

Periodic pattern mining

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Data Mining and Visualization course – M2 SIF

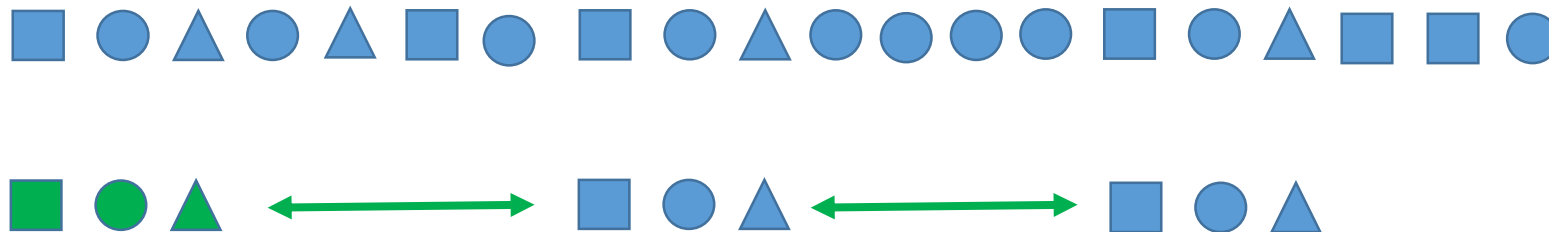
These slides adapted from an invited talk at [SFC 2019](#)

Motivation

- Pattern mining : finding **regularities** in data
- « Habits »
 - Regularity in the actions performed
 - **Temporal regularity between occurrences**
- Different problem for pattern miner
 - WHAT is repeated => **HOW** is it repeated

Periodicity

- Pattern P is repeated (as usual) => has occurrences
- Some temporal property between occurrences
 - Sequencing
 - Timestamps
- Periodicity (naïve version) : constant inter-occurrence delay



This talk

Several approaches on periodic/near periodic pattern mining

- Condensed representation for mining periodic pattern with gaps
- Nested periodic pattern mining with MDL
- « Signature » patterns

How periodic is your set-top box? Analyzing the execution of a video decoder

Patricia López Cueva, Aurélie Bertaux, Alexandre Termier, Jean-François Méhaut, Miguel Santana: *Debugging embedded multimedia application traces through periodic pattern mining*. EMSOFT 2012: 13-22

Patricia López Cueva, *Debugging Embedded Multimedia Application Execution Traces through Periodic Pattern Mining*, PhD, 2013.

Slides adapted from Patricia Lopez Cueva

Context

- Data : execution traces of set-top boxes
 - System level info : interrupts, context switches,...
 - Applicative info : start/end of (some) high level functions
 - Application : video decoding

- Problem :
 - Understand complex periodic behavior of video decoding software
 - Determine when the periodicity is broken

Data

Execution trace =
Sequence of
timestamped events

Cut into windows

Transform into
sequence of itemsets
(window -> itemset)

Execution Trace (s.μs)

0.1 ms {

68.770630	getFrame
68.770697	displayFrame
68.770741	int16
68.770768	swint16
68.770869	displayFrame
68.770913	getFrame
68.770959	write16
68.770982	cpu_clock
68.771032	getFrame
68.771099	displayFrame
68.771150	read16
68.771235	fork
68.771324	get_pid
68.771346	getFrame
68.771372	displayFrame
68.771402	printk
68.771456	sem_up
68.771487	sem_down
68.771540	getFrame
68.771586	displayFrame

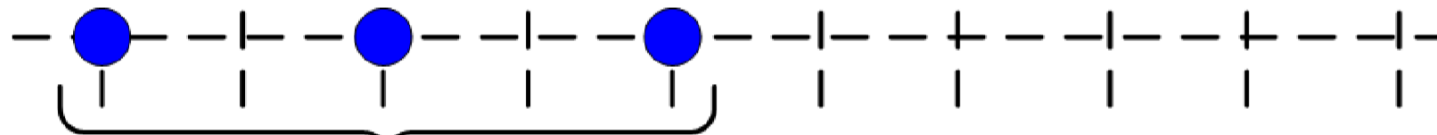
Preprocessing

Transactional Database

t ₁	getFrame, displayFrame
t ₂	int16, swint16
t ₃	displayFrame, getFrame
t ₄	write16, cpu_clock
t ₅	getFrame, displayFrame
t ₆	read16
t ₇	fork, get_pid
t ₈	getFrame, displayFrame, printk
t ₉	sem_up, sem_down
t ₁₀	getFrame, displayFrame

Pattern building block : the **cycle**

t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF	l16	gF	w16	gF	r16	fk	gF	sup	gF
dF	SI16	dF	clk	dF		gp id	dF	sd	dF
							pk		



cycle({gF,dF}, 2, 1, 3)

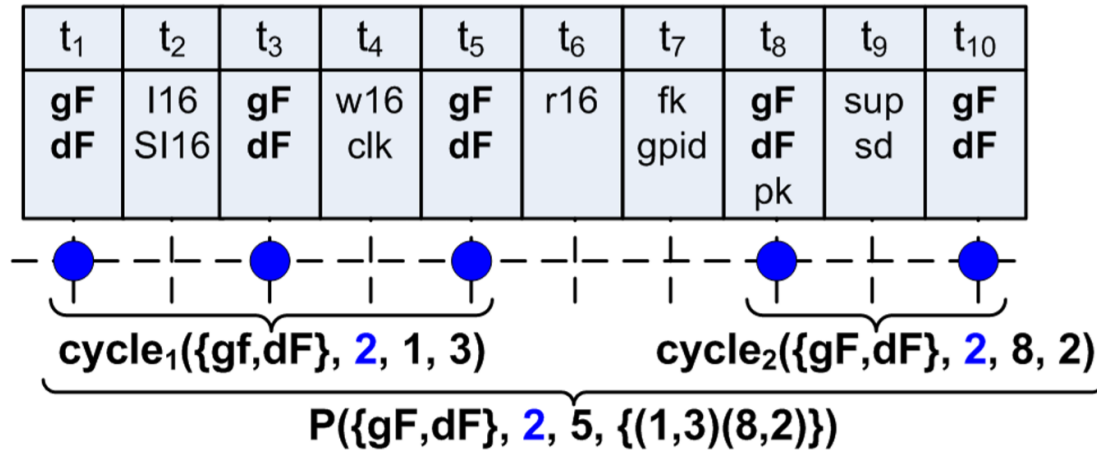
Repeated events

Period

Start offset

#repetition

Periodic pattern



Periodic Pattern

[Ma & Hellerstein, 2001]

A group of cycles forms a periodic pattern if:

- 1 Same period for all cycles.
- 2 All cycles are consecutive.
- 3 Cycles do not overlap.

Support

Sum of all *cycles* lengths:

$\text{cycles} = \{(o_1, l_1), \dots, (o_k, l_k)\}$

$$\text{support} = \sum_{i=1}^k l_i$$

Many redundancies

Frequent Periodic Pattern

Given a minimum support threshold (min_sup), a pattern is frequent if

$$\text{support} \geq \text{min_sup}$$

Redundancies in periodic patterns defined

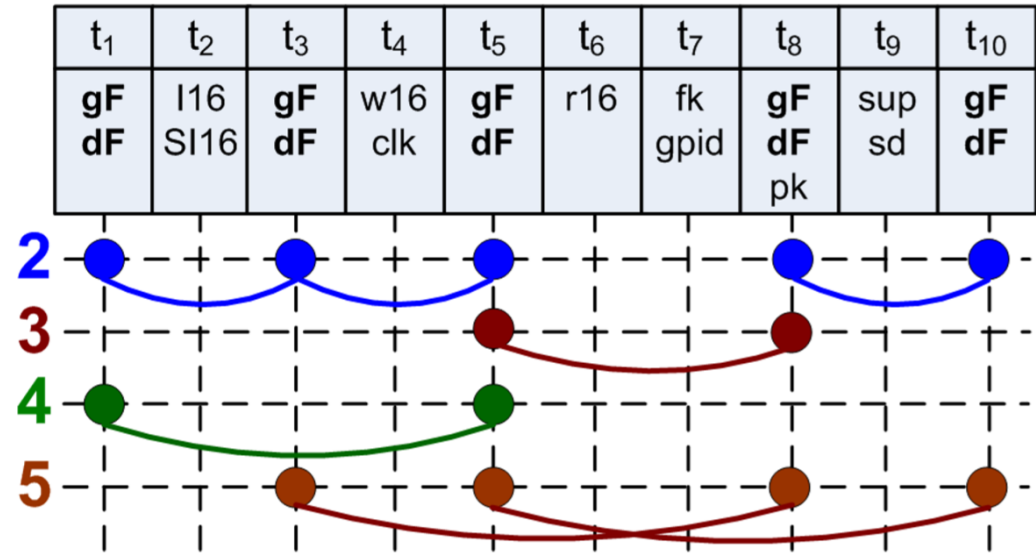
1. All subsets of the itemset part
2. Combinations / multiples of the period

Frequent Periodic Patterns	
1	$P_1(\{gF\}, 2, 5, \{(1, 3)(8, 2)\})$
	$P_2(\{dF\}, 2, 5, \{(1, 3)(8, 2)\})$
	$P_3(\{gF, dF\}, 2, 5, \{(1, 3)(8, 2)\})$
	...
2	$P_6(\{gF, dF\}, 3, 2, \{(5, 2)\})$
	...
	$P_9(\{gF, dF\}, 4, 2, \{(1, 2)\})$
	...
	$P_{12}(\{gF, dF\}, 5, 2, \{(3, 2)\})$
	...
	$P_{15}(\{gF, dF\}, 5, 2, \{(5, 2)\})$

Towards a condensed representation

- Too many redundant patterns -> condensed representation
 - Closed periodic patterns ?
- Pb : cannot compute classic closure with (Itemset, Period, Transactions)
- Solution : move from diadic to triadic !
 - Based on a *ternary relation*

Triadic representation



Itemsets	Periods	2										3									
	Transactions	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF		X		X		X			X		X					X			X		
dF		X		X		X			X		X					X			X		
...																					
Itemsets	Periods	4										5									
	Transactions	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF		X				X								X		X			X		X
dF		X				X								X		X			X		X
...																					

Itemsets	Periods	2										3									
	Transactions	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF		X		X		X			X		X					X			X		
dF		X		X		X			X		X					X			X		
...																					
Itemsets	Periods	4										5									
	Transactions	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF		X				X								X		X			X		X
dF		X				X								X		X			X		X
...																					

Triples
$(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5\})$

		2										3									
Itemsets	Periods	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
	gF		X		X		X			X		X					X			X	
dF		X		X		X			X		X					X			X		
...																					
		4										5									
Itemsets	Periods	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
	gF	X				X								X		X			X		X
dF	X				X									X		X			X		X
...																					

Periodic Concepts

$$T_1(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$$

Itemsets	Periods	2										3									
	Transactions	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF		X		X		X			X		X					X			X		
dF		X		X		X			X		X					X			X		
...																					
Itemsets	Periods	4										5									
	Transactions	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF		X				X								X		X			X		X
dF		X				X								X		X			X		X
...																					

Periodic Concepts
$T_1(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$
$T_2(\{gF, dF\}, \{2, 4\}, \{t_1, t_5\})$

Itemsets	Periods	2										3									
	Transactions	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF		X	X	X		X		X	X					X			X				
dF		X	X	X		X		X	X					X			X				
...																					
Itemsets	Periods	4										5									
	Transactions	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF		X				X								X	X			X		X	
dF		X				X								X	X			X		X	
...																					

