t_5, t_8, t_{10}\})$$

Itemsets	Periods	2										3									
	Transactions	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
gF		X		X		X			X		X					X			X		
dF		X		X		X			X		X					X			X		
...																					
Itemsets	Periods	4										5									
	Transactions	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
gF		X				X								X		X			X		X
dF		X				X								X		X			X		X
...																					

Periodic Concepts
$T_1(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$
$T_2(\{gF, dF\}, \{2, 4\}, \{t_1, t_5\})$
$T_3(\{gF, dF\}, \{2, 5\}, \{t_3, t_5, t_8, t_{10}\})$
$T_4(\{gF, dF\}, \{2, 3, 5\}, \{t_5, t_8\})$

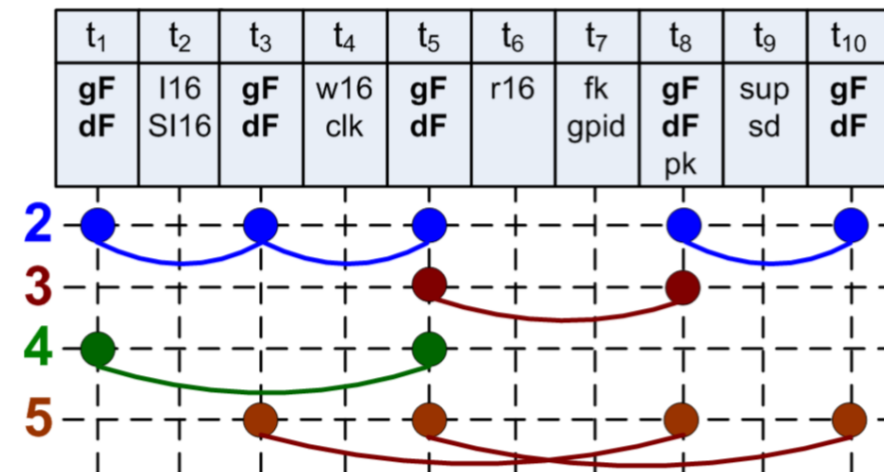


# Core Periodic Concept [EMSoft 2012]

## Core Periodic Concept

A periodic concept  $(I, P, T)$  is a **core periodic concept** if there does not exist any other periodic concept  $(I', P', T')$  such that  $I = I'$ ,  $P' \subset P$  and  $T' \supset T$ .

Periodic Concepts
$T_1(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$
$T_2(\{gF, dF\}, \{2, 4\}, \{t_1, t_5\})$
$T_3(\{gF, dF\}, \{2, 5\}, \{t_3, t_5, t_8, t_{10}\})$
$T_4(\{gF, dF\}, \{2, 3, 5\}, \{t_5, t_8\})$

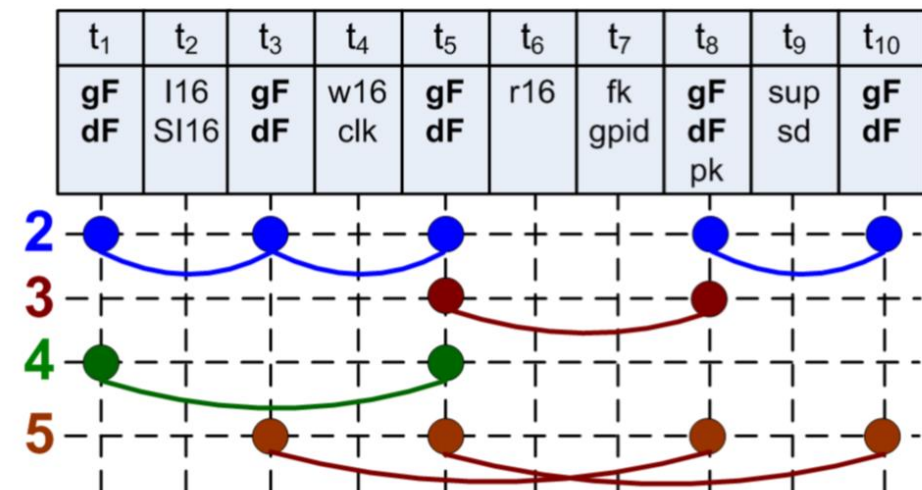


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Core Periodic Concepts		
$T_1$	$(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$	
$T_2$	$(\{gF, dF\}, \{2, 4\}, \{t_1, t_5\})$	
$T_3$	$(\{gF, dF\}, \{2, 5\}, \{t_3, t_5, t_8, t_{10}\})$	
$T_4$	$(\{gF, dF\}, \{2, 3, 5\}, \{t_5, t_8\})$	

