

Computer-Based Visualization

Data Mining and Visualization

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Web site of the course (Remember)

- <http://people.irisa.fr/Alexandre.Termier/dmv/>
- Web site contains:
 - General information
 - Up-to-date schedule (will be the reference)
 - Links to documents

Definition

Computer-based visualization systems provide **visual representations of datasets** designed to **help people carry out tasks more effectively**

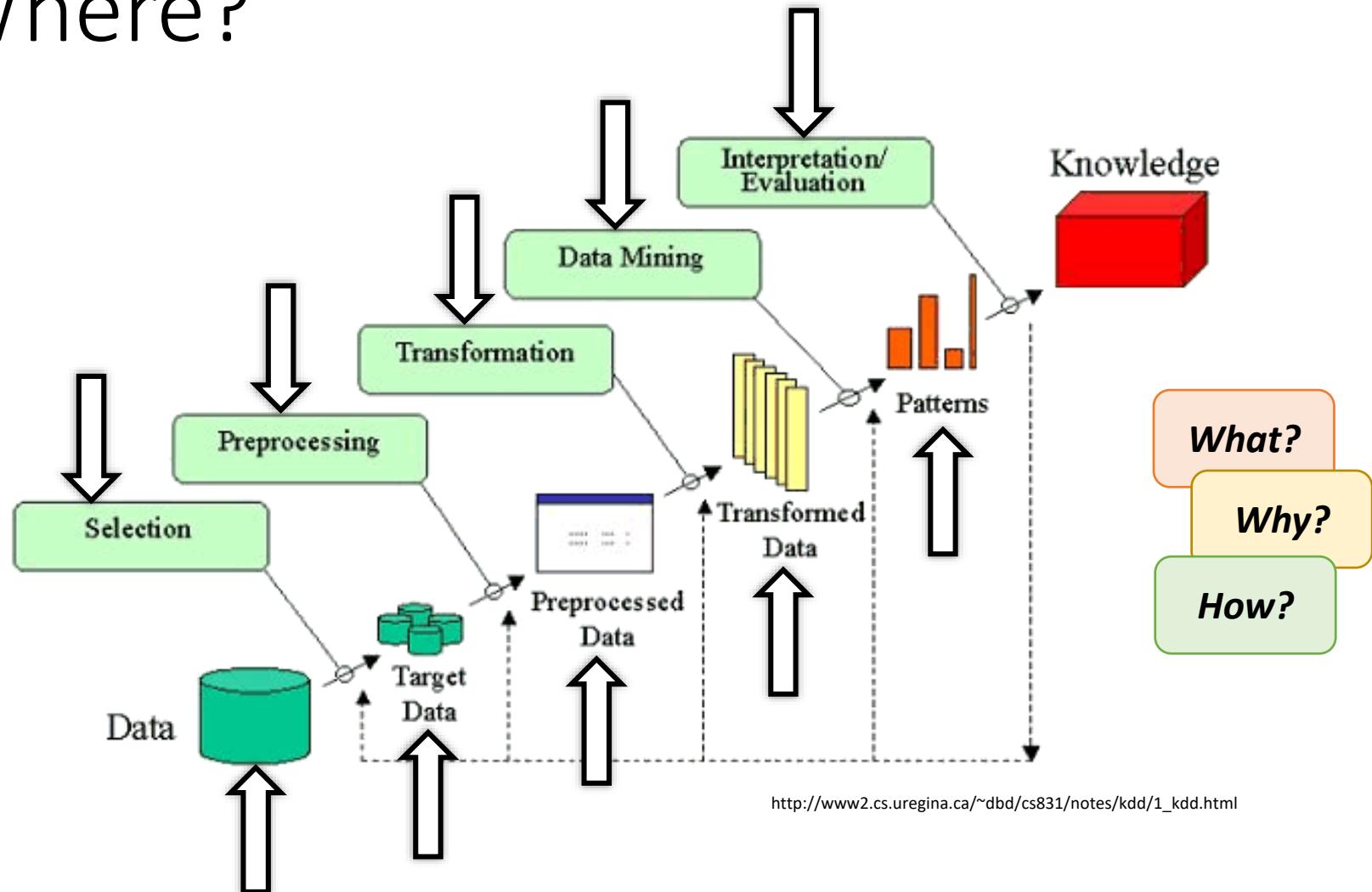


Context

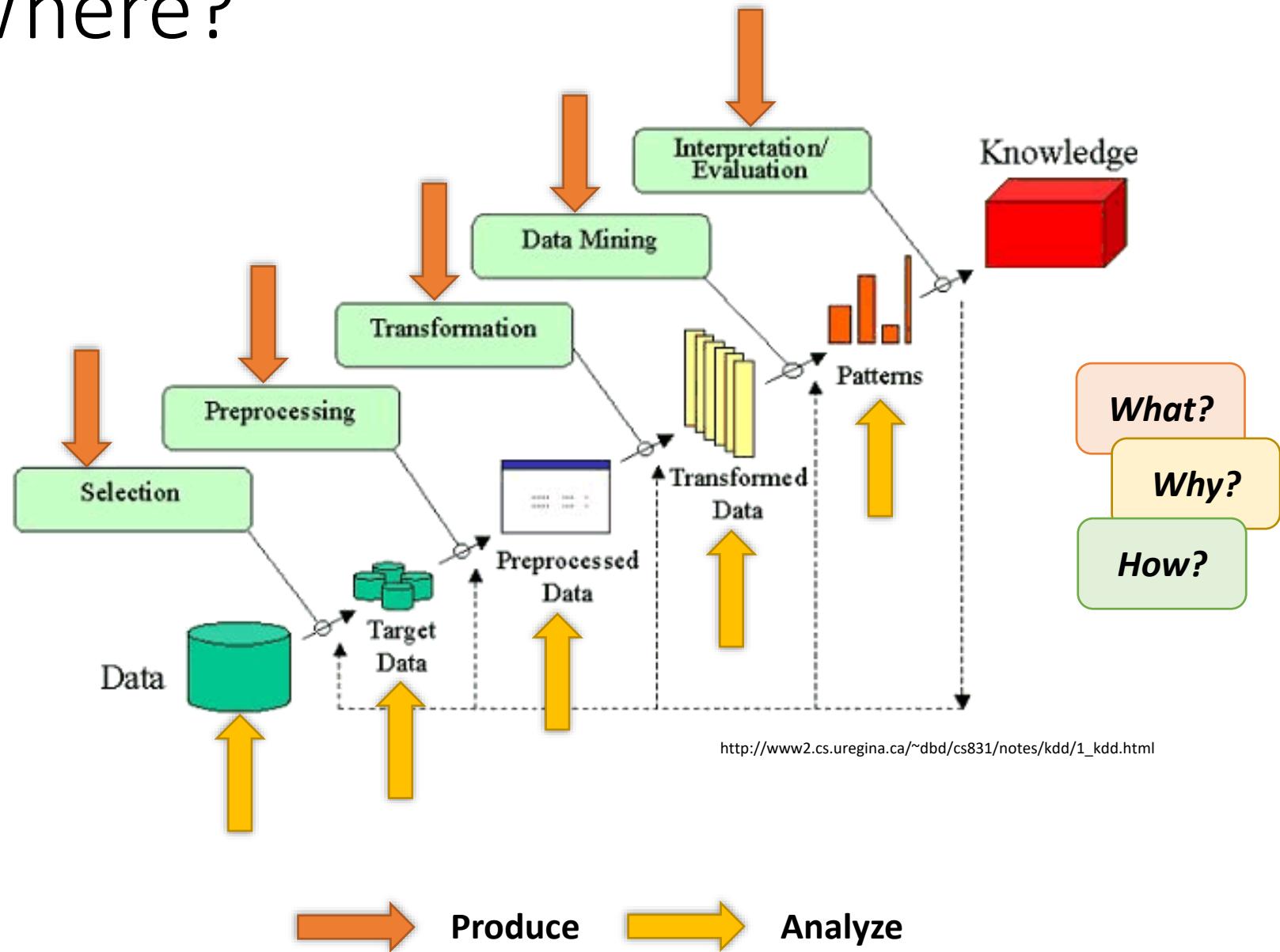
Visualization is suitable when there is a **need to augment human capabilities** rather than replace people with computational decision-making methods

- Need to present results to users -> data visualization
 - Huge lack of communication between data mining / data vis community
 - This course: a small step to improve this communication

Where?

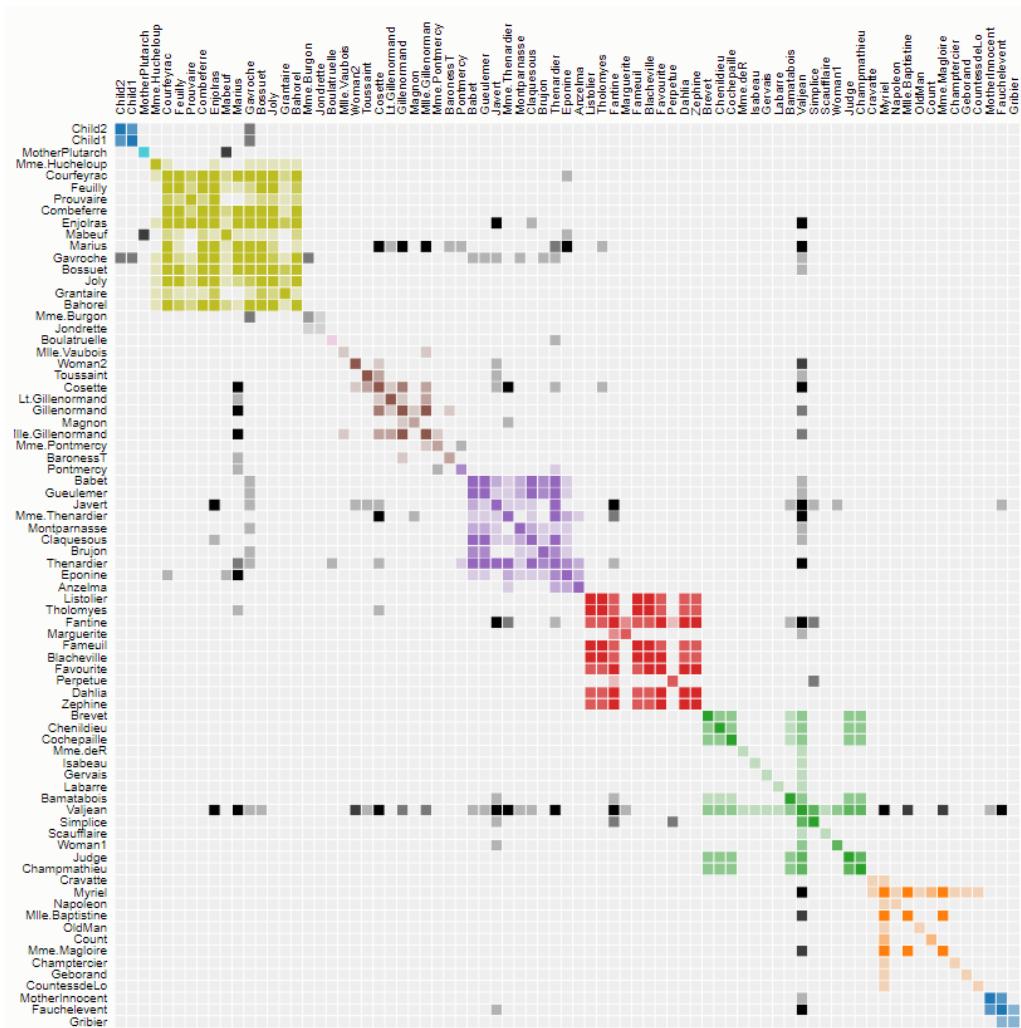


Where?



Simple Example

- 1.1.1:MY,NP;MY,MB
- 1.1.2:MY,ME;ME,MB
- 1.1.3:MY
- 1.1.4:MY,ME;MY,CL;MY,GE;MY,MC;MY,MB
- 1.1.5:MY,MB,ME
- 1.1.6:ME,MY
- 1.1.7:MY,CV;MY,MB,ME
- 1.1.8:SN,MY
- 1.1.9:MB
- 1.1.10:MY,GG
- 1.1.11:MY
- 1.1.12:MY
- 1.1.13:MY
- 1.1.14:MY,SN
- 1.2.1:JL,JV;JV,MT;MR,JV
- ...