Periodic Concepts

$$T_1(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$$

$$T_2(\{gF, dF\}, \{2, 4\}, \{t_1, t_5\})$$

$$T_3(\{gF, dF\}, \{2, 5\}, \{t_3, t_5, t_8, t_{10}\})$$

Itemsets	Periods	2										3									
	Transactions	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF		X		X		X			X		X					X			X		
dF		X		X		X			X		X					X			X		
...																					
Itemsets	Periods	4										5									
	Transactions	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF		X				X								X		X			X		X
dF		X				X								X		X			X		X
...																					

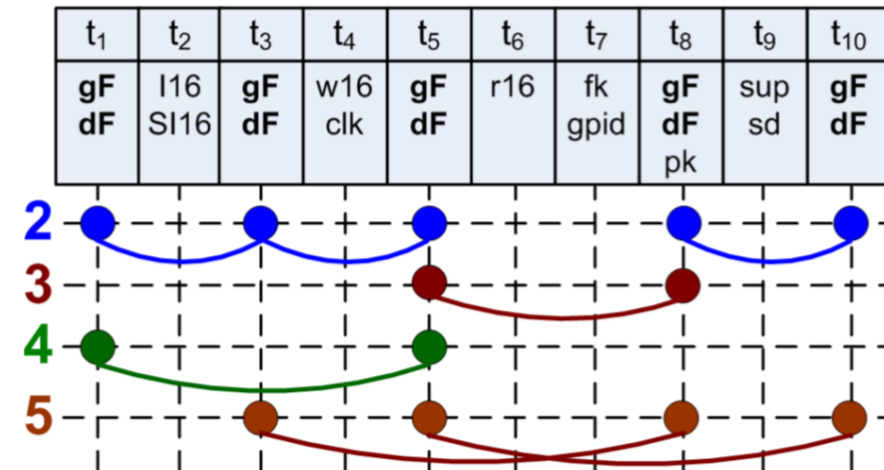
Periodic Concepts
$T_1(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$
$T_2(\{gF, dF\}, \{2, 4\}, \{t_1, t_5\})$
$T_3(\{gF, dF\}, \{2, 5\}, \{t_3, t_5, t_8, t_{10}\})$
$T_4(\{gF, dF\}, \{2, 3, 5\}, \{t_5, t_8\})$

Core Periodic Concept [EMSoft 2012]

Core Periodic Concept

A periodic concept (I, P, T) is a **core periodic concept** if there does not exist any other periodic concept (I', P', T') such that $I = I'$, $P' \subset P$ and $T' \supset T$.

Periodic Concepts	
T_1	$(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$
T_2	$(\{gF, dF\}, \{2, 4\}, \{t_1, t_5\})$
T_3	$(\{gF, dF\}, \{2, 5\}, \{t_3, t_5, t_8, t_{10}\})$
T_4	$(\{gF, dF\}, \{2, 3, 5\}, \{t_5, t_8\})$

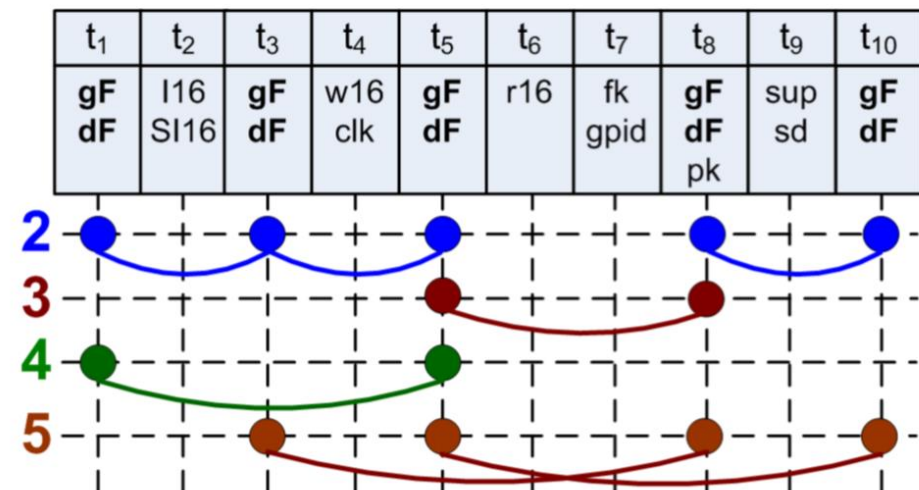


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A periodic concept (I, P, T) is a **core periodic concept** if there does not exist any other periodic concept (I', P', T') such that $I = I'$, $P' \subset P$ and $T' \supset T$.

Core Periodic Concepts		
T_1	$(\{gF, dF\}, \{2\}, \{t_1, t_3, t_5, t_8, t_{10}\})$	
T_2	$(\{gF, dF\}, \{2, 4\}, \{t_1, t_5\})$	
T_3	$(\{gF, dF\}, \{2, 5\}, \{t_3, t_5, t_8, t_{10}\})$	
T_4	$(\{gF, dF\}, \{2, 3, 5\}, \{t_5, t_8\})$	

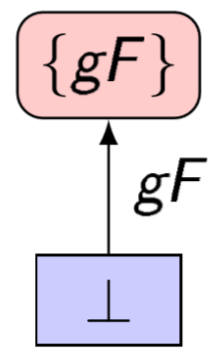
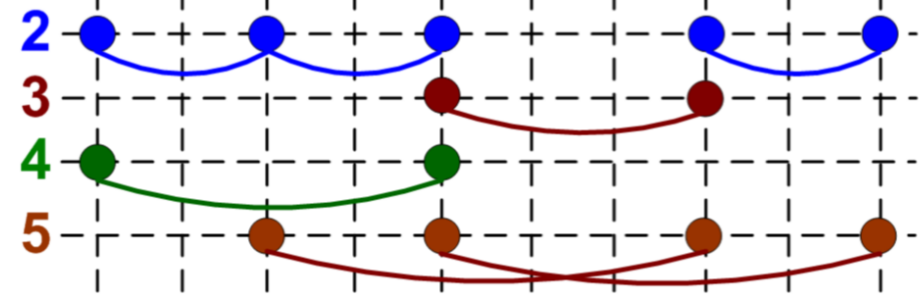


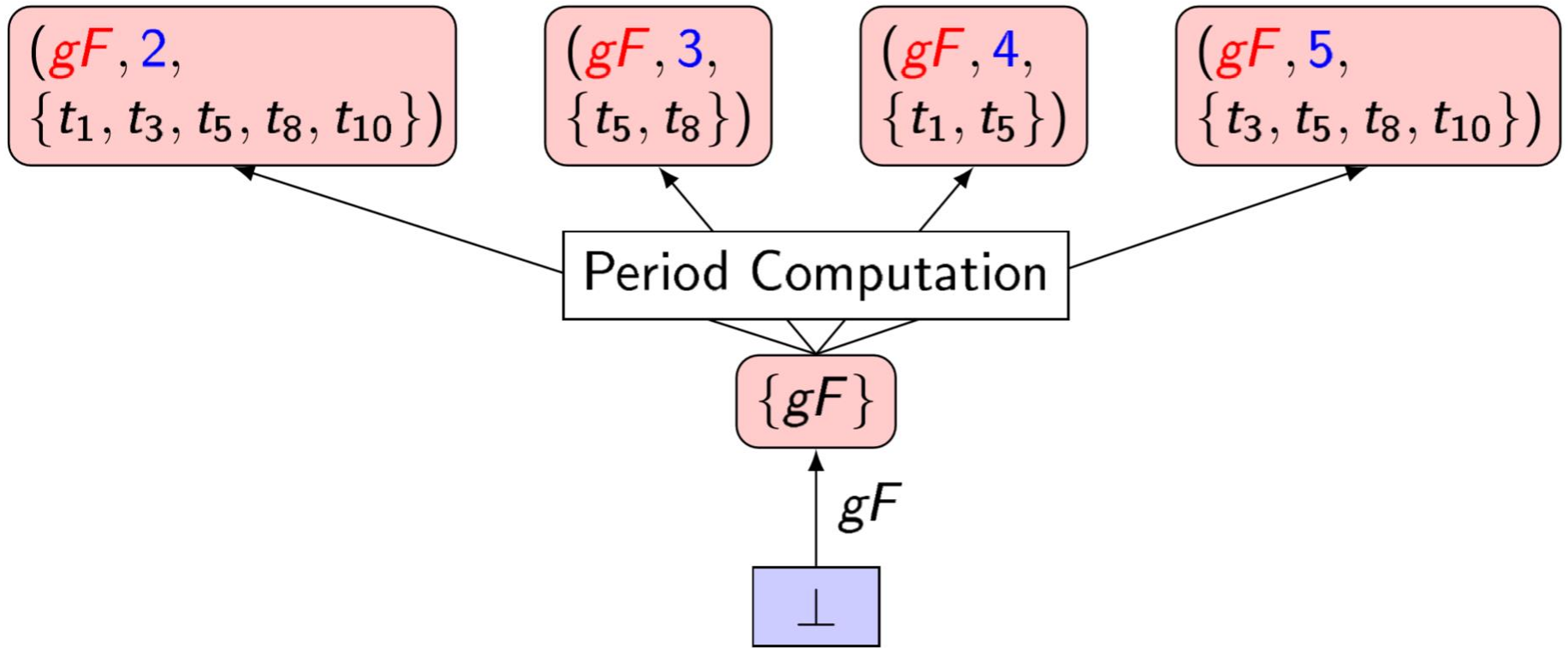
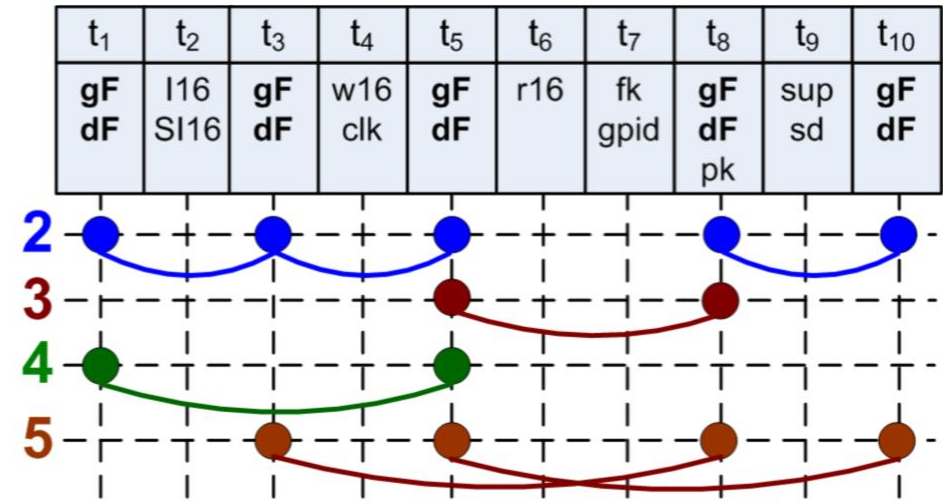
CPC = condensed representation of all periodic concepts