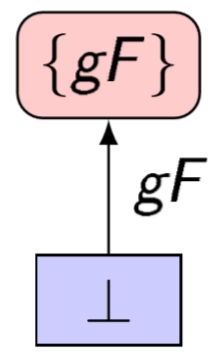
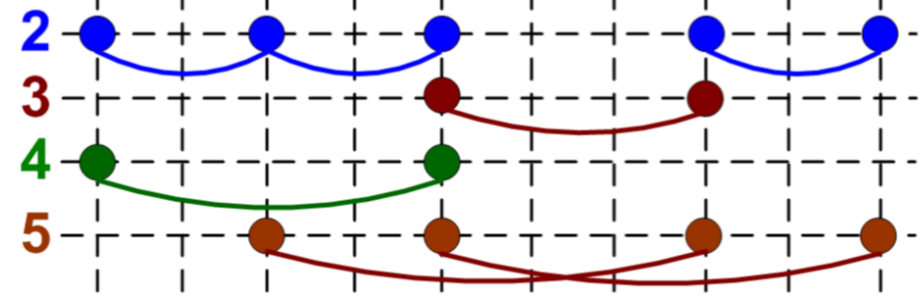


CPC = condensed representation of all periodic concepts

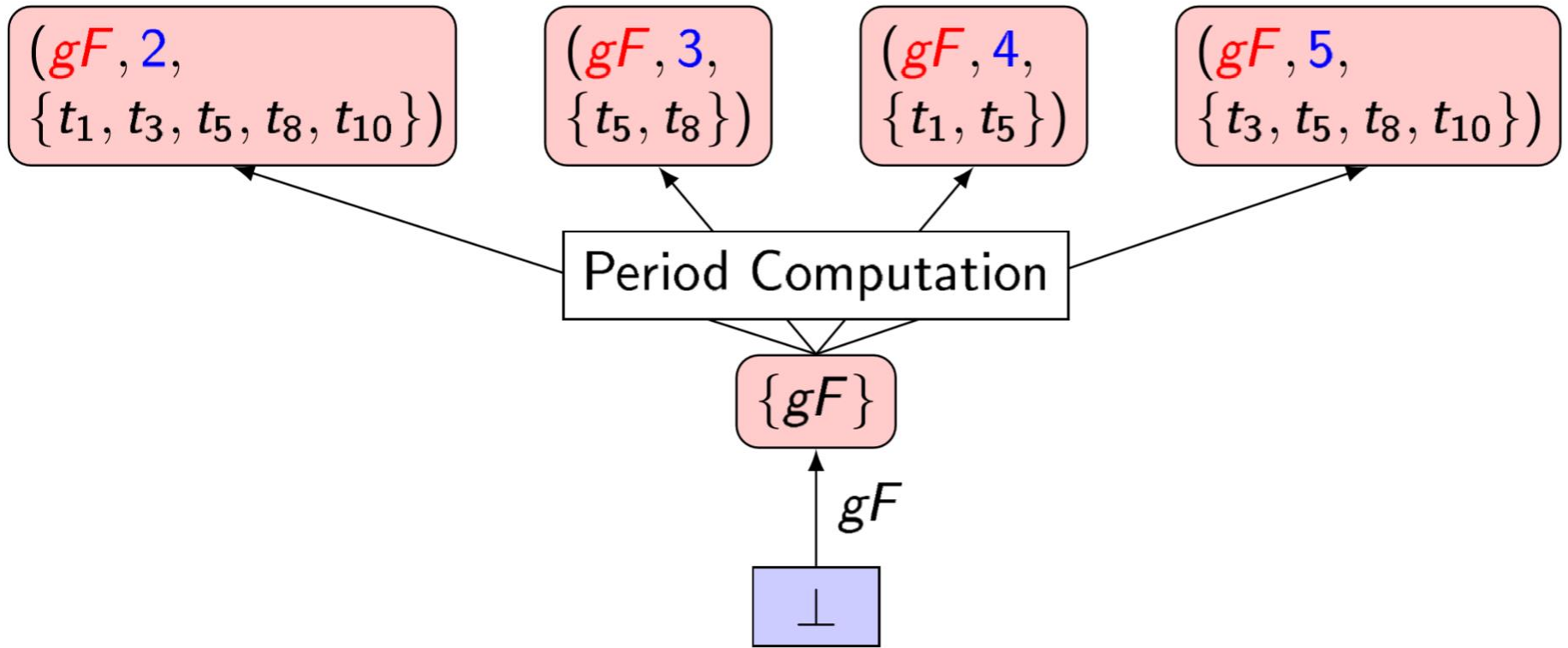
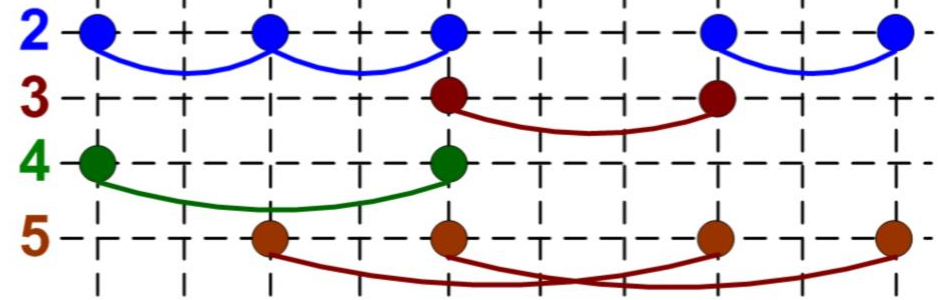
# Mining Core Periodic Concepts