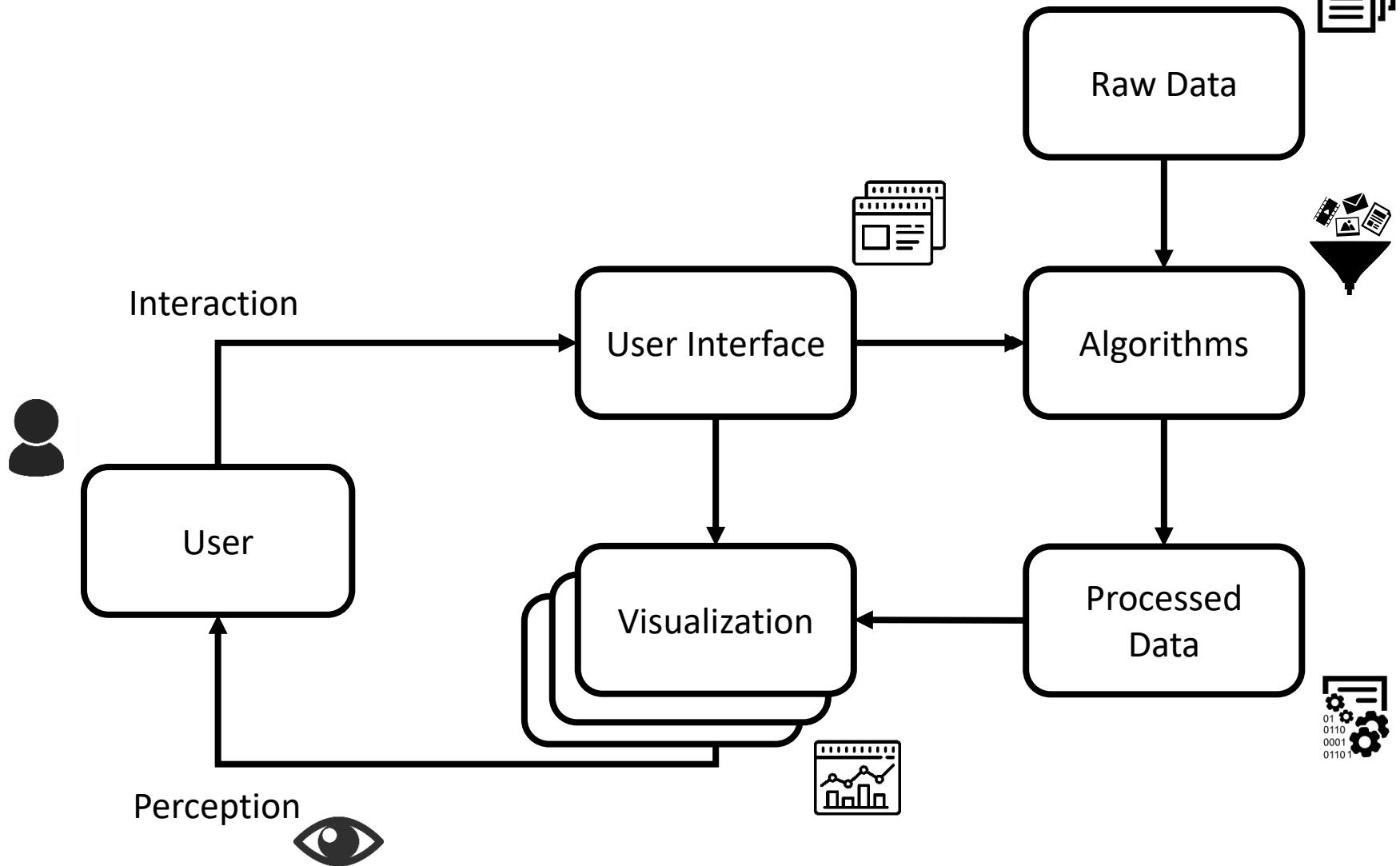


<https://bost.ocks.org/mike/miserables/>

Context

- Scientific visualization is mostly concerned with:
 - 2, 3, 4 dimensional, spatial or spatio-temporal data
 - Discretized data
- Information visualization focuses on:
 - High-dimensional, abstract data
 - Discrete data
 - Financial, statistical, etc
 - Visualization of large trees, networks, graphs
 - Data mining: finding patterns, clusters, voids, outliers

System Overview



Content

- Introduction
- Data abstraction
- Task abstraction
- Visualization Design
- Validation

Introduction

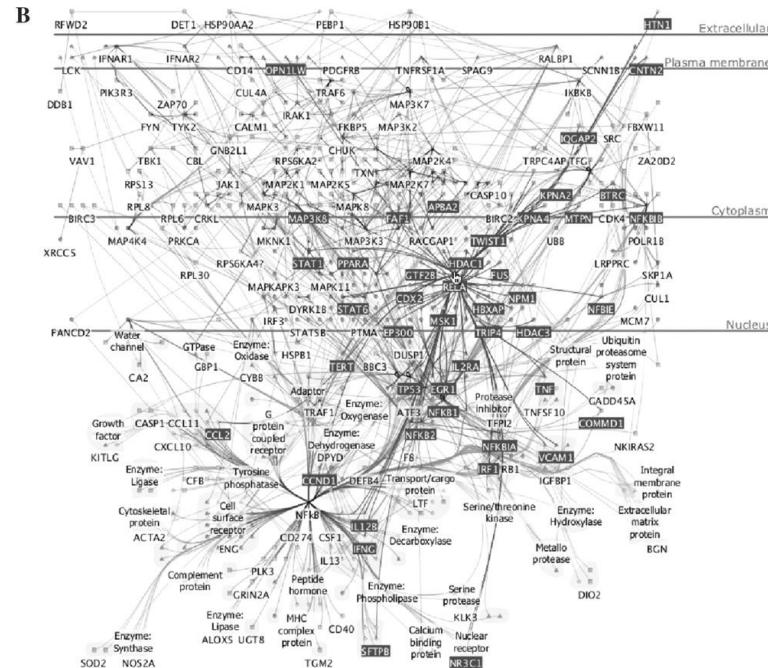
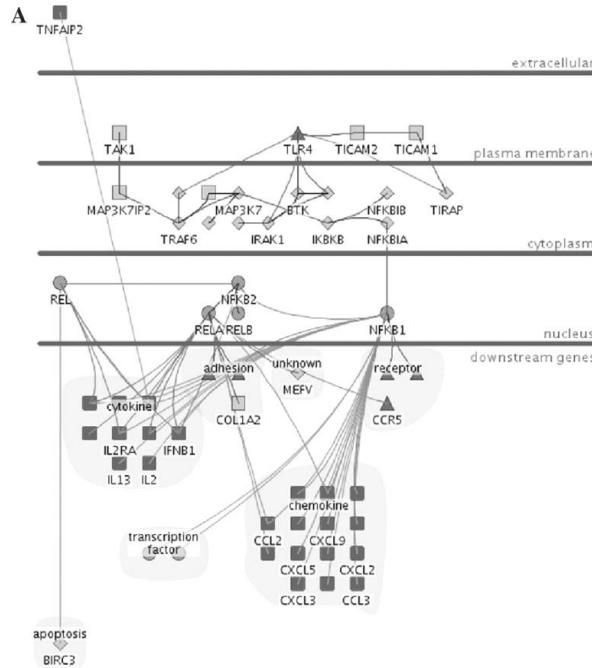
Why data vis (in general)?

Overview



Bring the computer in the loop

- Enable the exploration of large datasets
 - Temporal dimension



Cerebral: a Cytoscape plugin for layout of and interaction with biological networks using subcellular localization annotation.
Aaron Barsky Jennifer L. Gardy Robert E. W. Hancock Tamara Munzner. Bioinformatics, Volume 23, Issue 8, 2007, 1040–1042.



Bring the computer in the loop

- Computational capacity
 - Scalability: How to deal with increasingly data sizes?
- Display capacity
 - Information density: limit of the displayed information



Bring the human in the loop

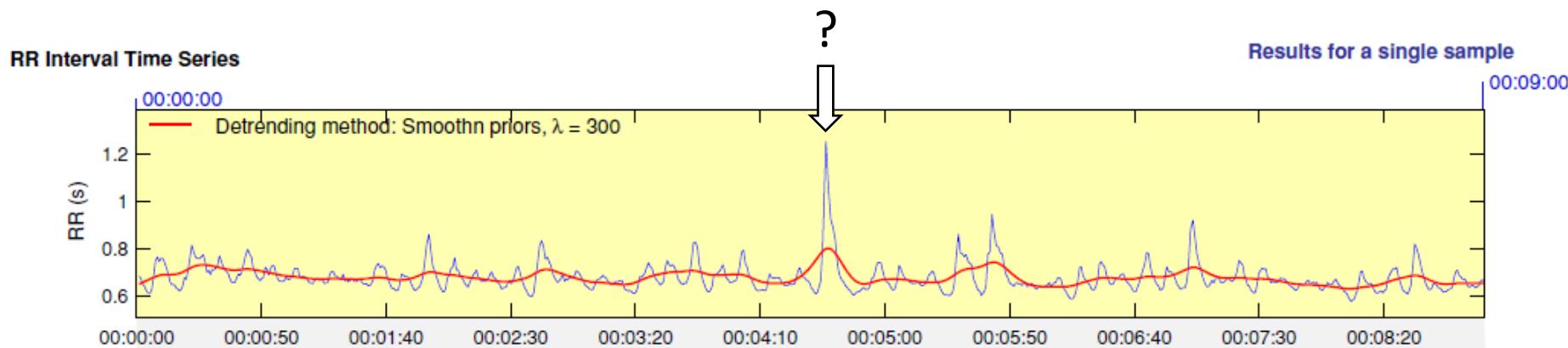


Digiscope - Univ. Paris Saclay
<http://www.digiscope.fr>

Bring the human in the loop



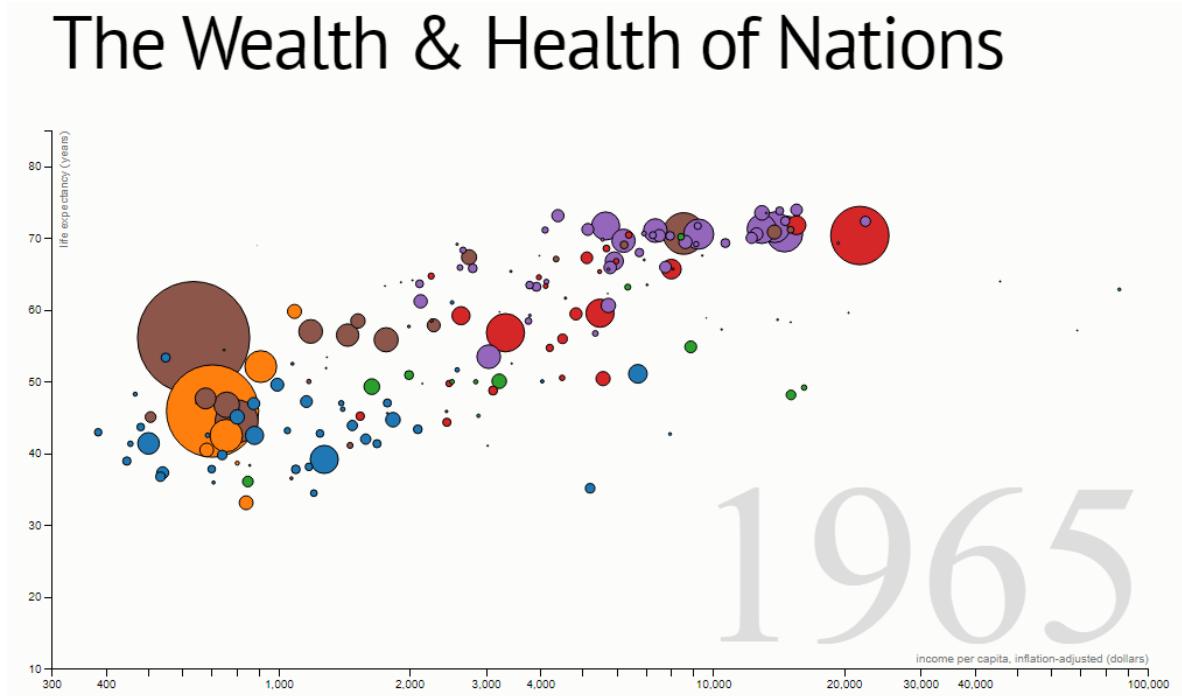
- The question is not known in advance
 - The analysis process is driven by the user
 - Take advantage of the ability of humans to find patterns
- Augment the human decision process
 - Improve decision making