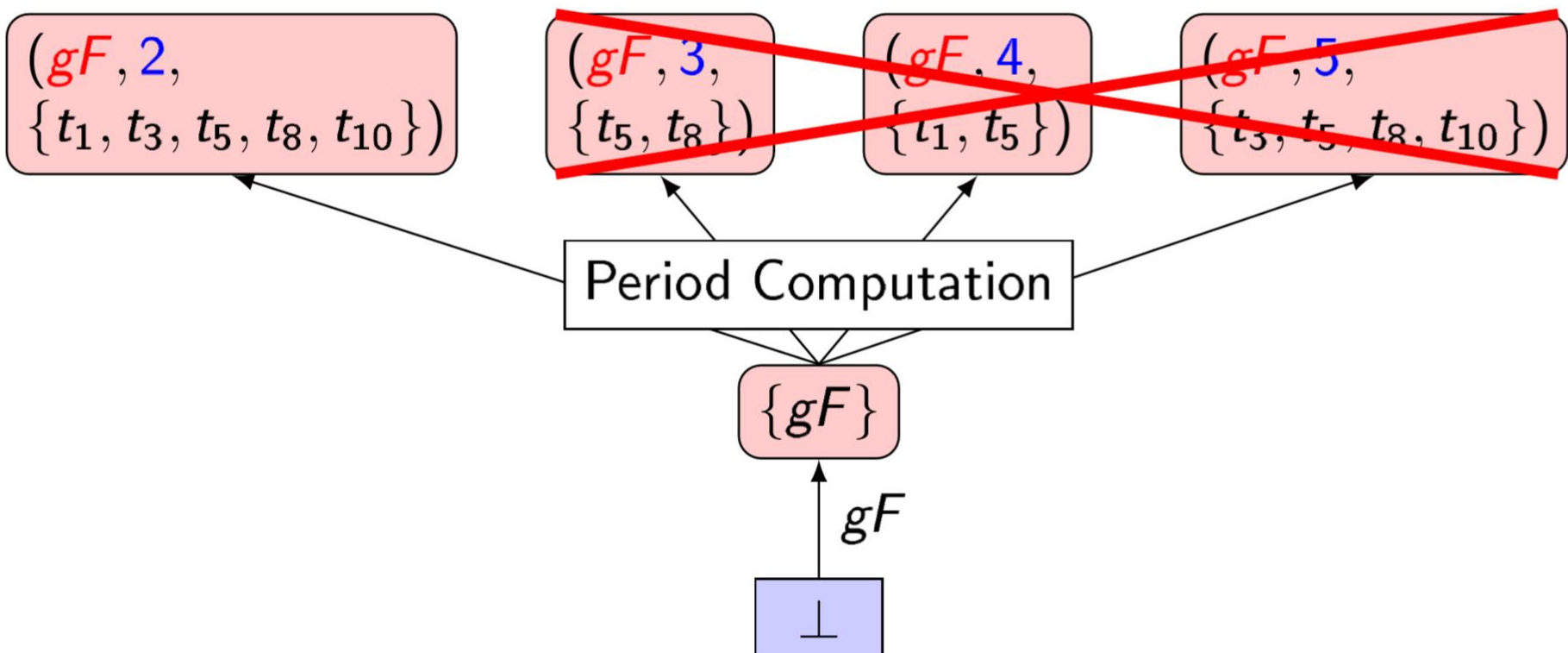
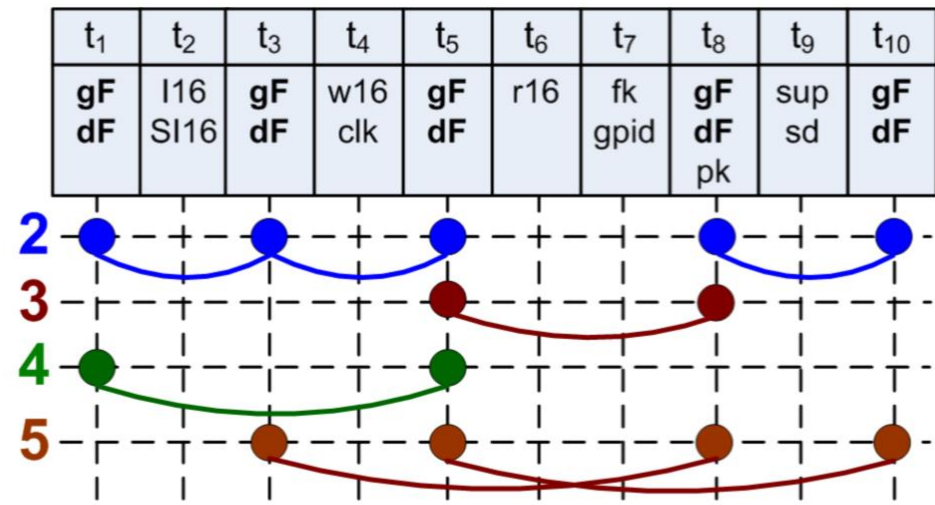
Mining Core Periodic Concepts

- Solution 1: [EMSoft 2012]
 - Use DataPeeler (Cerf et al., 2009) to get triadic patterns
 - Postprocess to filter CPC
- Solution 2: [López Cueva PhD, 2013]
 - Direct mining of CPC
 - Based on LCM/CbO enumeration strategy
 - Proven poly-delay time, poly space

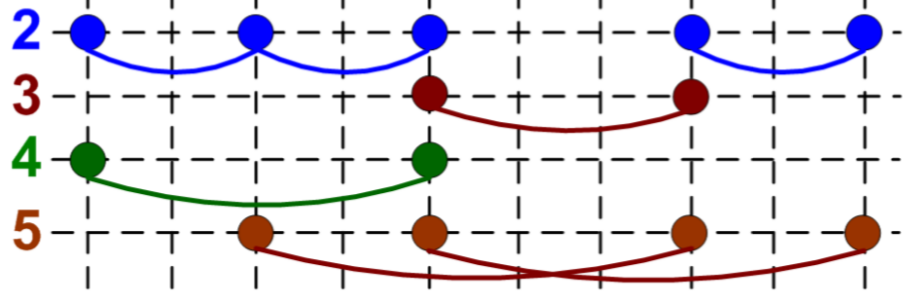
t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
gF	l16	gF	w16	gF	r16	fk	gF	sup	gF
dF	Sl16	dF	clk	dF		gpId	dF	sd	dF
							pk		







t_1	t_2	t_3	t_4	t_5	t_6	t_7	t_8	t_9	t_{10}
gF dF	l16 SI16	gF dF	w16 clk	gF dF	r16	fk gpid	gF dF pk	sup sd	gF dF



$(\{gF, dF\}, 2, \{t_1, t_3, t_5, t_8, t_{10}\})$

$\cap t_1, t_3, t_5, t_8, t_{10}$

$(gF, 2, \{t_1, t_3, t_5, t_8, t_{10}\})$

~~$(gF, 3, \{t_5, t_8\})$~~

~~$(gF, 4, \{t_1, t_5\})$~~

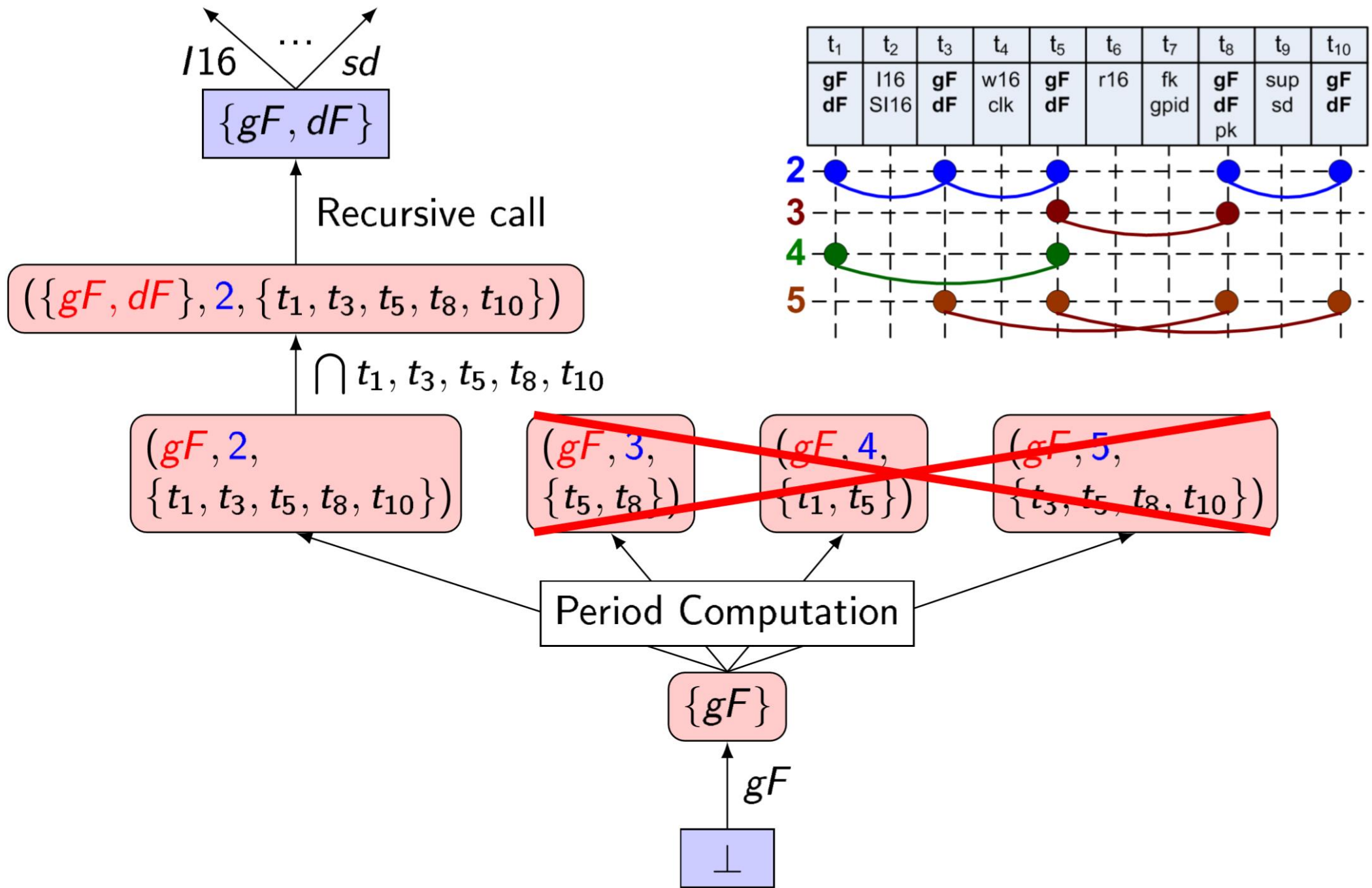
~~$(gF, 5, \{t_3, t_5, t_8, t_{10}\})$~~

Period Computation

$\{gF\}$

gF

\perp

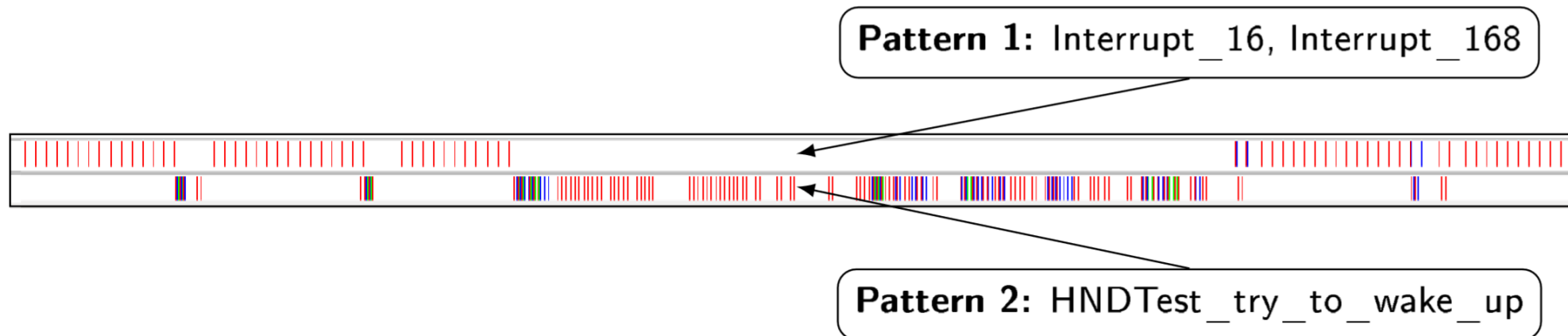


Trace of STi7200 stb
500k events
-> 13k transactions, ~8
items/transac
Mining 10% -> 195s
758 CPC (20k per pats)