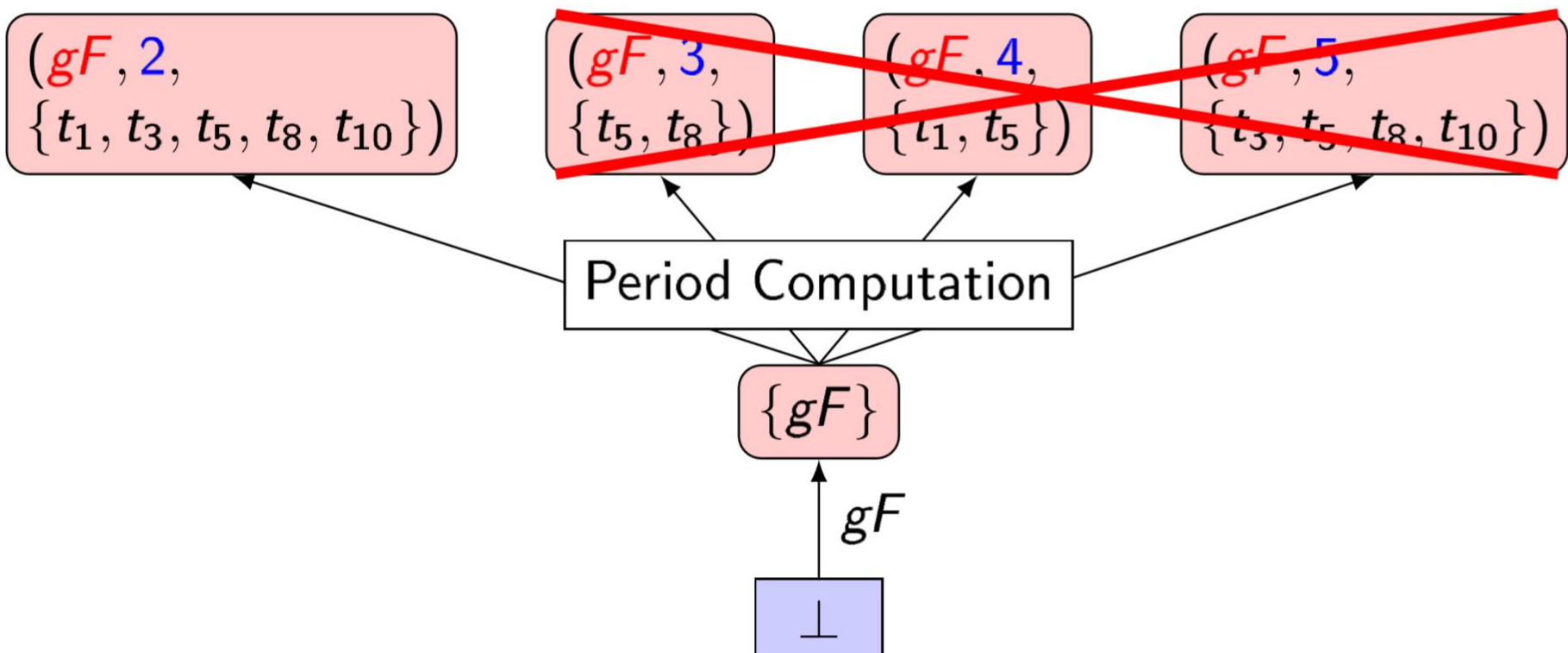
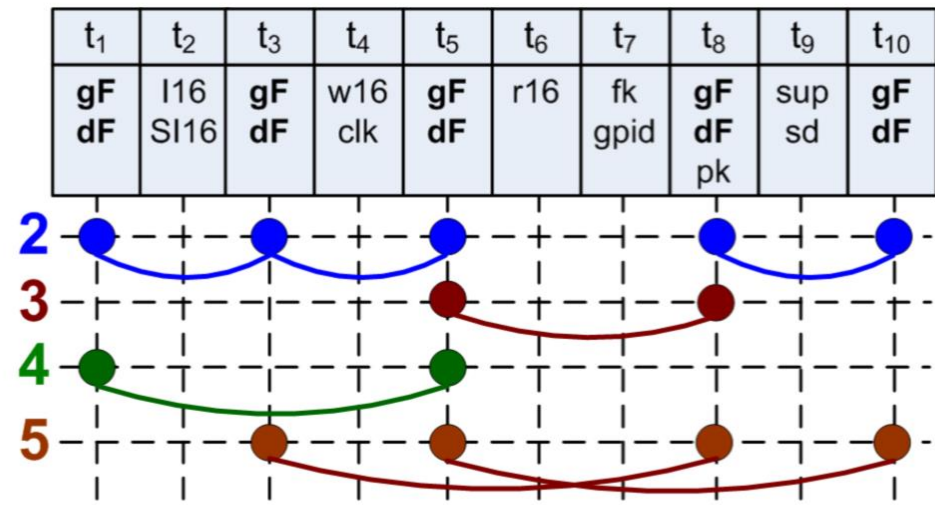
- Solution 1: [EMSoft 2012]
  - Use DataPeeler (Cerf et al., 2009) to get triadic patterns
  - Postprocess to filter CPC
- Solution 2: [López Cueva PhD, 2013]
  - Direct mining of CPC
  - Based on LCM/CbO enumeration strategy
  - Proven poly-delay time, poly space