Provide external representations

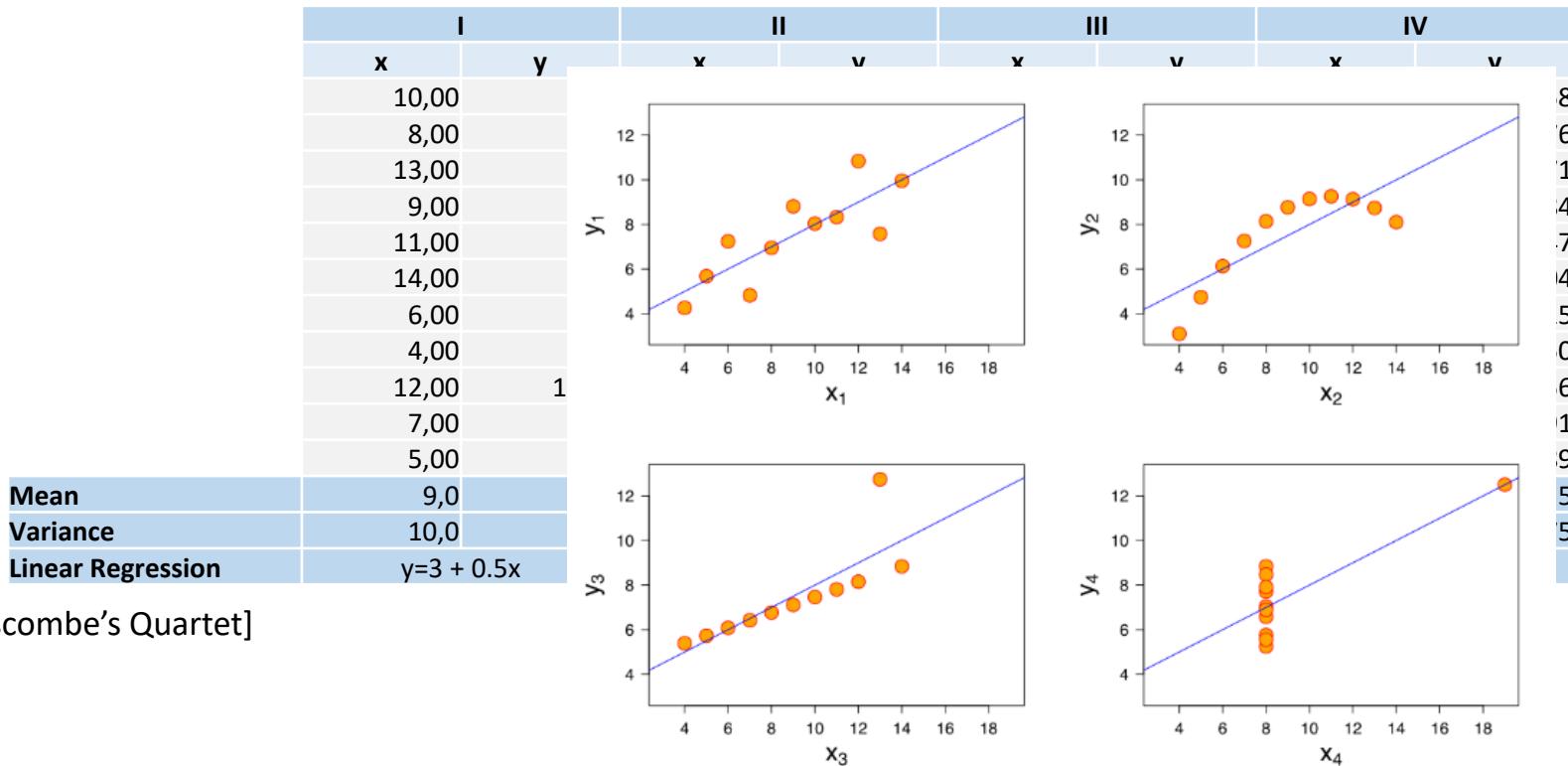
- Offload internal cognition and memory usage to the perceptual system
 - Data organized by spatial location
 - Support perceptual inference
 - Select just the relevant information





Show the data in detail

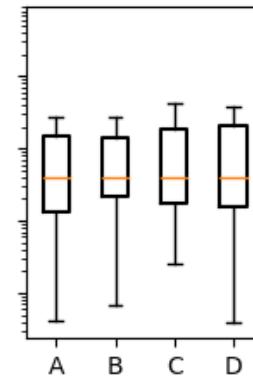
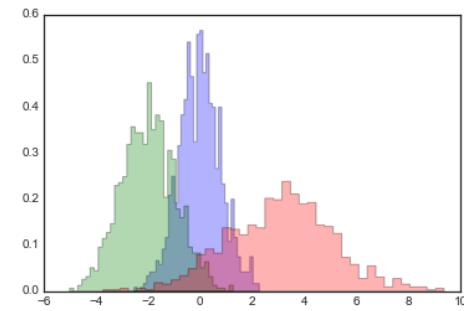
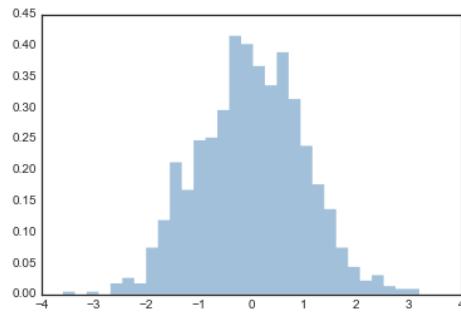
- The dataset structure in detail is better just a summary
 - Explore the data to find patterns





Show the data in detail

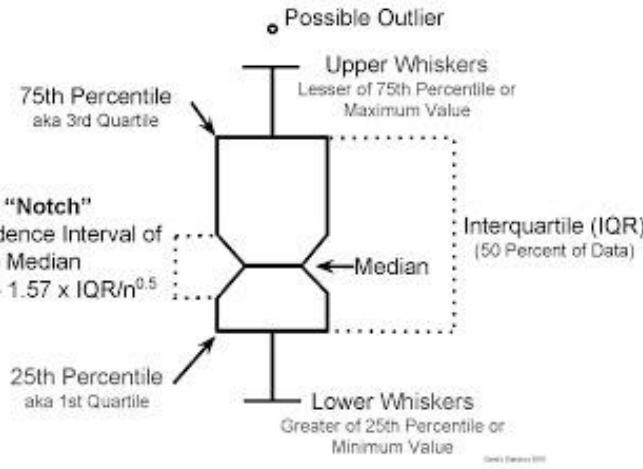
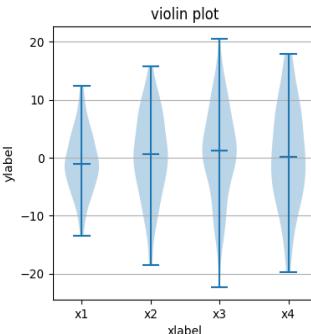
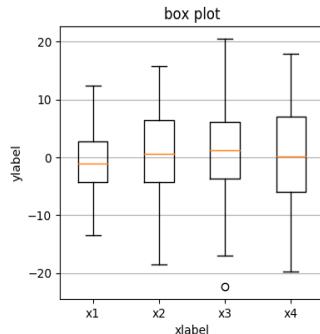
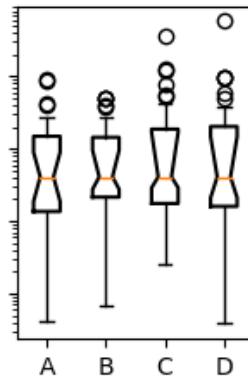
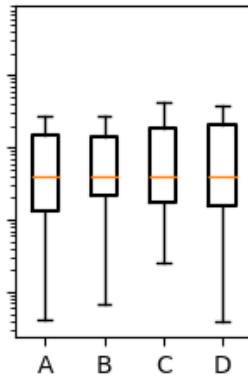
- The dataset structure in detail is better just a summary
 - Explore the data to find patterns





Show the data in detail

- The dataset structure in detail is better just a summary
 - Explore the data to find patterns

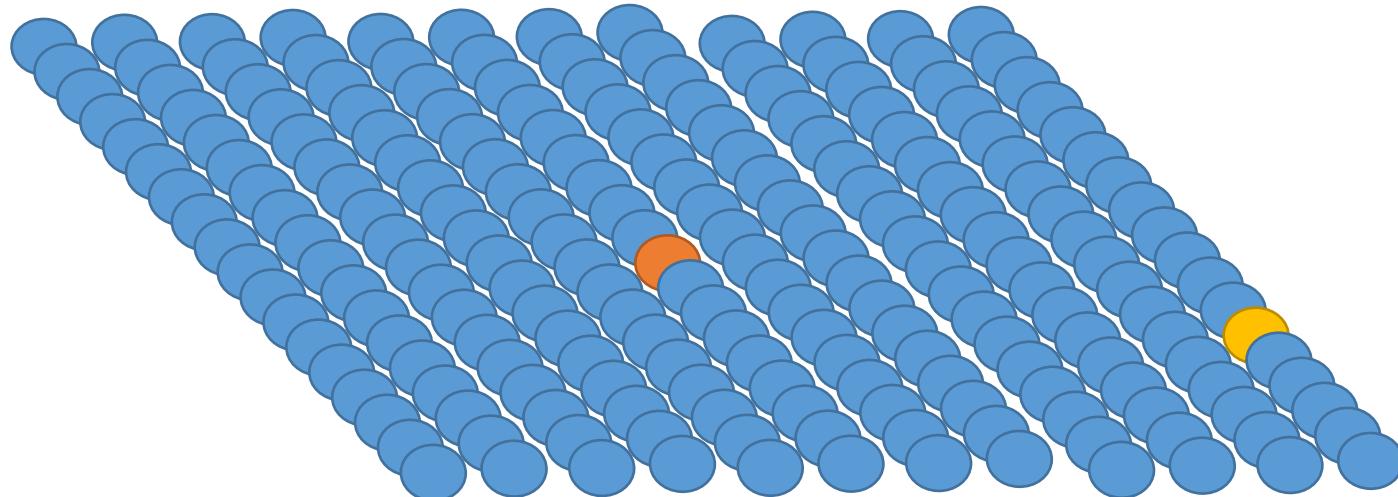


Chambers, John M., William S. Cleveland, Beat Kleiner, and Paul A. Tukey. **"Comparing Data Distributions."** In Graphical Methods for Data Analysis, 62. Belmont, California: Wadsworth International Group;, 1983. ISBN 0-87150-413-8 International ISBN 0-534-98052-X



Depend on vision...

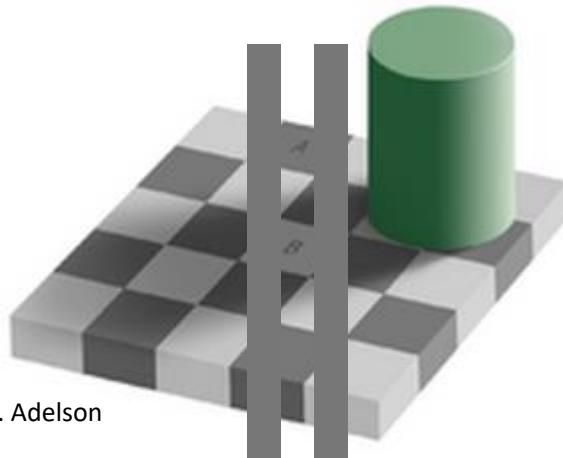
- The Visual system is a high-bandwidth channel of information
 - A significant amount of visual information is done in parallel at the preconscious level



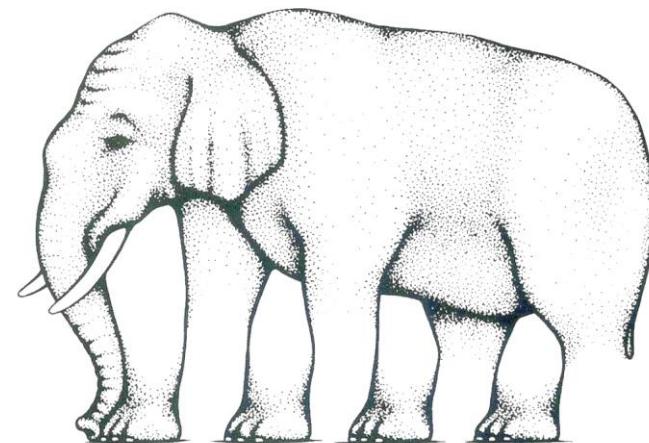


... but be careful

- Need to know its strengths and limitations



Edward H. Adelson





... but be careful

- Need to know its strengths and limitations
- Human perceptual and cognitive capacity limits?