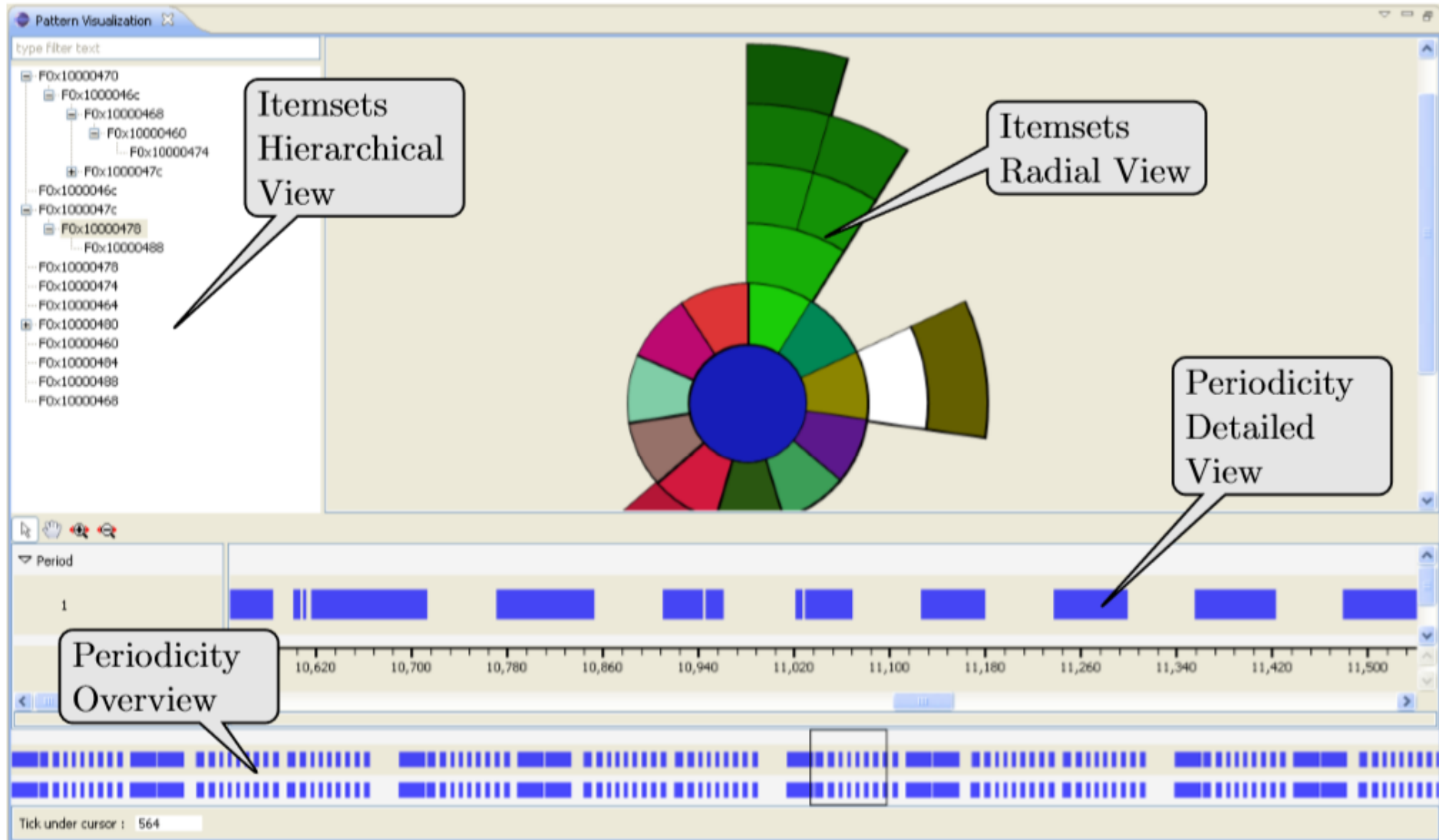
Application on real execution trace

Discovered conflict between the application and the system (USB port)

- Interrupt_16: processor clock interrupt.
- Interrupt_168: USB interrupt.
- HNDTest_try_to_wake_up: system call (try_to_wake_up).



A visualization of CPC



How periodic are we?

Analyzing the life of Sacha

Esther Galbrun, Peggy Cellier, Nikolaj Tatti, Alexandre Termier, Bruno Crémilleux:
Mining Periodic Patterns with a MDL Criterion. ECML/PKDD (2) 2018: 535-551

Slides adapted from Peggy Cellier

Motivations

- Previous work: we wanted few patterns
- With CPC, we still have 1k patterns...

- H. Arimura, at the defense of Patricia Lopez Cueva:
 - « *Periodic patterns should compress well the data* »

- => Periodic patterns + MDL *à la Krimp?*
 - Should give fewer patterns
 - With good representativity of the data

Motivation, #2: data of Sacha Chua

[Download as spreadsheet](#)

Start	End	Category	Duration	Data
02 Sep 18:44		Discretionary » Play » Other		
02 Sep 18:44	18:44	Sleep	0:00	
02 Sep 12:45	18:44	A- » Childcare	5:59	
02 Sep 12:12	12:45	Personal » Routines	0:32	
02 Sep 12:12	12:12	A- » Childcare	0:00	
02 Sep 12:11	12:12	Personal » Routines	0:00	
02 Sep 11:45	12:11	A- » Childcare	0:26	
02 Sep 10:12	11:45	A- » Childcare	1:33	
02 Sep 09:12	10:12	A- » Childcare	0:59	
02 Sep 08:04	09:12	Personal » Routines	1:07	
01 Sep 23:02	02 Sep 08:03	Sleep	9:00	

Simple periodic pattern in activity trace

$S = \langle$ (16-04-2018 7:30 , wake up), ← #1
(16-04-2018 7:40 , prepare coffee),
...
(16-04-2018 8:10 , take metro),
...
(16-04-2018 11:00 , attend meeting),
...
(16-04-2018 11:00 , eat dinner),
...
(17-04-2018 7:32 , wake up), ← #2
(17-04-2018 7:38 , prepare coffee),
...
(20-04-2018 7:28 , wake up), ← #5
(20-04-2018 7:41 , prepare coffee),
...
(15-06-2018 7:28 , wake up),
...
 \rangle

16-04-2018 7:30, wake up
repeat every 24 hours for 5 days

Cycle, again

*On April 16, at 7:30 AM, wake up,
repeat every 24 hours for 5 days*

A cycle is specified by:

event α : the repeating event,

length r : the number of repetitions of the event,

period p : the inter-occurrence distance,

starting point τ : the timestamp of the first occurrence, and

shift corrections E : a list of time offsets.

Hence, a cycle is a 5-tuple $C = (\alpha, r, p, \tau, E)$.

Noise tolerance

Tolerate variation in inter-occurrence distances,
shift corrections $E = \langle \mathbf{e}_1, \dots, \mathbf{e}_{r-1} \rangle$.

Reconstruct occurrences timestamps of repetitions recursively:

$$t_1 = \tau,$$

$$t_2 = t_1 + \rho + \mathbf{e}_1,$$

...

$$t_r = t_{r-1} + \rho + \mathbf{e}_{r-1}.$$

Problem statement v1

- Input
 - An event sequence
- Output
 - A representative collection of cycles

Introducing *cycle cover*

Denote as $cover(C)$ the corresponding set of reconstructed timestamp–event pairs:

$$cover(C) = \{(t_1, \alpha), (t_2, \alpha), \dots, (t_r, \alpha)\} ,$$

and for a collection \mathcal{C} of cycles

$$cover(\mathcal{C}) = \bigcup_{C \in \mathcal{C}} cover(C) .$$

For a sequence S and cycle collection \mathcal{C} we call **residual** the timestamp–event pairs of S not covered by any cycle in \mathcal{C} :

$$residual(\mathcal{C}, S) = S \setminus cover(\mathcal{C}) .$$

Problem statement v2

We associate

- a cost $L(o)$ to each individual occurrence
- a cost $L(C)$ to each cycle

Then, we can reformulate our problem as follows:

Problem

*Given an event sequence S , find the collection of cycles \mathcal{C} minimising the **cost***

$$L(\mathcal{C}, S) = \sum_{C \in \mathcal{C}} L(C) + \sum_{o \in \text{residual}(\mathcal{C}, S)} L(o) .$$

What cost?

- Many possible choices for *cost*
- Our cost: based on the **MDL principle** (Grünwald, 2007)
 - Comes from Information Theory
 - Based on compression
 - « *more representative structures allow better compression of data* »
 - Good results in **model selection...**
 - ...especially for pattern mining!
 - cf works of Vreeken, van Leeuwen, Siebes, Tatti...

Alignment of MDL and our problem

- Classic MDL formula

$$L(\text{Data}, \text{Model}) = L(\text{Model}) + L(\text{Model} \mid \text{Data})$$

where $L(\dots)$ = description length in bits - called **encoding**

- Our problem

$$L(\mathcal{C}, \mathcal{S}) = \sum_{C \in \mathcal{C}} L(C) + \sum_{o \in \text{residual}(\mathcal{C}, \mathcal{S})} L(o)$$

- Paper explains our encoding $L(\dots)$ in detail

More complex patterns

$S = \langle$ (16-04-2018 7:30 , wake up), ← #1 - 1st week
(16-04-2018 7:40 , prepare coffee),
...
(16-04-2018 8:10 , take metro), 16-04-2018 7:30, wake up
... 10 min later, prepare coffee
(16-04-2018 11:00 , attend meeting), repeat every 24 hours for 5 days
...
(16-04-2018 11:00 , eat dinner), **repeat every 7 days for 3 months**
...
(17-04-2018 7:32 , wake up), ← #2
(17-04-2018 7:38 , prepare coffee),
...
(20-04-2018 7:28 , wake up), ← #5
(20-04-2018 7:41 , prepare coffee),
...
(15-06-2018 7:28 , wake up), ← #5 - 9th week
... \rangle