t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>	t <sub>9</sub>	t <sub>10</sub>
<b>gF</b> <b>dF</b>	l16 Sl16	<b>gF</b> <b>dF</b>	w16 clk	<b>gF</b> <b>dF</b>	r16	fk gpid	<b>gF</b> <b>dF</b> pk	sup sd	<b>gF</b> <b>dF</b>

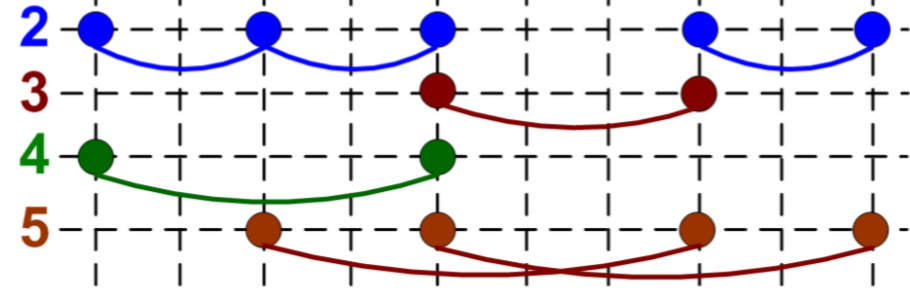


$t_1$	$t_2$	$t_3$	$t_4$	$t_5$	$t_6$	$t_7$	$t_8$	$t_9$	$t_{10}$
gF dF	l16 SI16	gF dF	w16 clk	gF dF	r16	fk gpid	gF dF pk	sup sd	gF dF