THE ATTENTION TEST

<https://www.youtube.com/watch?v=uO8wpm9HSB0>



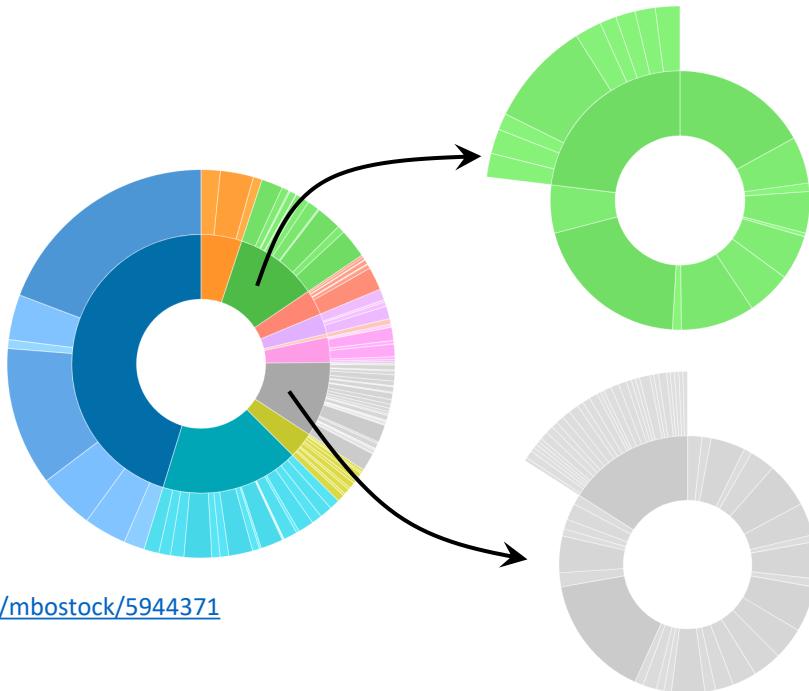
... but be careful

- Need to know its strengths and limitations
- Human perceptual and cognitive capacity limits?
 - Change blindness: the phenomenon where even very large changes are not noticed if we are attending to something else in our view



Interactivity

- For big datasets, the user nor the display can enable the visualization of the entire dataset at once

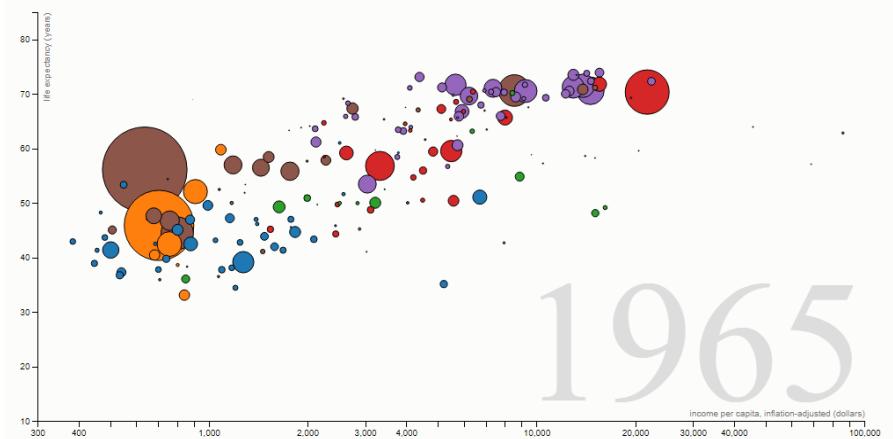
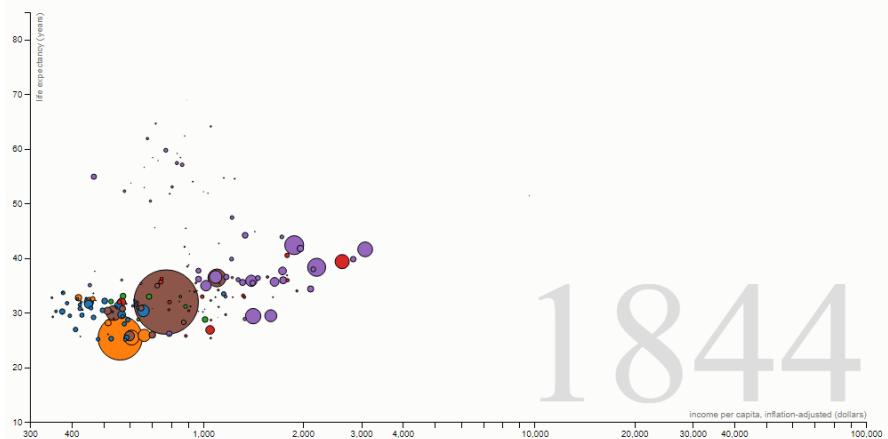


<https://bl.ocks.org/mbostock/5944371>



Interactivity

- A static view only allows for a single view of a limited number of dimensions

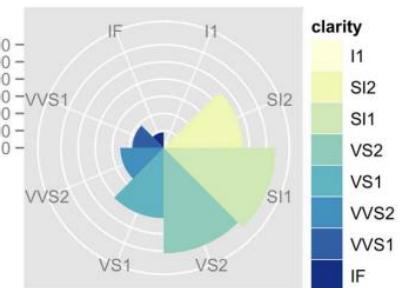
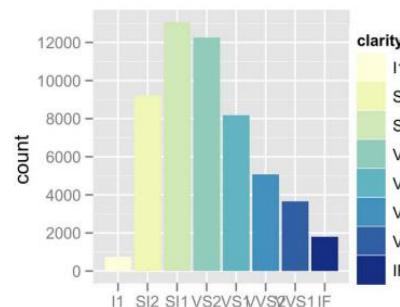
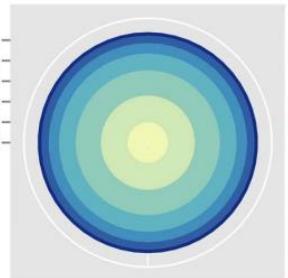
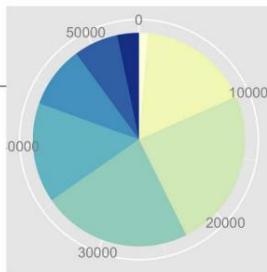


<https://bostocks.org/mike/nations/>



Interactivity

- A static view only allows for a single view of a limited number of dimensions
- The same dataset can be sorted using a number of different criteria



Hadley Wickham *A Layered Grammar of Graphics*. Journal of Computational and Graphical Statistics Vol. 19 , Iss. 1,2010



Interactivity

datavoyager

Bookmarks (1) Undo Redo

Data

Cars Change

Fields

A Cylinders T+
A Name T+
A Origin T+
T Year T+
Acceleration T+
Displacement T+
Horsepower T+
Miles per Gallon T+
Weight in lbs T+
COUNT +

Wildcards

A Categorical Fields +
Temporal Fields +
Quantitative Fields +

Filter Filter invalid numbers

Encoding Clear

Specified View

No specified visualization yet. Start exploring by dragging a field to encoding pane on the left or examining univariate summaries below.

Related Views

Univariate Summaries

A Cylinders # COUNT A Name # COUNT A Origin # COUNT YEAR(YEAR) # COUNT

A Cylinders COUNT
Cylinders
0 50 100 150 200
3
4
5
6
8
200

A Name COUNT
0 1 2 3 4 5 6
amc ambassador brougham
amc ambassador dpl
amc ambassador dl
amc concord
amc concord dl
amc concord dl 6
amc gremlin
amc hornet
amc hornet sportabout
amc matador
amc matador (sw)
amc pacer
amc pacer dl
amc rebel sst
amc rebel sst (sw)
amc spirit dl
audi 100s
audi 100s
audi 4000
audi 4000
audi 5000 (diesel)
audi fox
bmw 2002
bmw 320i
buick century

A Origin COUNT
0 50 100 150 200 250
Europe
Japan
USA
250

YEAR(YEAR) COUNT
1970 1972 1974 1976 1978 1980 1982
65
60
55
50
45
40
35
30
25
20
15
10
5
0

BIN(Acceleration) # COUNT # BIN(Displacement) # COUNT # BIN(Horsepower) # COUNT # BIN(Miles per Gallon) # COUNT

BIN(Acceleration) COUNT
BIN(Acceleration)
0 10 12 14 16 18 20 22 24 26
130
120
110
100
90
80
70
60
50
40
30
20
10
0

BIN(Displacement) COUNT
BIN(Displacement)
50 100 150 200 250 300 350 400 450 500
110
100
90
80
70
60
50
40
30
20
10
0

BIN(Horsepower) COUNT
BIN(Horsepower)
40 60 80 100 120 140 160 180 200 220 240
120
110
100
90
80
70
60
50
40
30
20
10
0

BIN(Miles_per_Gallon) COUNT
BIN(Miles_per_Gallon)
10 15 20 25 30 35 40 45 50
100
90
80
70
60
50
40
30
20
10
0

<https://vega.github.io/voyager2/>

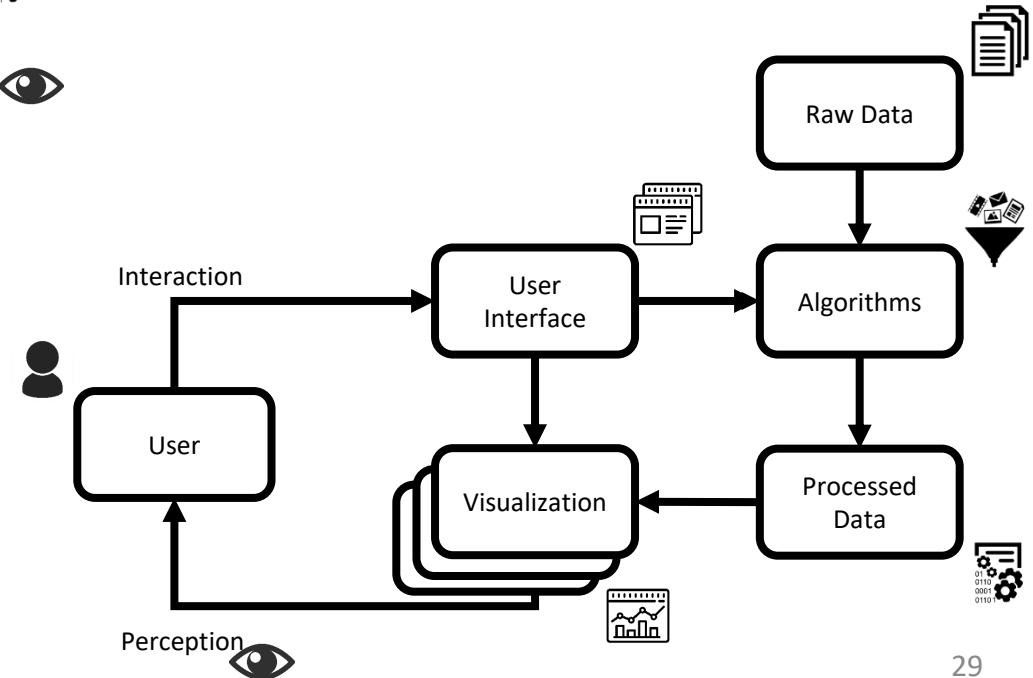
Wrap Up

What?

Why?

How?

- Bring the computer in the loop 
- Bring the human in the loop 
- Provide external representations 
- Show data in detail 
- Depend on vision 
- Interactivity 



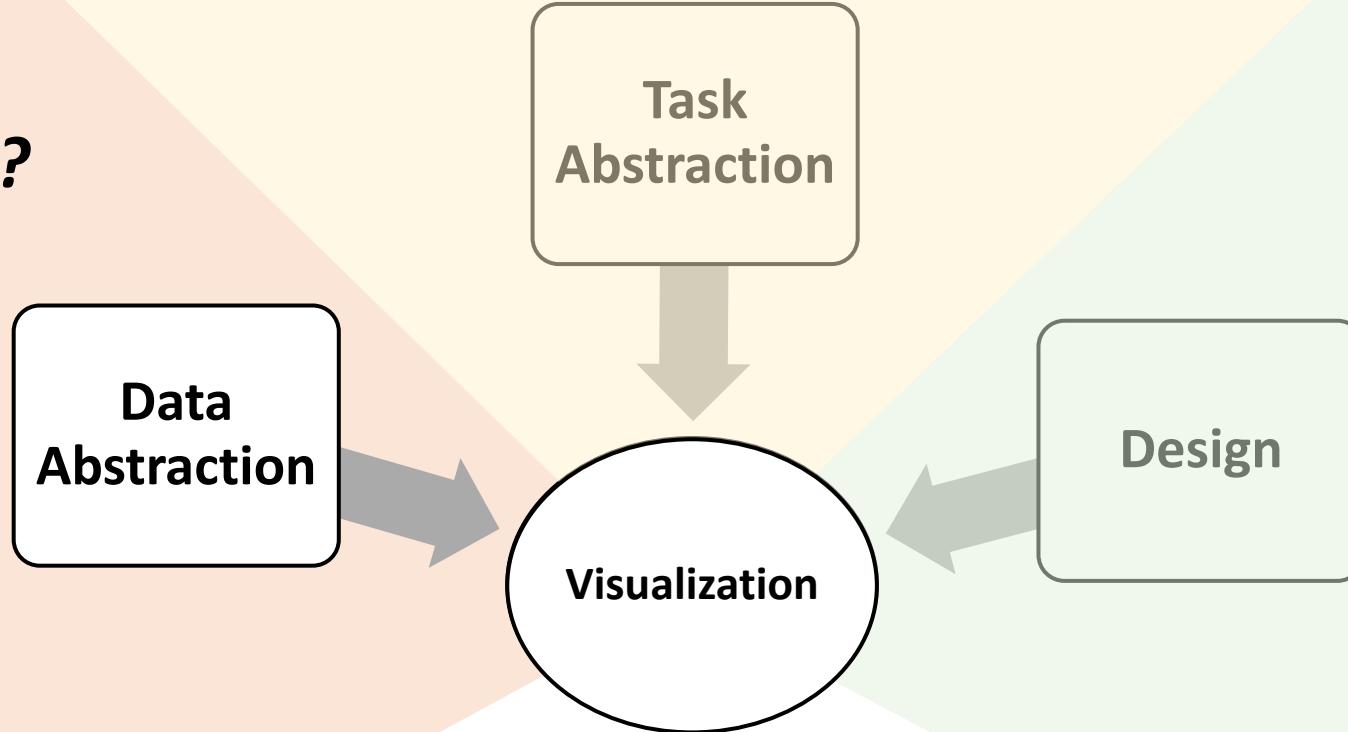
Visualization Design

Methodology to design visualizations

Why?