Nested cycles
Tree structure

Tree representation

On *April 16, at 7:30 AM, wake up,*
repeat every 24 hours for 5 days

$\tau = 16-04-2018\ 7:30$

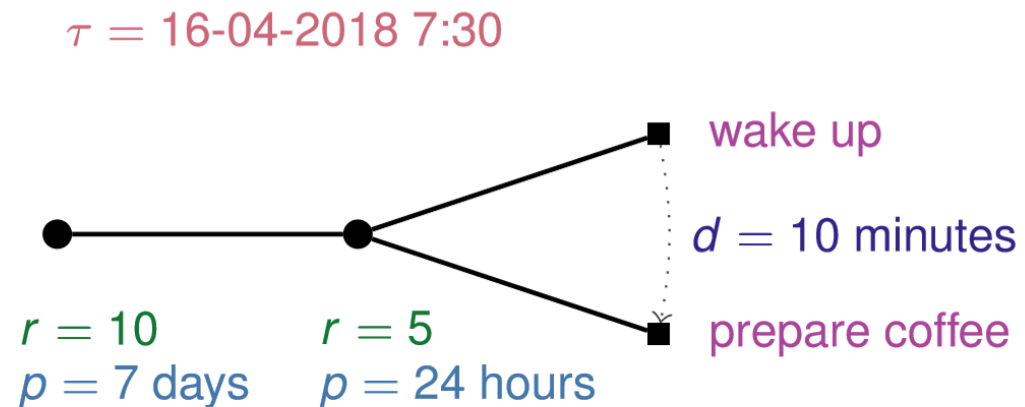
● ————— ■ wake up

$r = 5$

$p = 24\ \text{hours}$

Tree representation

On *April 16, at 7:30 AM*, *wake up*,
10 minutes later, *prepare coffee*,
repeat every 24 hours for 5 days,
repeat this every 7 days for 3 months



Update to problem statement

- Problem statement updated: cycles -> patterns

Problem

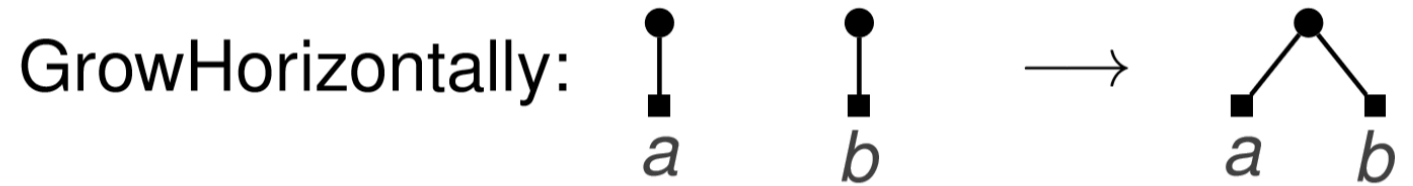
Given an event sequence S , find the collection of patterns \mathcal{P} minimising the cost

$$L(\mathcal{P}, S) = \sum_{P \in \mathcal{P}} L(P) + \sum_{o \in \text{residual}(\mathcal{P}, S)} L(o) .$$

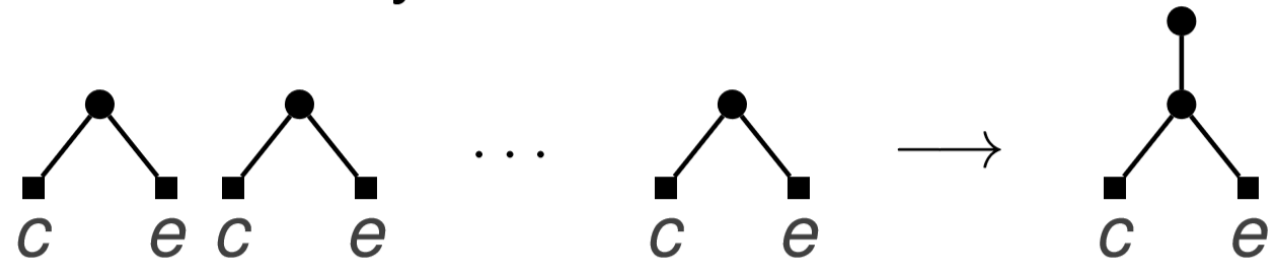
- Encoding $L(\dots)$ defined for the tree patterns

Algorithm 1/2

- Start from cycles (easy to extract)
- Combine them:



GrowVertically:



Algorithm 2/2

We propose an algorithm with three stages:

Extracting cycles: extract cycles for each event in turn, using a dynamic programming routine and a heuristic extracting triples and chaining them

Building tree patterns from cycles: perform combination rounds to generate increasingly complex patterns

Selecting the final pattern collection: solve weighted set cover problem with greedy algorithm

Some qualitative results

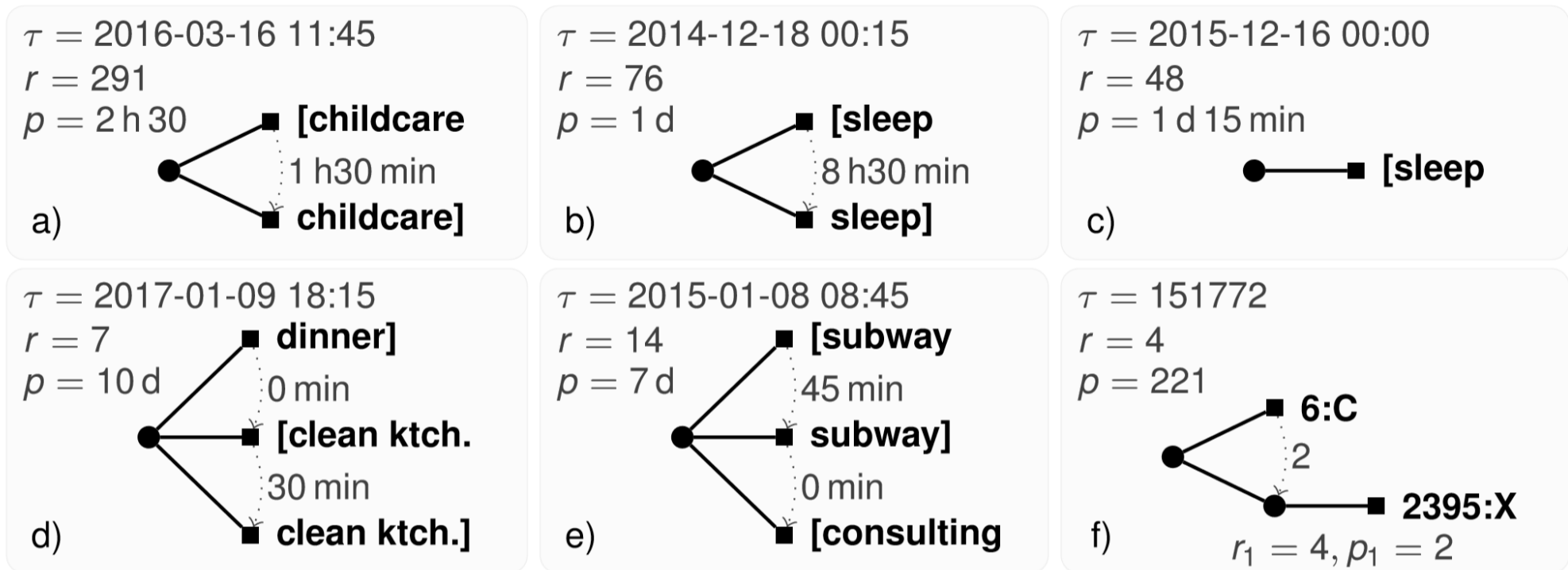


Figure: Example patterns from sacha (a–e) and 3zap (f).

How periodic is your shopping?

Analyzing your market basket tickets, v2.0

Clément Gautrais, René Quiniou, Peggy Cellier, Thomas Guyet, Alexandre Termier:

Purchase Signatures of Retail Customers. PAKDD (1) 2017: 110-121

Clément Gautrais, Peggy Cellier, René Quiniou, Alexandre Termier:

Topic Signatures in Political Campaign Speeches. EMNLP 2017: 2342-2347

Slides adapted from Clément Gautrais

Signatures: detecting and characterizing recurrent behavior in sequential data, Clément Gautrais PhD, 2018

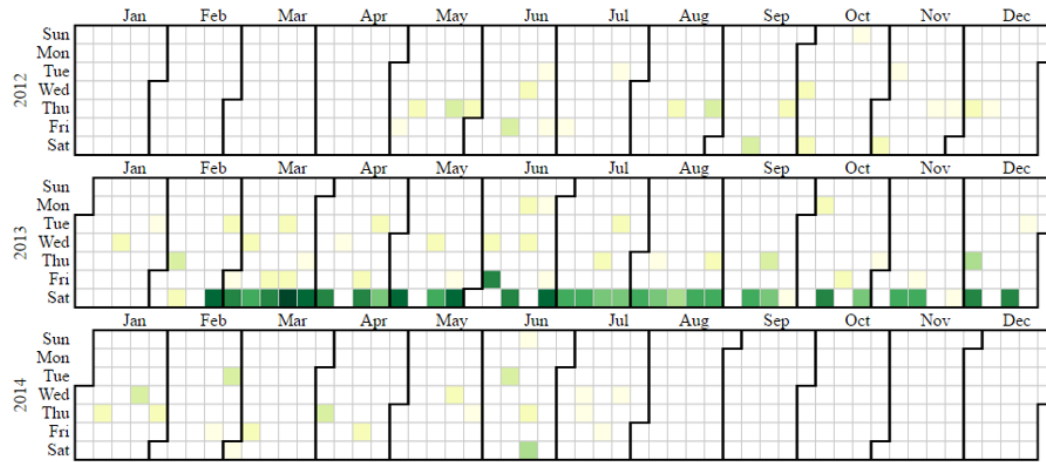
Motivations

- Detection customer habits in market basket data
- => what are the favorite products of customers?
- => how often do they replenish these products?

- Challenges
 - Few results (ideally, ONE pattern with the set of products)
 - Robustness to noise

Example from real data

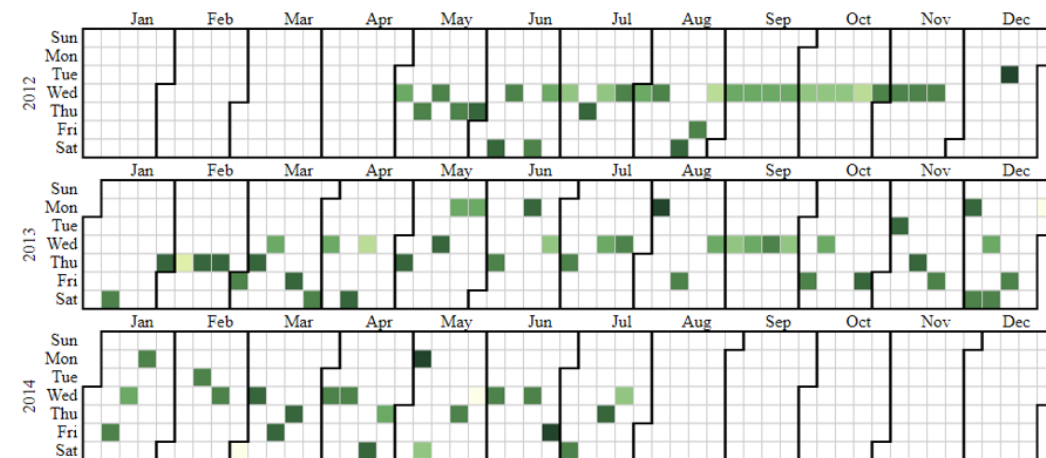
- 2 real customers



Ideal rhythm (replenishment period)

Rare profiles

Might have non ideal purchases



Some regularities

Most profiles











































Challenging!