$t_1$	$t_2$	$t_3$	$t_4$	$t_5$	$t_6$	$t_7$	$t_8$	$t_9$	$t_{10}$
gF	l16	gF	w16	gF	r16	fk	gF	sup	gF
dF	Sl16	dF	clk	dF		gpid	dF	sd	dF
							pk		



$(\{gF, dF\}, 2, \{t_1, t_3, t_5, t_8, t_{10}\})$

$\cap t_1, t_3, t_5, t_8, t_{10}$

$(gF, 2, \{t_1, t_3, t_5, t_8, t_{10}\})$

~~$(gF, 3, \{t_5, t_8\})$~~

~~$(gF, 4, \{t_1, t_5\})$~~

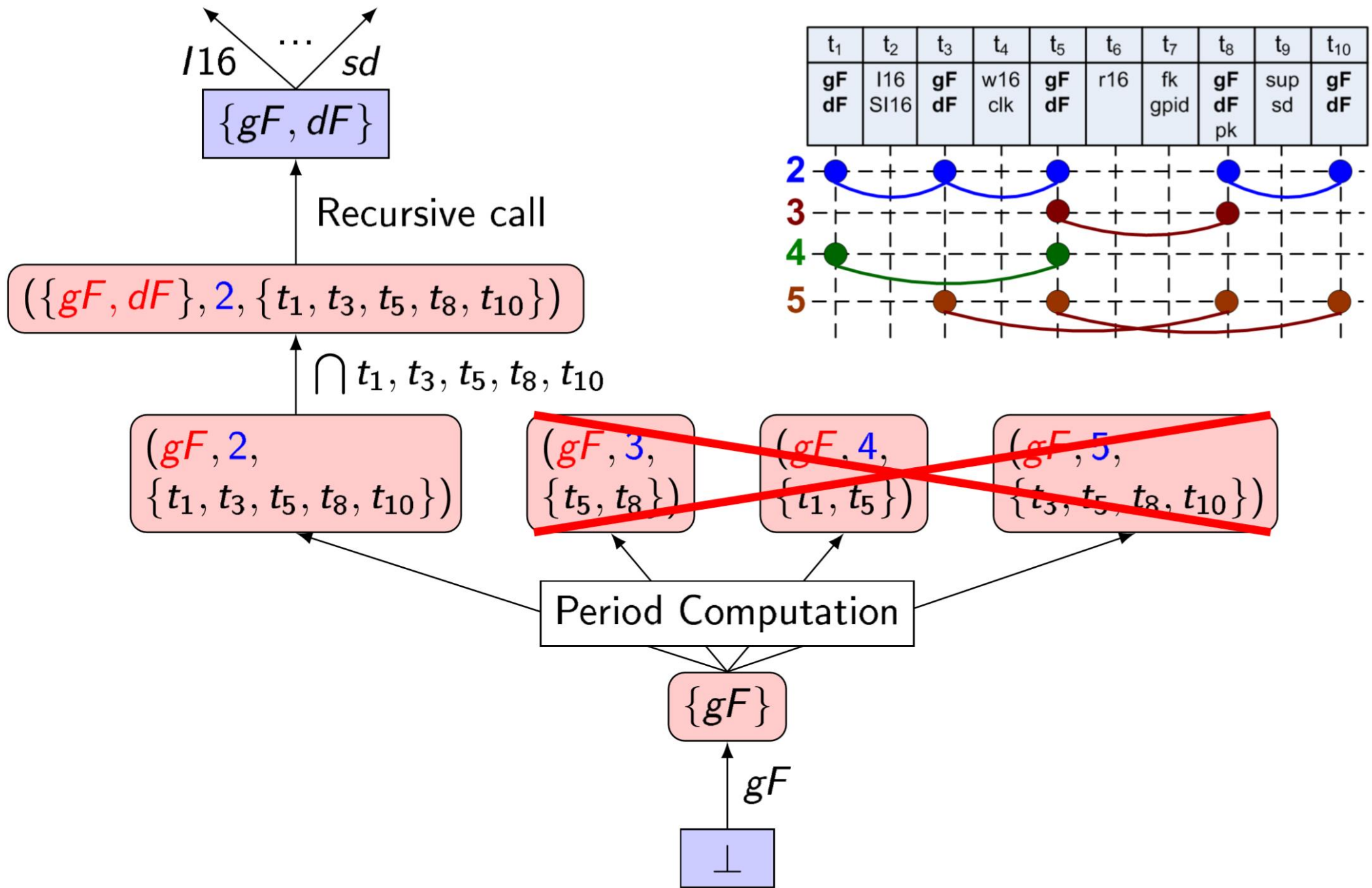
~~$(gF, 5, \{t_3, t_5, t_8, t_{10}\})$~~