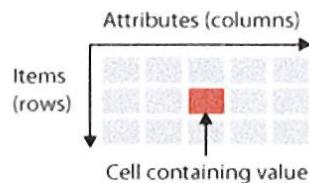
What?

How?

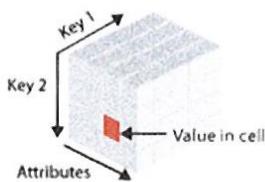


Data and Dataset Types

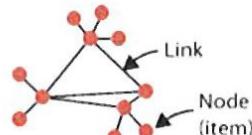
→ Tables



→ Multidimensional Table



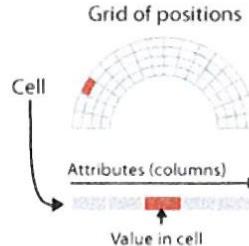
→ Networks



→ Trees



→ Fields (Continuous)



- Items
- Attributes
- Links
- Positions
- Grids

→ Geometry (Spatial)



→ Dataset Availability

→ Static

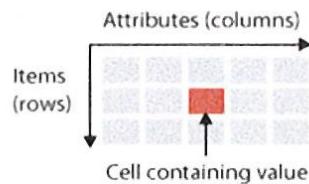


→ Dynamic

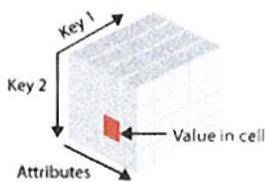


Data and Dataset Types

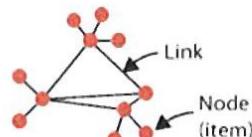
→ Tables



→ Multidimensional Table



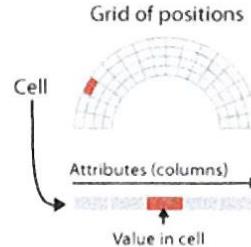
→ Networks



→ Trees



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→ Items

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→ Dataset Availability

→ Static



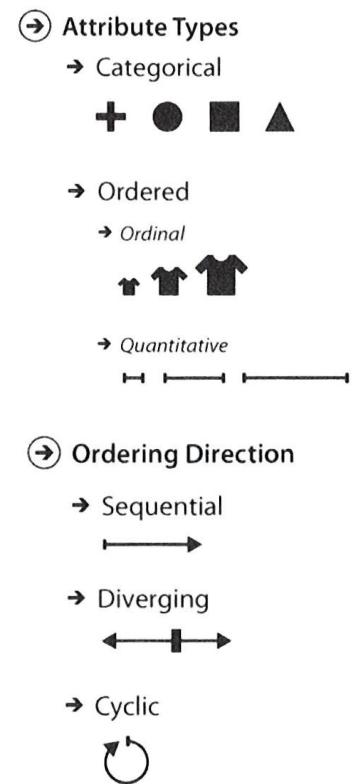
→ Dynamic



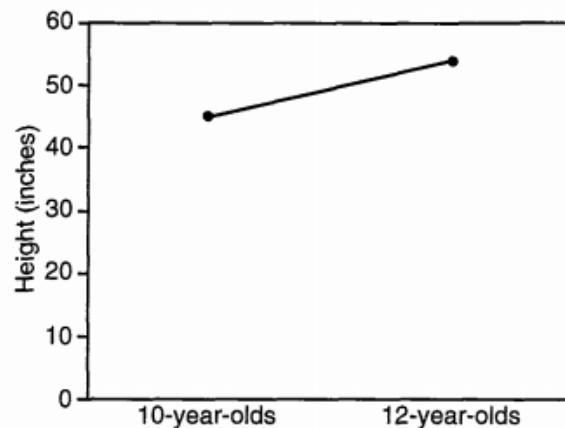
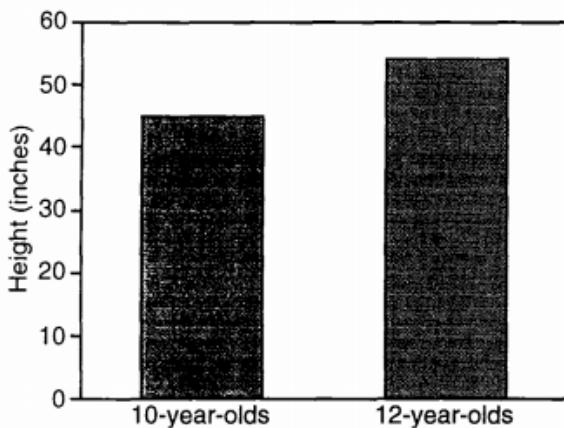
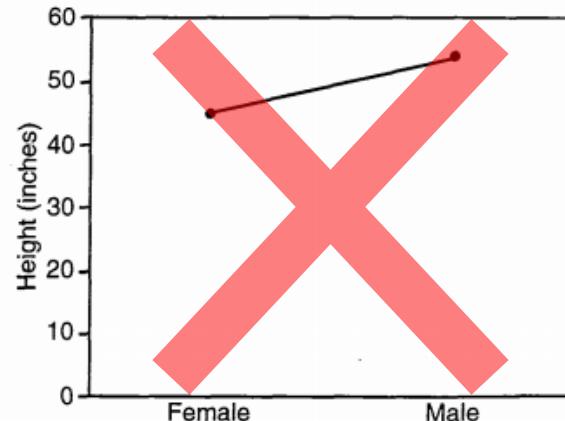
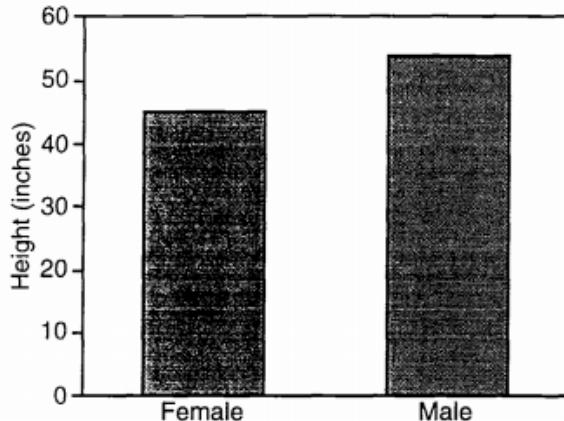
Attributes

*An **attribute** is some specific property that can be measured, observed or logged*

- ➡ • Categorical
 - Non-numerical, limited number of values, usually fixed
 - Non-ordered, unless explicitly stated
- Ordinal
 - Non-numerical, limited number of values, usually fixed
 - Ordered
- Numerical
 - Quantitative, Infinite number of values
 - Ordered

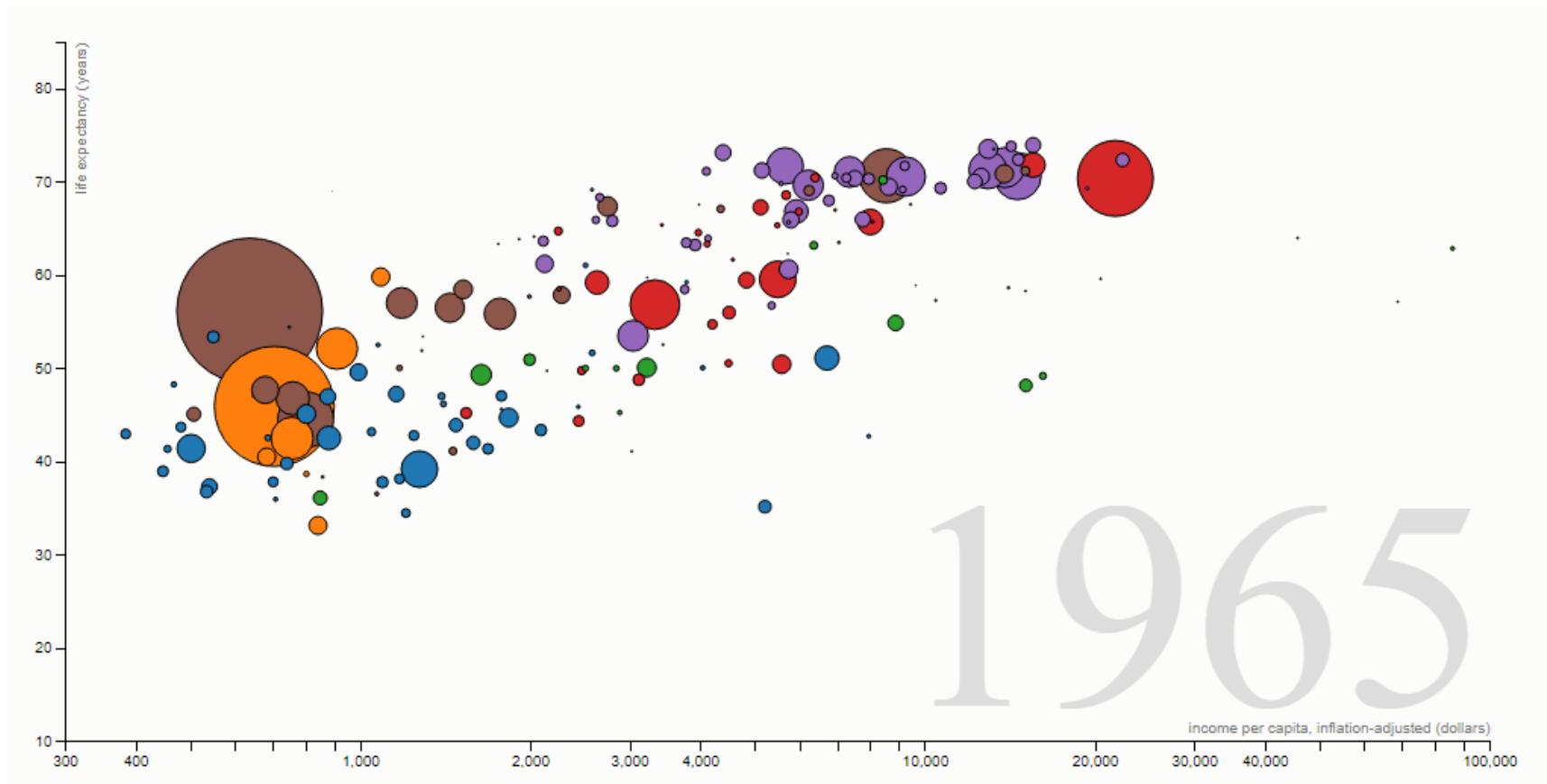


Bar Charts vs Line Charts



Zacks, Jeff, and Barbara Tversky. "Bars and lines: A study of graphic communication." *Memory and Cognition* 27 (1999): 1073-1079.