Signature model intuition

- Find favourite products of a customer
 - Bought several times with some regularity
 - **Not** necessarily in the **same transaction**
- Find **recurrent symbols** and their **occurrences** in a symbolic sequence, with no predefined period
 - **A set** of products and its **occurrences** as results
 - Period adapts to the sequence rhythm

Sequence segmentation

























- k-segmentation [TT06]: split a sequence of n transactions into k segments
















Time	Items	Time	Items
May 3	   	May 3	   
May 5	  	May 5	  
May 10	 	May 10	 
May 17	  	May 17	  
May 18		May 18	
May 20	 	May 20	 
May 24		May 24	
May 31	    	May 31	    

A 3-segmentation of a customer purchase sequence

Segment representative




- Segment representative: $\mu(S_i) = U_{t \in S_i} t$

	Time	Items
S1	May 3	   
	May 5	  
S2	May 10	 
	May 17	  
	May 18	 
S3	May 20	  
	May 24	 
	May 31	    




Segment index	Segment representative $\mu(S_i)$
1	     
2	   
3	    

Adequation

- Adequation: $A(\alpha, S) = |\cap_{S_i \in S} \mu(S_i)|$

Segment index	Segment representatives $\mu(S_i)$
1	
2	
3	

• $A(\alpha, S) = |\cap_{S_i \in S} \mu(S_i)| = |\{\text{cheese, wine, apple, candy, beer, Pringles}\} \cap \{\text{cheese, wine, apple, candy}\} \cap \{\text{cheese, wine, apple, candy, beer}\} \cap \{\text{cheese, wine, apple, candy}\}| = 4$

Segment index	Segment representatives $\mu(S_i)$
1	
2	
3	

Signature problem statement






















- $S_{opt}(\alpha, k) = \operatorname{argmax}_{S \in \mathcal{S}_{n,k}} A(\alpha, S)$
















Time	Items
May 3	   
May 5	  
May 10	 
May 17	  
May 18	
May 20	 
May 24	
May 31	    

+ $k = 3$

- Solve $S_{opt}(\alpha, k)$






















Example














	Time	Items
S1	May 3	   
	May 5	  
S2	May 10	 
	May 17	  
	May 18	
S3	May 20	 
	May 24	
	May 31	    

Segment index	Segment representatives $\mu(S_i)$
1	     
2	   
3	    

- $A(\alpha, S) = 4$






















Example

















	Time	Items
S1	May 3	   
	May 5	  
	May 10	 
	May 17	  
S2	May 18	
	May 20	 
S3	May 24	
	May 31	    

Segment index	Segment representatives $\mu(S_i)$
1	     
2	 
3	    

- $A(\alpha, S) = 2$

Example

	Time	Items
S1	May 3	   
	May 5	  
	May 10	 
S2	May 17	  
	May 18	
	May 20	 
S3	May 24	
	May 31	    

Segment index	Segment representatives $\mu(S_i)$
1	     
2	    
3	    

- $A(\alpha, S) = 5 = \operatorname{argmax}_{S \in \mathcal{S}_{8,3}} A(\alpha, S)$

Signature mining

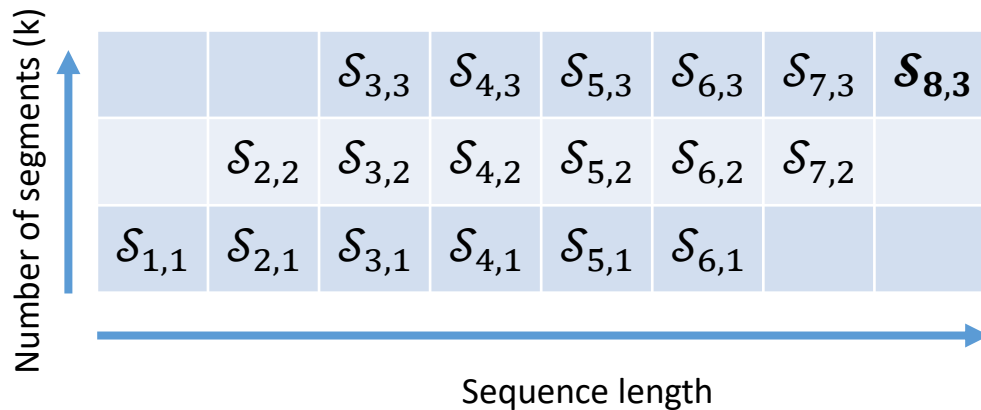
- Mining algorithms: exact approaches
 - Dynamic programming $O(n^2k)$
 - Pattern growth $O(2^{|I|})$
- Mining algorithms: other approaches
 - Greedy algorithms $O(nk)$

Dynamic programming

- Dynamic programming [Bel13]
 - Optimization method based on sub problem decompositions

- Find $\operatorname{argmax}_{S \in \mathcal{S}_{n,k}} A(\alpha, S)$

- First solve $\operatorname{argmax}_{S \in \mathcal{S}_{n_1, k-1} \forall n_1 < n} A(\alpha, S)$



Id	Items	
1		S1
2		
3		S2
4		
5		S3
6		
7		
8		

Dynamic programming (level 1.1)

$\operatorname{argmax}_{S \in \mathcal{S}_{8,3}} A(\alpha, S)$

Id	Items	
1		S1
2		
3		
4		S2
5		
6		S3
7		
8		

		$\mathcal{S}_{3,3}$	$\mathcal{S}_{4,3}$	$\mathcal{S}_{5,3}$	$\mathcal{S}_{6,3}$	$\mathcal{S}_{7,3}$	$\mathcal{S}_{8,3}$
	$\mathcal{S}_{2,2}$	$\mathcal{S}_{3,2}$	$\mathcal{S}_{4,2}$	$\mathcal{S}_{5,2}$	$\mathcal{S}_{6,2}$	$\mathcal{S}_{7,2}$	
$\mathcal{S}_{1,1}$	$\mathcal{S}_{2,1}$	$\mathcal{S}_{3,1}$	$\mathcal{S}_{4,1}$	$\mathcal{S}_{5,1}$	$\mathcal{S}_{6,1}$		

$\operatorname{argmax}_{S \in \mathcal{S}_{7,2}} A(\alpha, S)$

Id	Items	
1		S1
2		
3		
4		S2
5		
6		
7		

\cap

8		S3
---	--	----

Dynamic programming (level 1.2)

$\operatorname{argmax}_{S \in \mathcal{S}_{8,3}} A(\alpha, S)$

Id	Items	
1		S1
2		
3		S2
4		
5		S3
6		
7		
8		

		$\mathcal{S}_{3,3}$	$\mathcal{S}_{4,3}$	$\mathcal{S}_{5,3}$	$\mathcal{S}_{6,3}$	$\mathcal{S}_{7,3}$	$\mathcal{S}_{8,3}$
	$\mathcal{S}_{2,2}$	$\mathcal{S}_{3,2}$	$\mathcal{S}_{4,2}$	$\mathcal{S}_{5,2}$	$\mathcal{S}_{6,2}$	$\mathcal{S}_{7,2}$	
$\mathcal{S}_{1,1}$	$\mathcal{S}_{2,1}$	$\mathcal{S}_{3,1}$	$\mathcal{S}_{4,1}$	$\mathcal{S}_{5,1}$	$\mathcal{S}_{6,1}$		



$\operatorname{argmax}_{S \in \mathcal{S}_{6,2}} A(\alpha, S)$

Id	Items	
1		S1
2		
3		S2
4		
5		S3
6		
\cap		
7		S3
8		

Dynamic programming (level 1.3)

$\operatorname{argmax}_{S \in \mathcal{S}_{8,3}} A(\alpha, S)$

Id	Items	
1		S1
2		
3		S2
4		
5		S3
6		
7		
8		

		$\mathcal{S}_{3,3}$	$\mathcal{S}_{4,3}$	$\mathcal{S}_{5,3}$	$\mathcal{S}_{6,3}$	$\mathcal{S}_{7,3}$	$\mathcal{S}_{8,3}$
	$\mathcal{S}_{2,2}$	$\mathcal{S}_{3,2}$	$\mathcal{S}_{4,2}$	$\mathcal{S}_{5,2}$	$\mathcal{S}_{6,2}$	$\mathcal{S}_{7,2}$	
$\mathcal{S}_{1,1}$	$\mathcal{S}_{2,1}$	$\mathcal{S}_{3,1}$	$\mathcal{S}_{4,1}$	$\mathcal{S}_{5,1}$	$\mathcal{S}_{6,1}$		

$\operatorname{argmax}_{S \in \mathcal{S}_{5,2}} A(\alpha, S)$

Id	Items	
1		S1
2		
3		S2
4		
5		
\cap		
6		S3
7		
8		

Dynamic programming (level 1.3, in depth)

$\operatorname{argmax}_{S \in \mathcal{S}_{8,3}} A(\alpha, S)$

Id	Items	
1		S1
2		
3		S2
4		
5		S3
6		
7		
8		

		$\mathcal{S}_{3,3}$	$\mathcal{S}_{4,3}$	$\mathcal{S}_{5,3}$	$\mathcal{S}_{6,3}$	$\mathcal{S}_{7,3}$	$\mathcal{S}_{8,3}$
	$\mathcal{S}_{2,2}$	$\mathcal{S}_{3,2}$	$\mathcal{S}_{4,2}$	$\mathcal{S}_{5,2}$	$\mathcal{S}_{6,2}$	$\mathcal{S}_{7,2}$	
$\mathcal{S}_{1,1}$	$\mathcal{S}_{2,1}$	$\mathcal{S}_{3,1}$	$\mathcal{S}_{4,1}$	$\mathcal{S}_{5,1}$	$\mathcal{S}_{6,1}$		