Period Computation

$\{gF\}$

$gF$

$\perp$



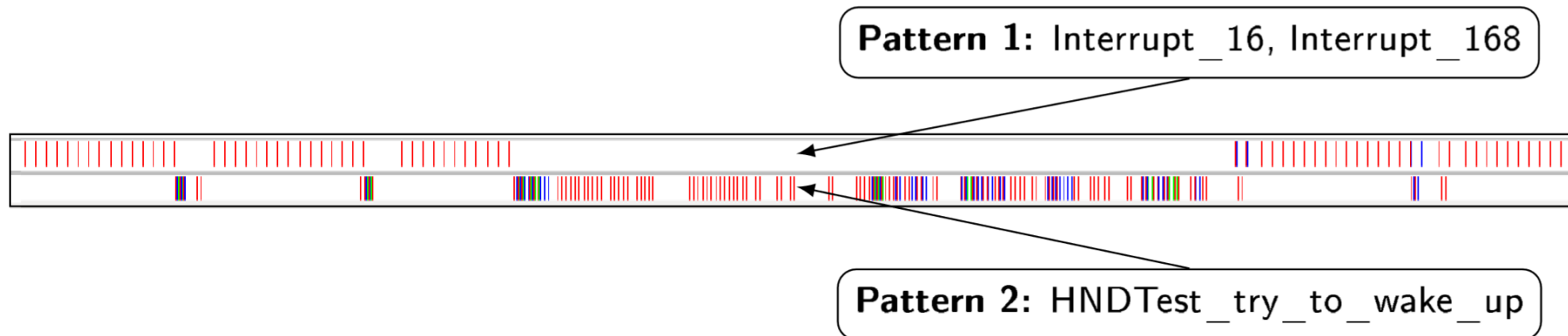


Trace of STi7200 stb  
500k events  
-> 13k transactions, ~8  
items/transac  
Mining 10% -> 195s  
758 CPC (20k per pats)

# Application on real execution trace

## Discovered conflict between the application and the system (USB port)

- Interrupt\_16: processor clock interrupt.
- Interrupt\_168: USB interrupt.
- HNDTest\_try\_to\_wake\_up: system call (try\_to\_wake\_up).



# Conclusion

- Three approaches for mining temporal regularities presented
  - Quite strict cycles, gaps allowed between cycles, transaction data, condensed representation
  - Tolerant + nested cycles, sequence data, MDL
  - Segmentation, transaction data, optimisation/Pareto/MDL
- Many other interesting problems await
- Surprisingly few people in that research area (since 1999)

# Perspectives

- Robustness, robustness, robustness
  - Most periodic pattern definitions break too easily
  - -> prevent the discovery of more general/covering patterns
- Take into account domain knowledge
- Provide easy to use implementations

Thank you for your attention!