Scaterplot

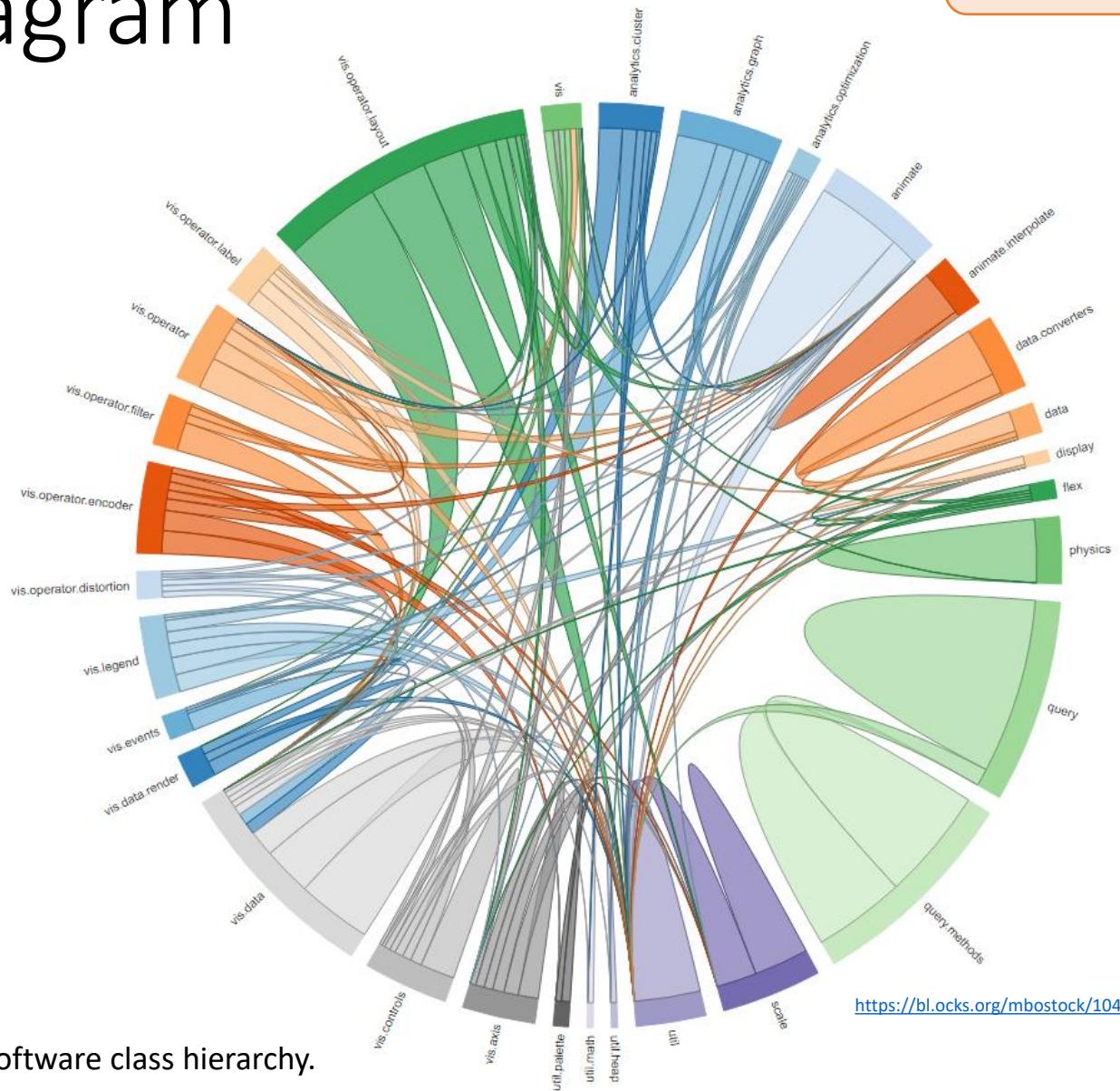


<https://bost.ocks.org/mike/nations/>

Multi dimensional table: N countries * T time
Attributes: 3 Qualitative

What?

Chord Diagram

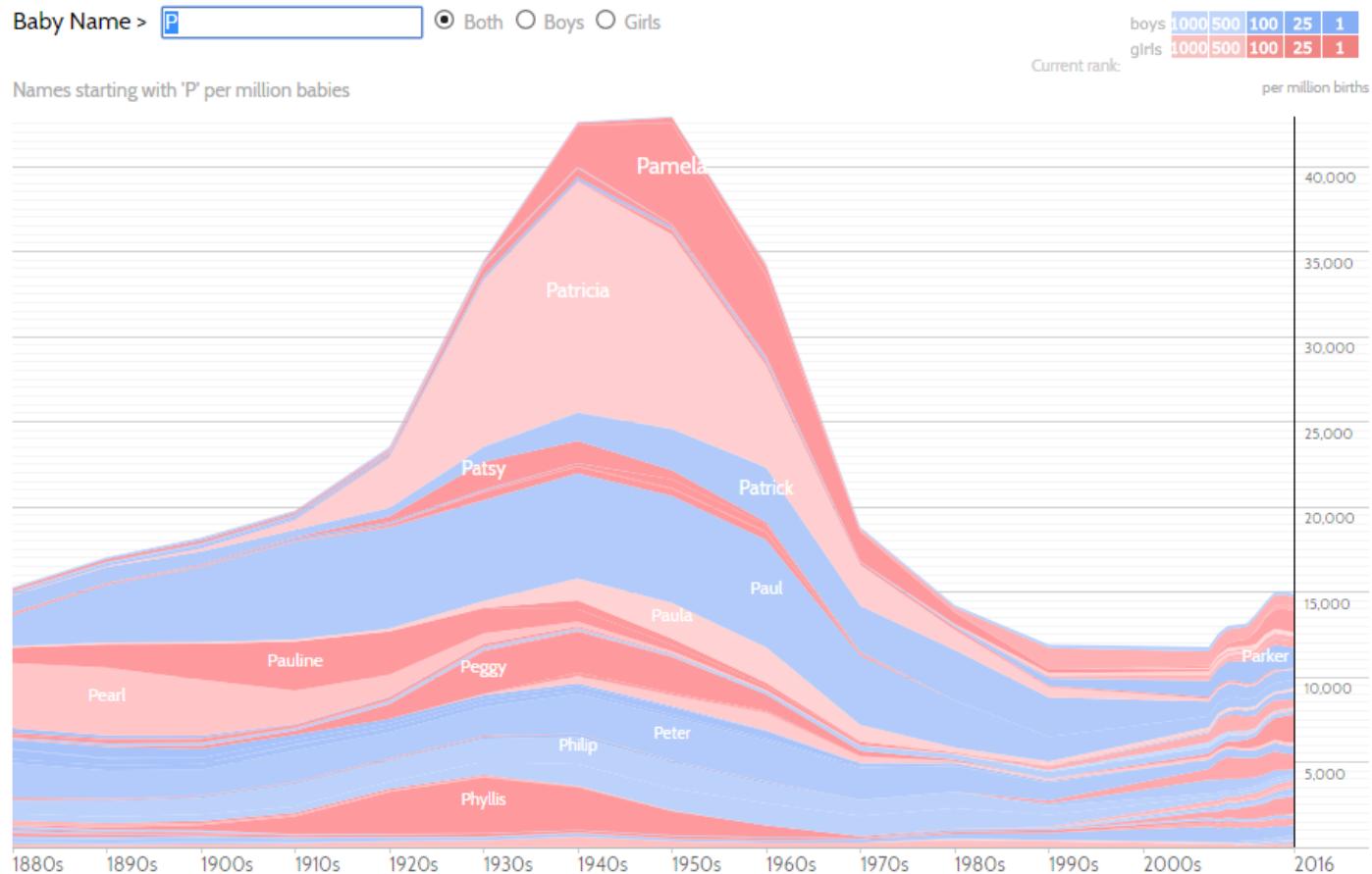


Network

Dependences between classes in a software class hierarchy.

What?

Time Varying Data



<http://www.babynamewizard.com/voyager>

Table: T time

Attributes: 1 Categorical, 1 Quantitative

What?

Tensor Visualization

Comparison: Ellipsoids vs. superquadrics (Kindlmann)

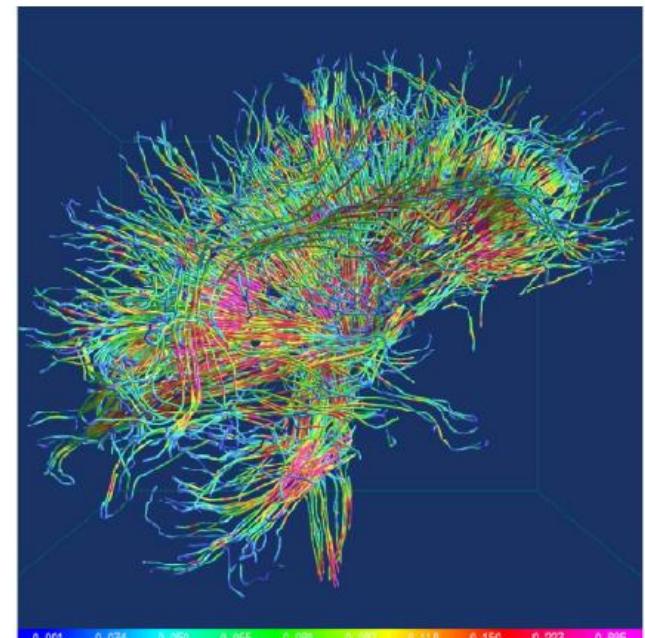
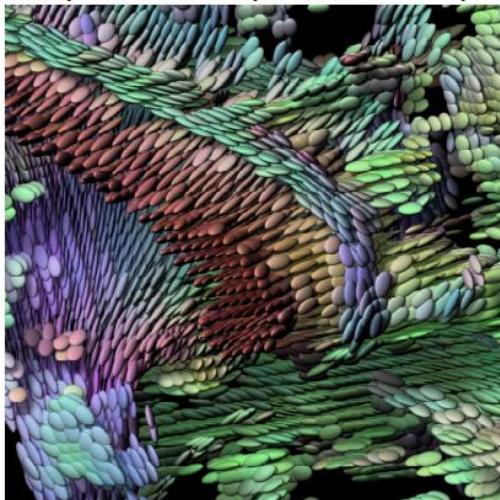
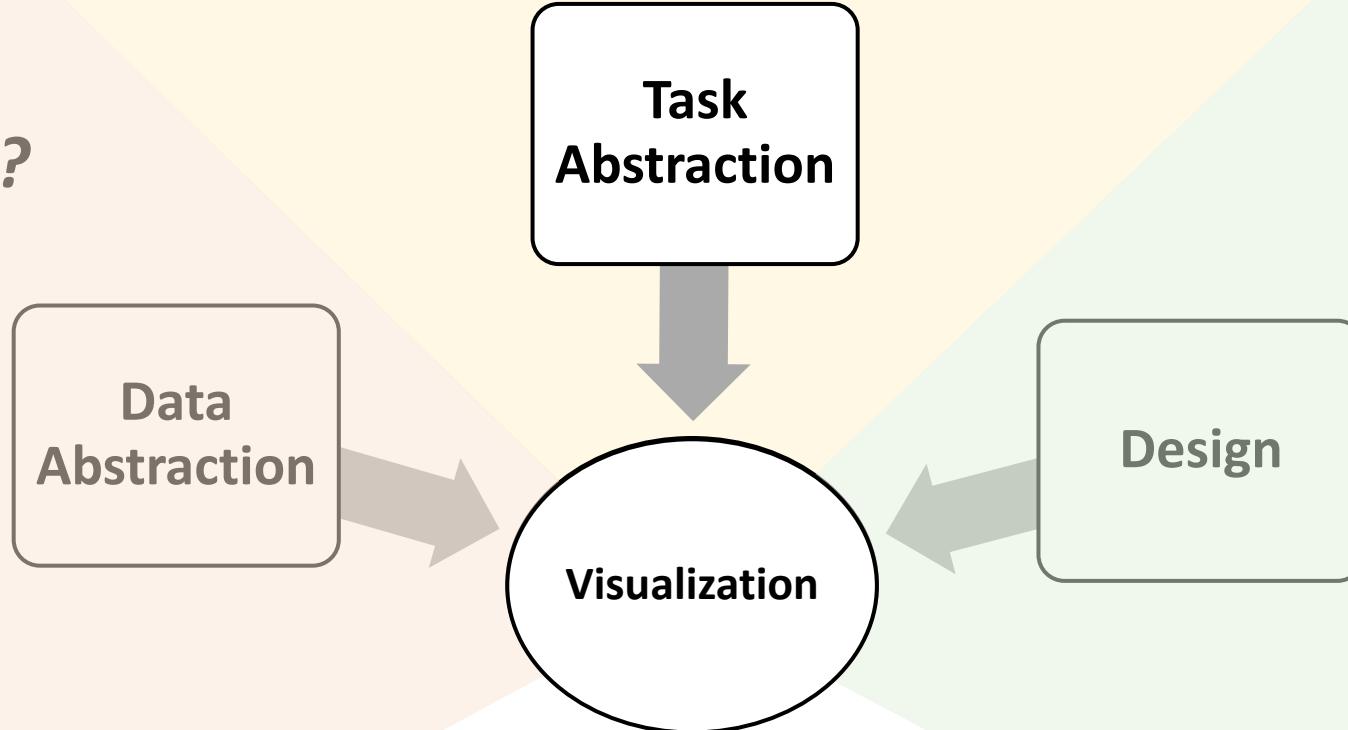


Image credit: W. Shen

Why?