$\operatorname{argmax}_{S \in \mathcal{S}_{5,2}} A(\alpha, S)$

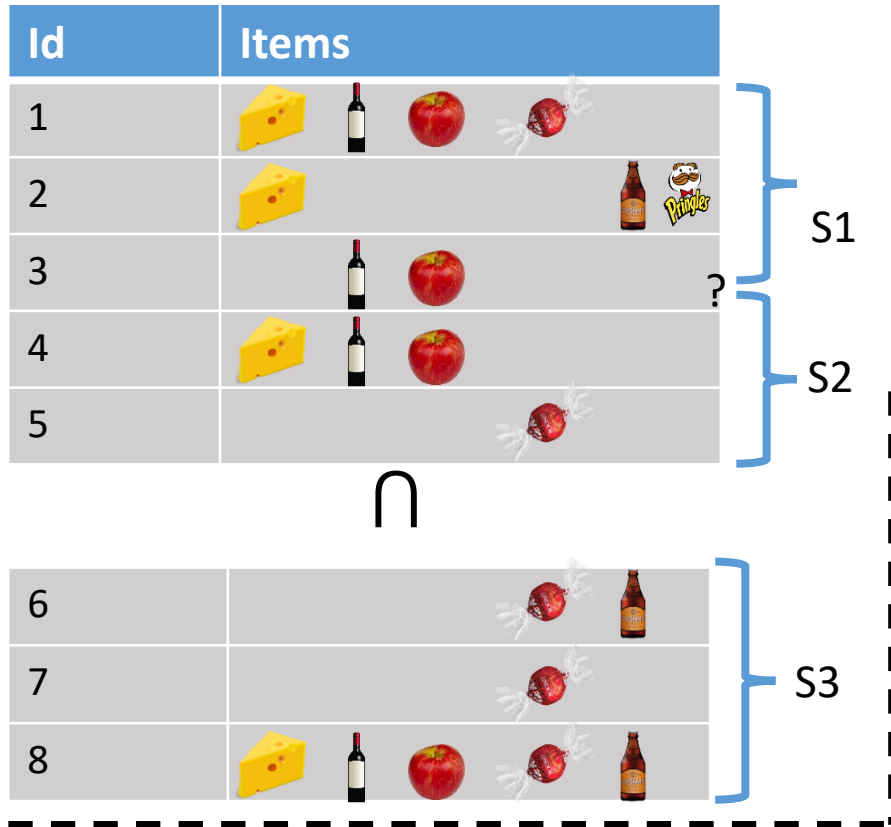
Id	Items	
1		S1
2		
3		S2
4		
5		

\cap

6		S3
7		
8		

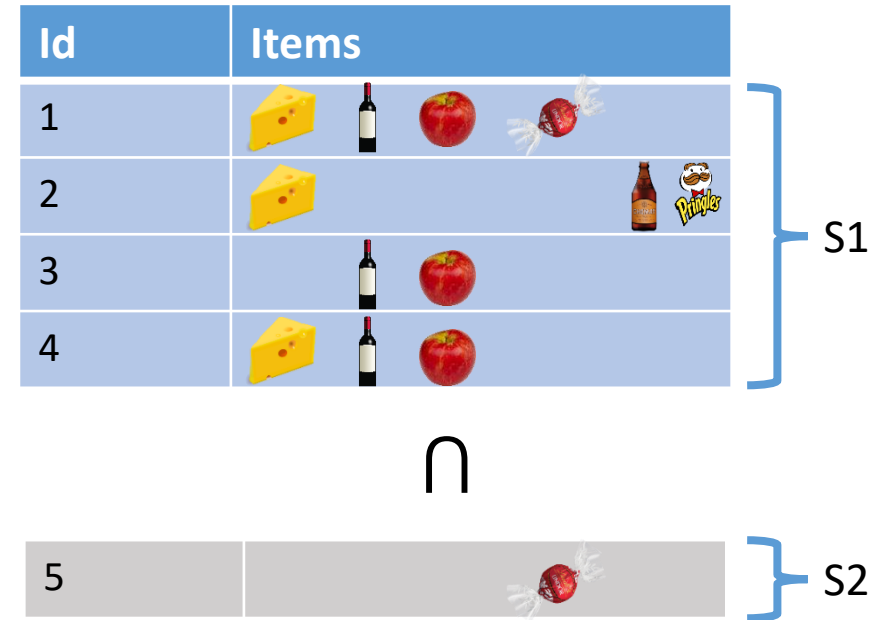
Dynamic programming (level 2.1)

$$\operatorname{argmax}_{S \in \mathcal{S}_{5,2}} A(\alpha, S)$$



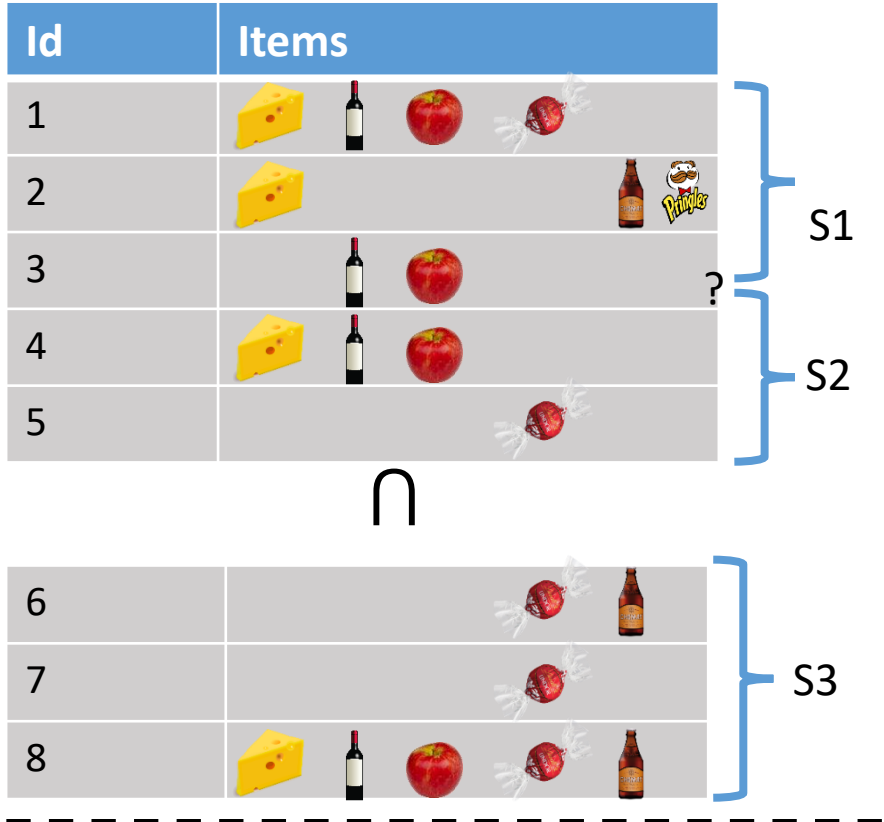
		$\mathcal{S}_{3,3}$	$\mathcal{S}_{4,3}$	$\mathcal{S}_{5,3}$	$\mathcal{S}_{6,3}$	$\mathcal{S}_{7,3}$	$\mathcal{S}_{8,3}$
	$\mathcal{S}_{2,2}$	$\mathcal{S}_{3,2}$	$\mathcal{S}_{4,2}$	$\mathcal{S}_{5,2}$	$\mathcal{S}_{6,2}$	$\mathcal{S}_{7,2}$	
$\mathcal{S}_{1,1}$	$\mathcal{S}_{2,1}$	$\mathcal{S}_{3,1}$	$\mathcal{S}_{4,1}$	$\mathcal{S}_{5,1}$	$\mathcal{S}_{6,1}$		

$$\operatorname{argmax}_{S \in \mathcal{S}_{4,1}} A(\alpha, S)$$



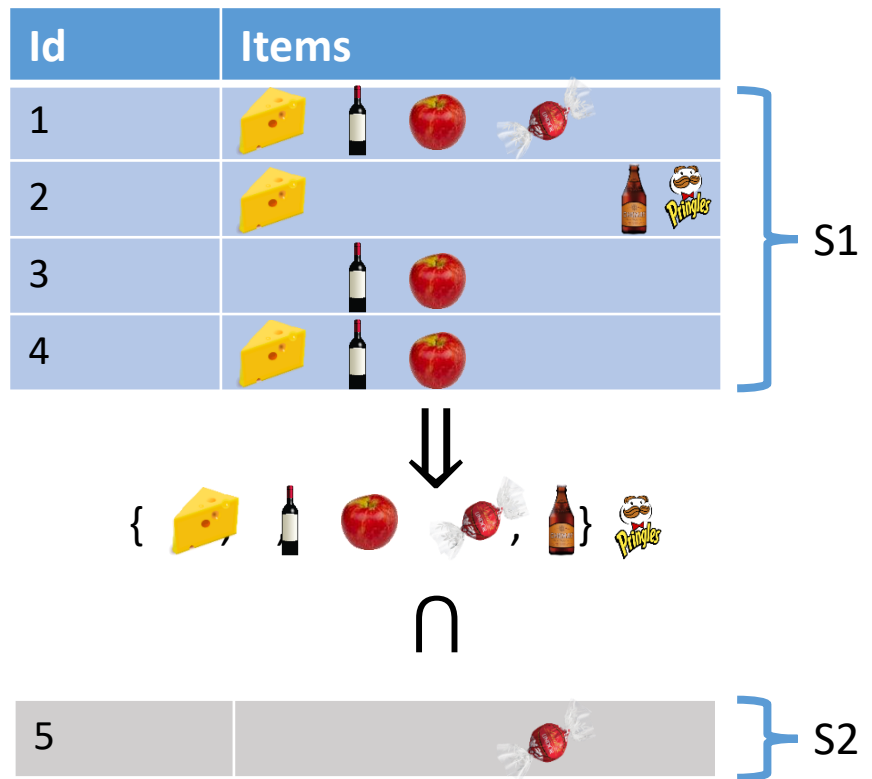
Dynamic programming (level 2.1)

$\operatorname{argmax}_{S \in \mathcal{S}_{5,2}} A(\alpha, S)$



		$\mathcal{S}_{3,3}$	$\mathcal{S}_{4,3}$	$\mathcal{S}_{5,3}$	$\mathcal{S}_{6,3}$	$\mathcal{S}_{7,3}$	$\mathcal{S}_{8,3}$
	$\mathcal{S}_{2,2}$	$\mathcal{S}_{3,2}$	$\mathcal{S}_{4,2}$	$\mathcal{S}_{5,2}$	$\mathcal{S}_{6,2}$	$\mathcal{S}_{7,2}$	
$\mathcal{S}_{1,1}$	$\mathcal{S}_{2,1}$	$\mathcal{S}_{3,1}$	$\mathcal{S}_{4,1}$	$\mathcal{S}_{5,1}$	$\mathcal{S}_{6,1}$		

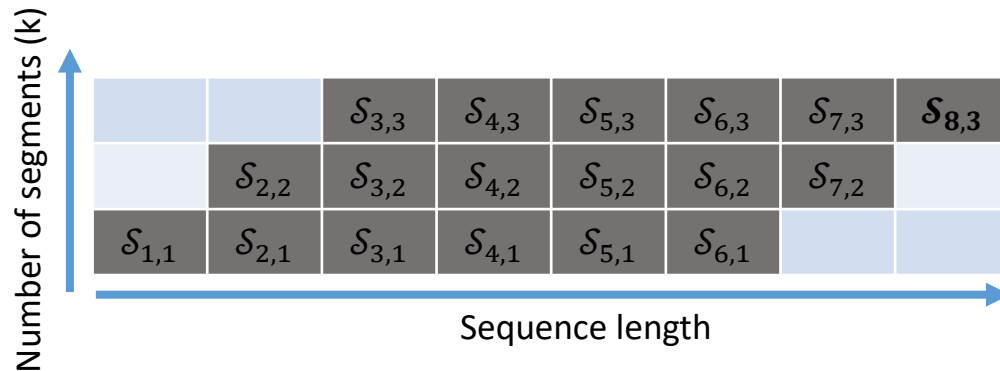
$\operatorname{argmax}_{S \in \mathcal{S}_{4,1}} A(\alpha, S) = 6$
























$\{ \text{Apple} \} = A(\alpha, S) = 1$

Dynamic programming (solution)

- In practice
 - We build the matrix row by row (increasing k)
 - The signature is in cell $[n, k]$



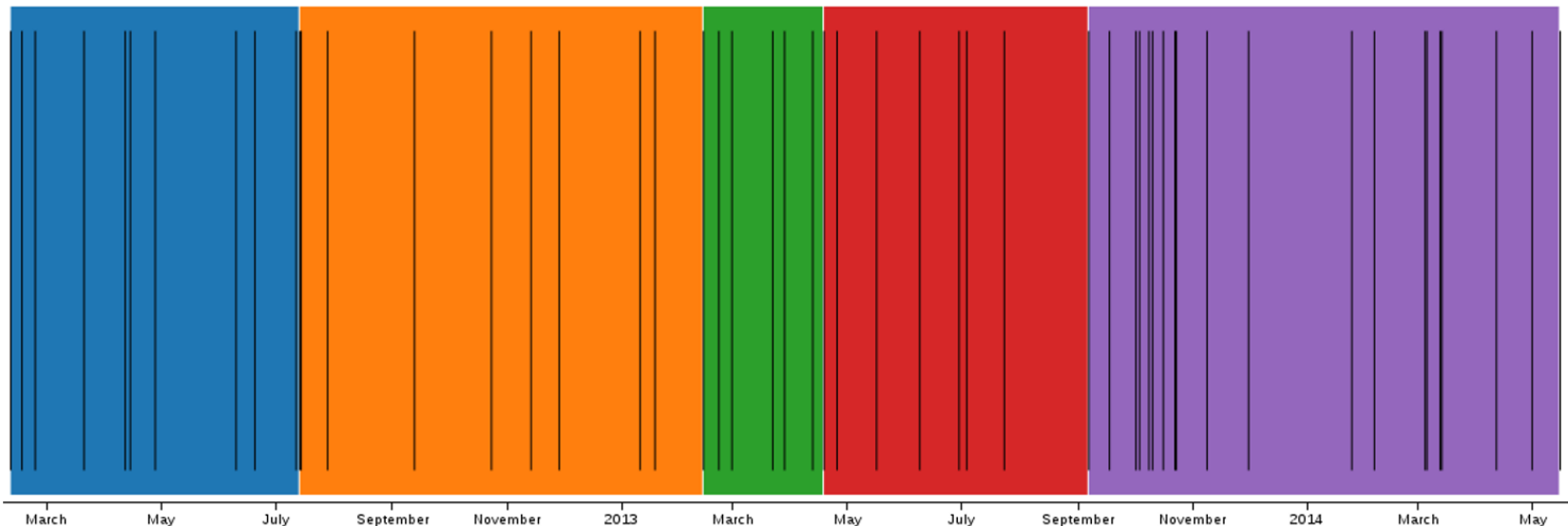
Time	Items
May 3	   
May 5	  
May 10	 
May 17	  
May 18	
May 20	 
May 24	
May 31	    