What?

How?

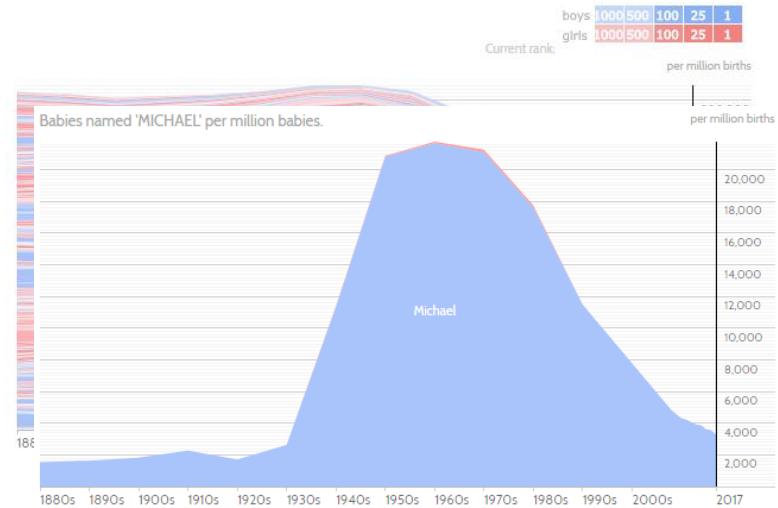
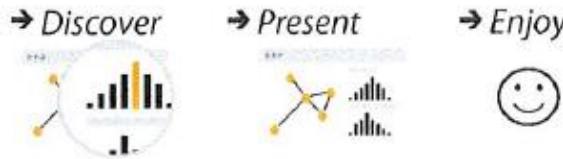


Task Abstraction

- Reframe tasks from domain-specific form into abstract form
 - Ease the design process using references
- The focus on tasks enables the improvement of them
 - Making more effective, user-friendly...
- Tasks can be classified in:
 - Actions – Verb - High-level task
 - Targets – Noun - Precise goal

Action Classification

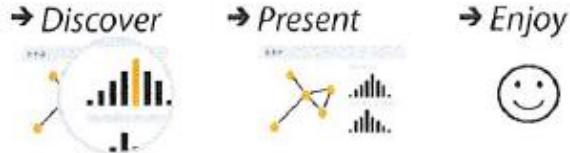
- Analyze
 - Consume



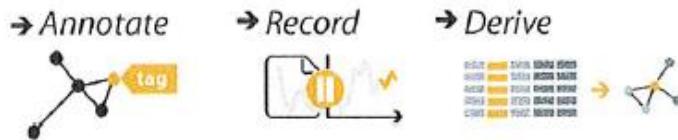
Why?

Action Classification

- Analyze
 - Consume



- Produce



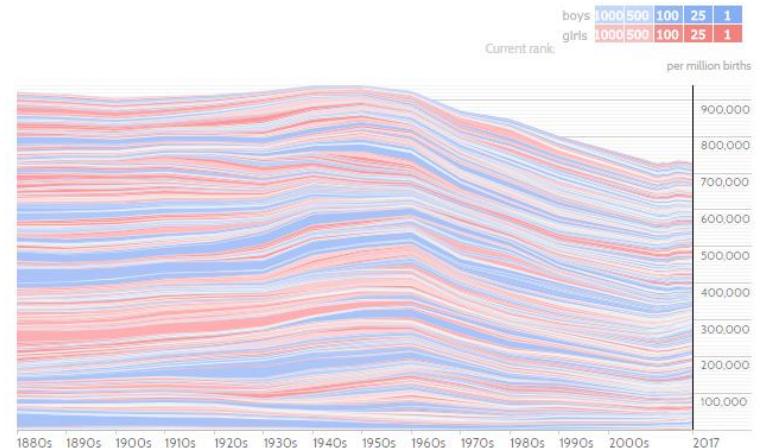
Action Classification

- Search

	Target known	Target unknown
Location known	•.. <i>Lookup</i>	•.. <i>Browse</i>
Location unknown	⟨.. ⟩ <i>Locate</i>	⟨.. ⟩ <i>Explore</i>

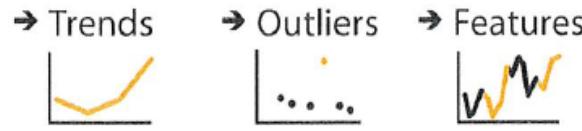
- Query

→ Identify → Compare → Summarize

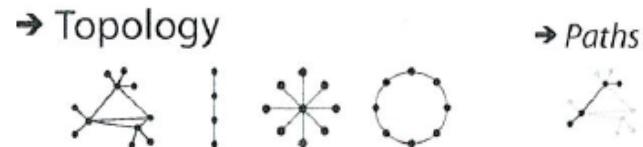


Target Classification

- All Data

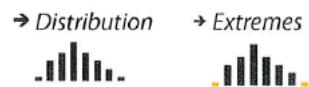


- Network Data

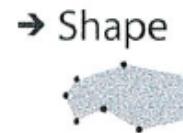


- Attributes

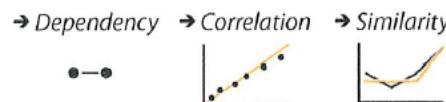
- One



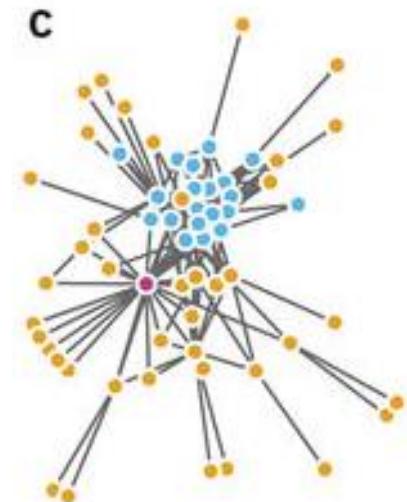
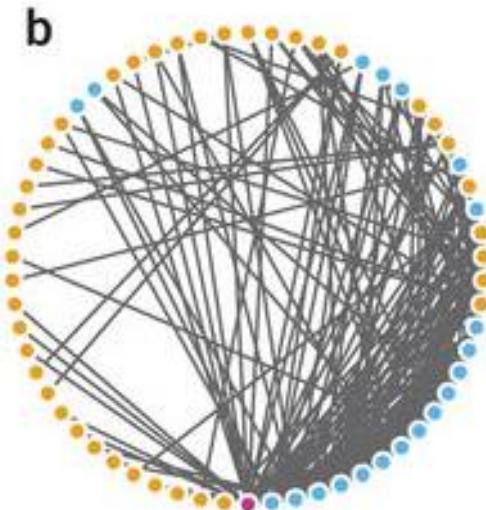
- Spatial Data



- Many



Network Visualization

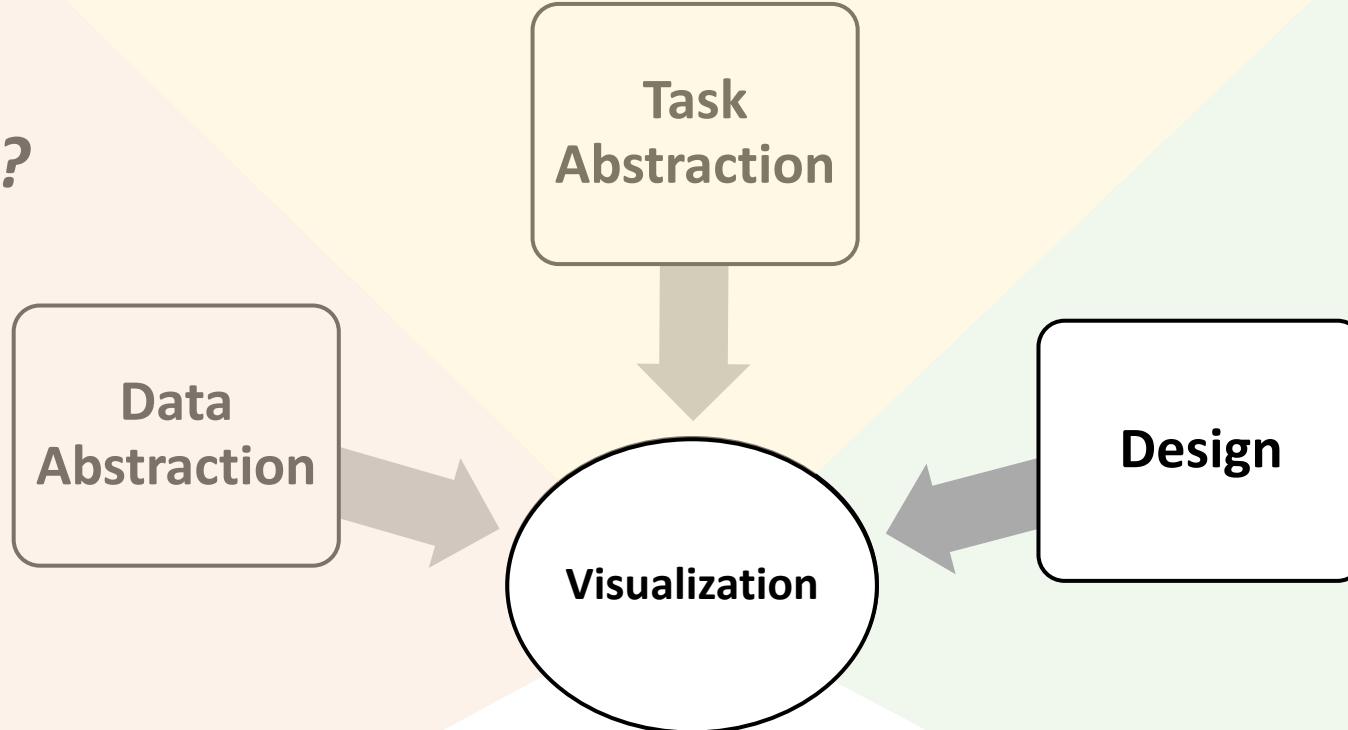


Gehlenborg, Nils, and Bang Wong. **Points of view: Networks**
Nature methods 9.2 (2012): 115-115.

Why?

What?

How?



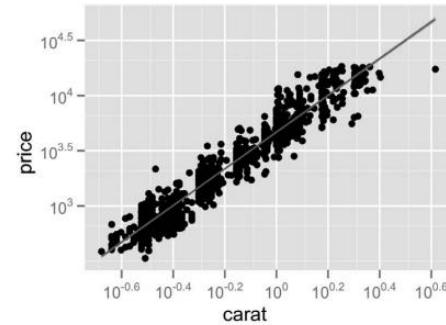
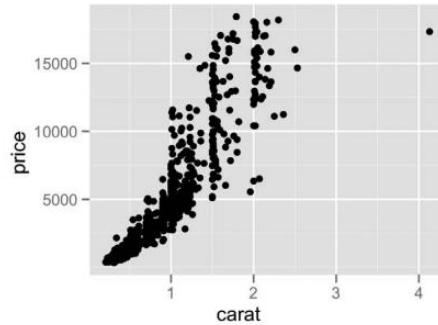
How to...

- ... **arrange** the data in the view spatially?

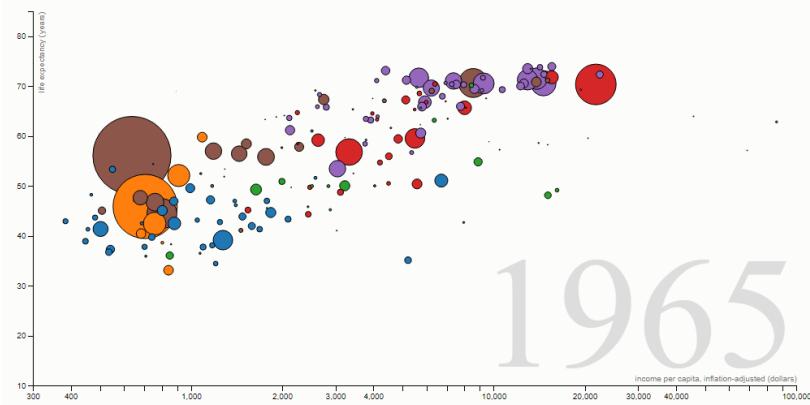
How?