Extensions

- Sky-signatures: based on pareto dominance / skypatterns
 - See EMNLP'18 paper
 - With an interesting analysis of Trump/Clinton campaign speeches!
- MDL signatures: find THE best signature
 - Joint work with Matthijs van Leeuwen
 - Paper should be accepted at some point...
 - *For the impatient: see PhD of Clément Gautrais*

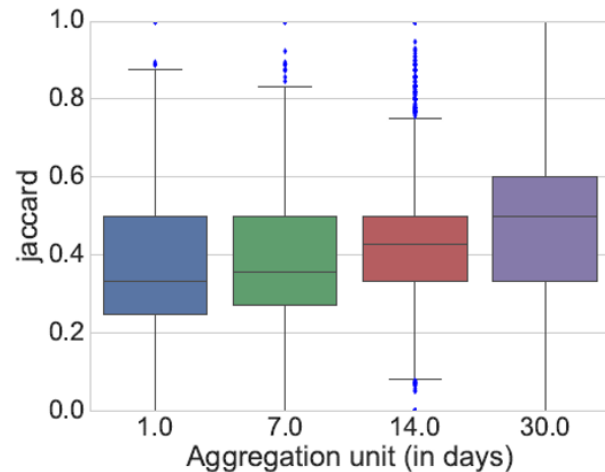
Example signature (real customer data)

- JOKER MULTIFRUIT BRK OVALINE1L
- SIROP SPORT CITROR BTL 1L
- BRETS CHIPS POULET BRAISE 6X25
- RANOU ROTI PORC 6TR 240G
- MINI BABYBEL X12 264G
- IDS CREME CASSIS 20D 70CL
- MT BLANC VANILLE MINI 6X125G
- J.ROZE S.HACHE LETENDR X10 1K
- 1ER PRIX BEURRE 1/2S PQ 500G
- ECRJAD COLOSSE CHOC.BLC4X120
- RANOU ROTI DE PORC 4TR 160G
- PASQUIER BISCOTTE MINC.36T 300
- RANOU JBON MON PARIS DD6T270G
- KINDER PINGUI CHOCOLAT 8X30G
- PASQUIER 12 CROISSANTS 480G

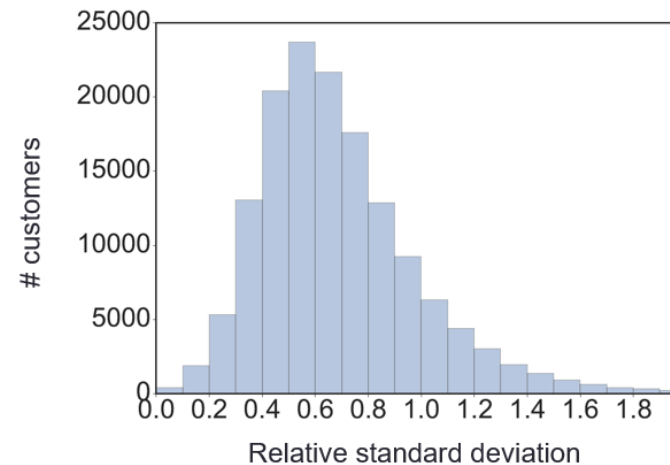


Signature VS periodic patterns

- Periodic pattern
 - Should the repetition constraint be more constrained?



Jaccard similarity between the signature and the longest periodic pattern.



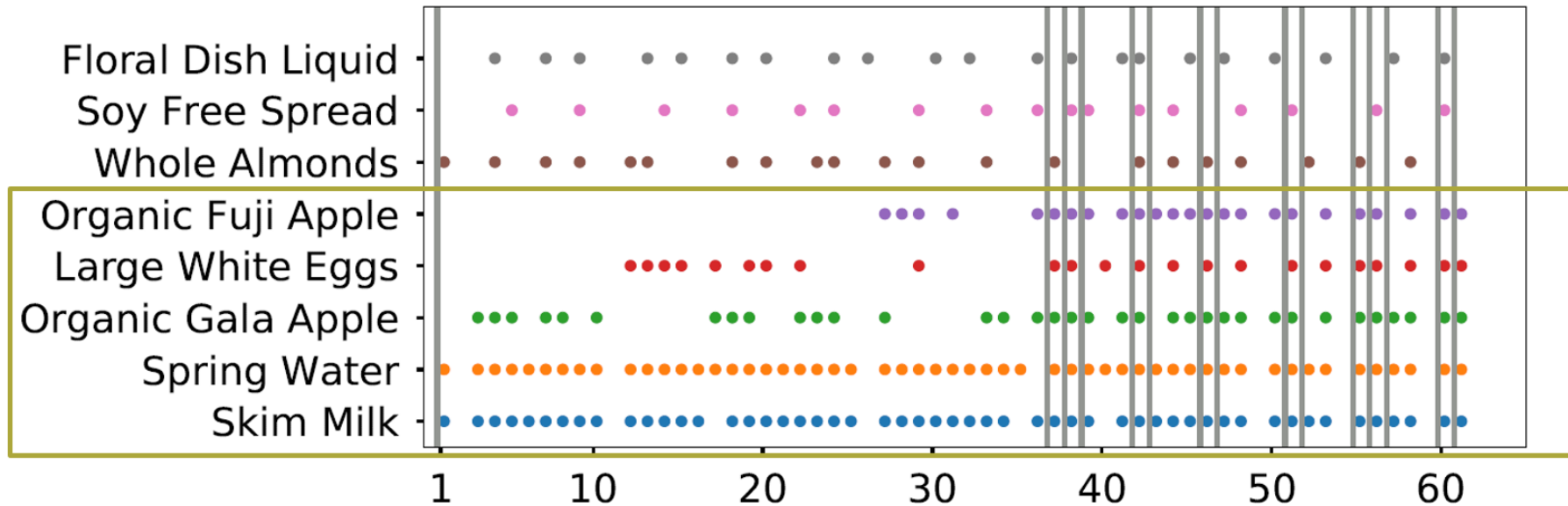
Relative standard deviation of the segment length

- 50% of the signature is composed of products from the longest periodic pattern
- The signature detects **periodic products**, along with **non periodic regular products**
- The signature produces **stable segments**

Real use case – Instacart data (Kaggle)

- Best signature found
 - Lowest encoded length
 - Fast and recent purchase habits

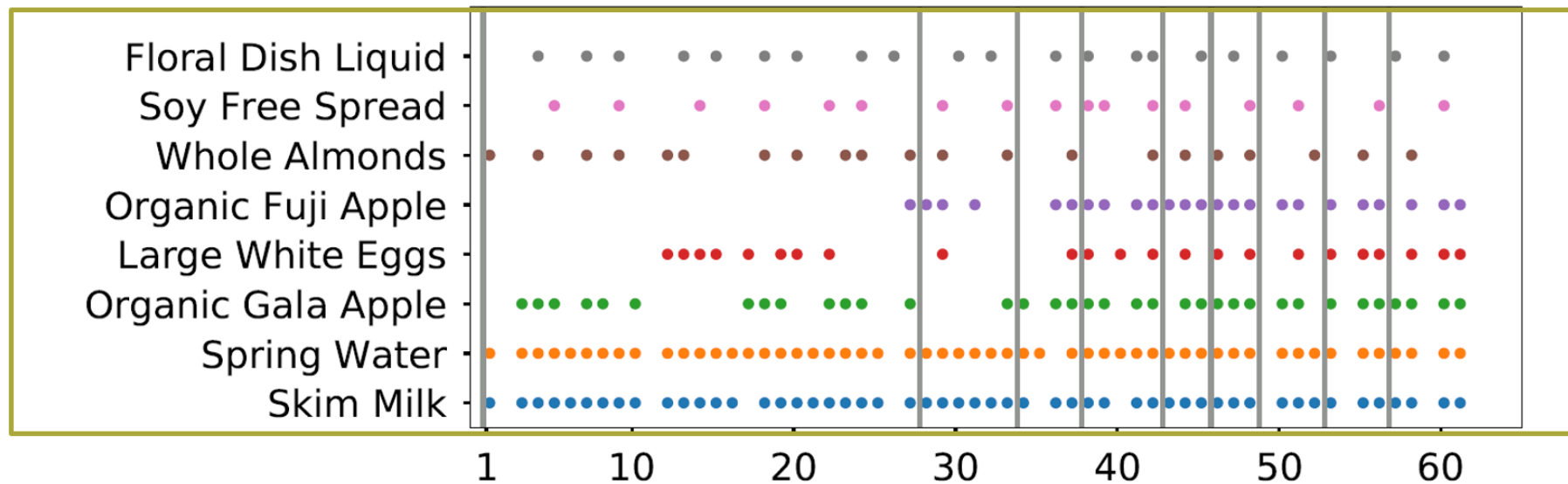
Length	Signature products	Segmentation
1924.72	Skim Milk, Spring Water, Organic Gala Apple, Large White Eggs, Organic Fuji Apple	1,36 37, 37 38, 38 39,41 42, 42 43, 45 46,46 47, 50 51, 51 52,54 55, 55 56, 56 57,59 60, 60 61, 61



Real use case – Instacart data (Kaggle)

- Second best signature found
 - Slower purchase rhythm

Length	Signature products	Segmentation
1924.72	Skim Milk, Spring Water, Organic Gala Apple, Large White Eggs, Organic Fuji Apple	1,36 37, 37 38, 38 39,41 42, 42 43, 45 46,46 47, 50 51, 51 52,54 55, 55 56, 56 57,59 60, 60 61, 61
1983.30	First signature + Whole Almonds +Soy Free Spread +Floral Dish Liquid	1,27 28, 33 34, 37 38,42 43, 45 46, 48 49,52 53, 56 57, 61



Conclusion

- Three approaches for mining temporal regularities presented
 - Quite strict cycles, gaps allowed between cycles, transaction data, condensed representation
 - Tolerant + nested cycles, sequence data, MDL
 - Segmentation, transaction data, optimisation/Pareto/MDL
- Many other interesting problems await
- Surprisingly few people in that research area (since 1999)

Perspectives

- Robustness, robustness, robustness
 - Most periodic pattern definitions break too easily
 - -> prevent the discovery of more general/covering patterns
- Take into account domain knowledge
- Provide easy to use implementations
 - Introducing the Scikit-Mine project

Thank you for your attention!