Arrange / Encode

→ Express



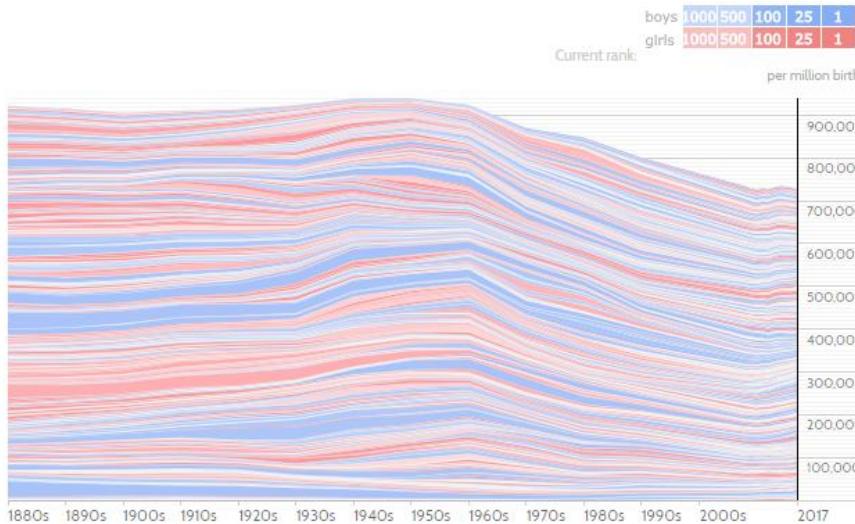
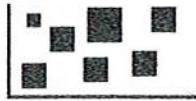
The Wealth & Health of Nations



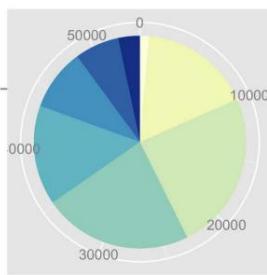
How?

Arrange / Encode

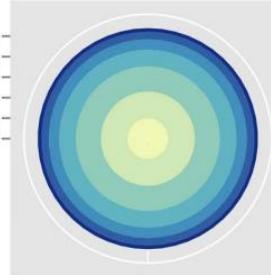
→ Separate



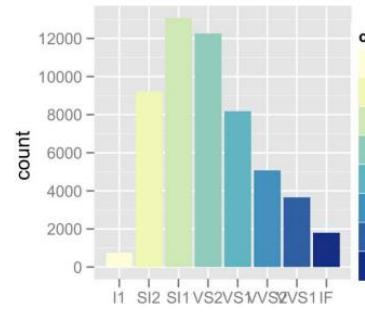
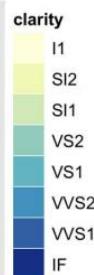
Streamgraphs



Pie Chart



Bullseye chart



Bar Plot



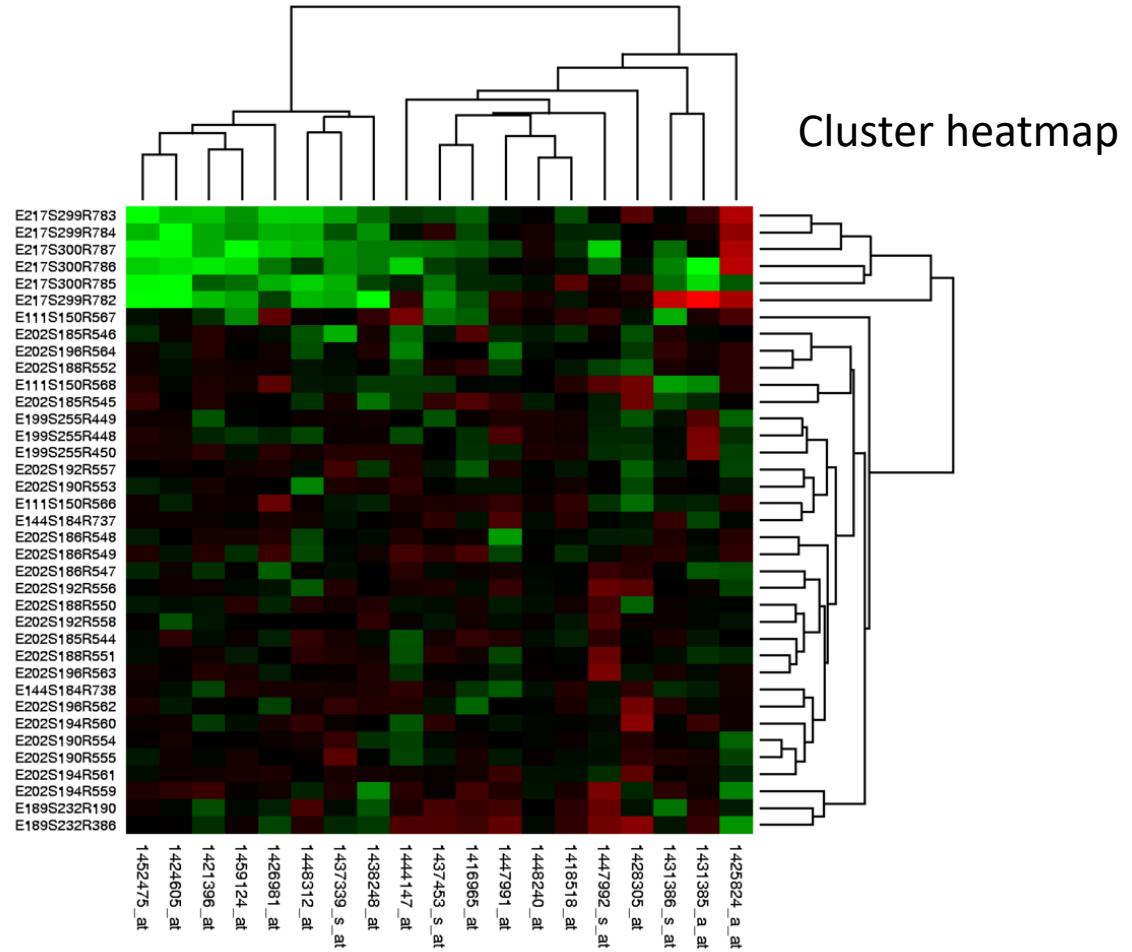
Coxcomb plot

Arrange / Encode

→ Order



→ Align



https://en.wikipedia.org/wiki/Heat_map

Arrange / Encode

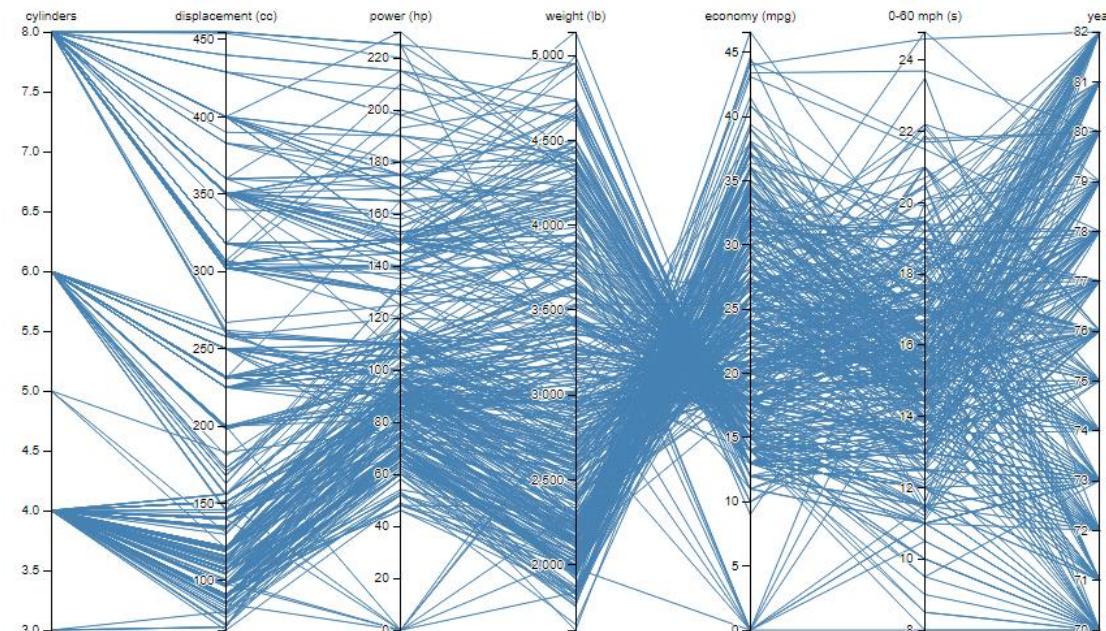
→ Order



→ Align



Parallel Coordinates



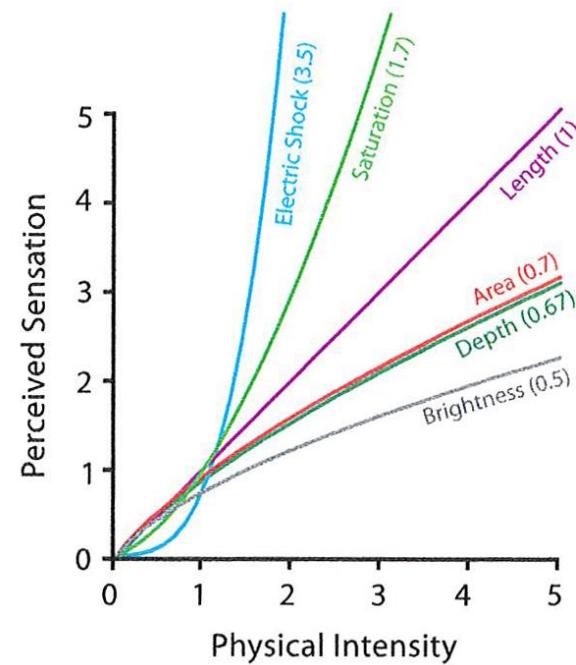
<https://bl.ocks.org/jasondavies/1341281>

How to...

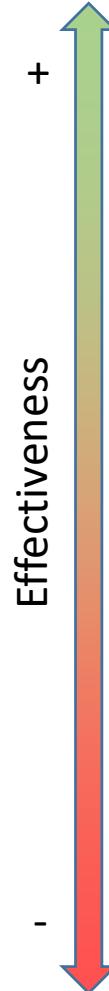
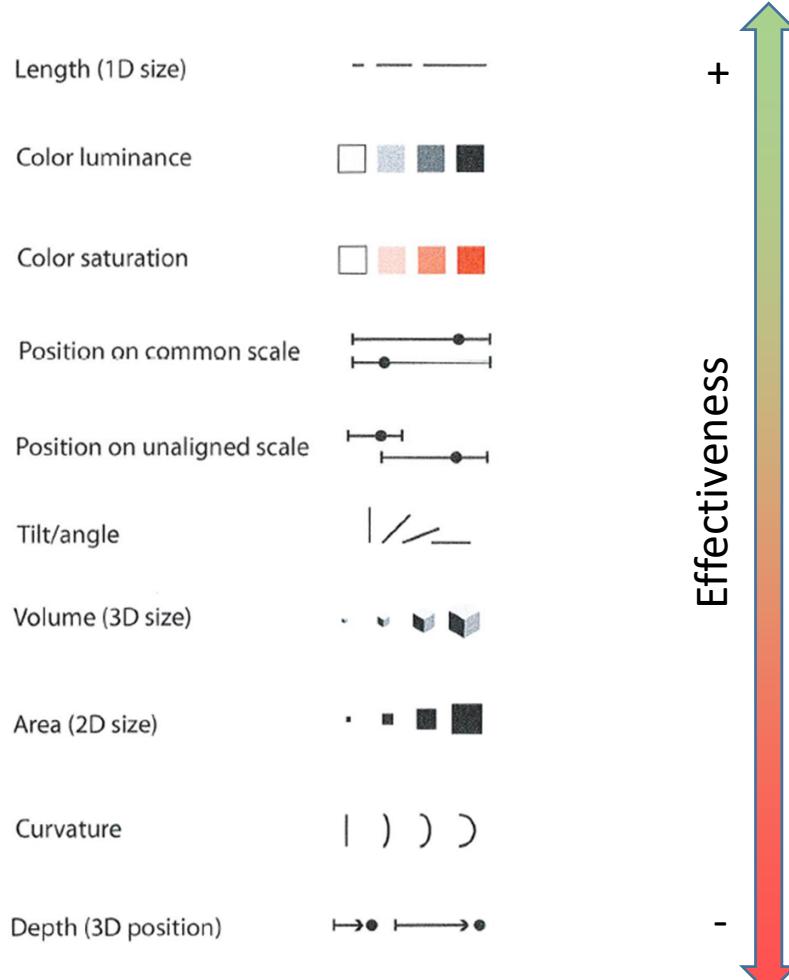
- ... **arrange** the data in the view spatially?
- ... **map** the data with all non-spatial channels?

Display

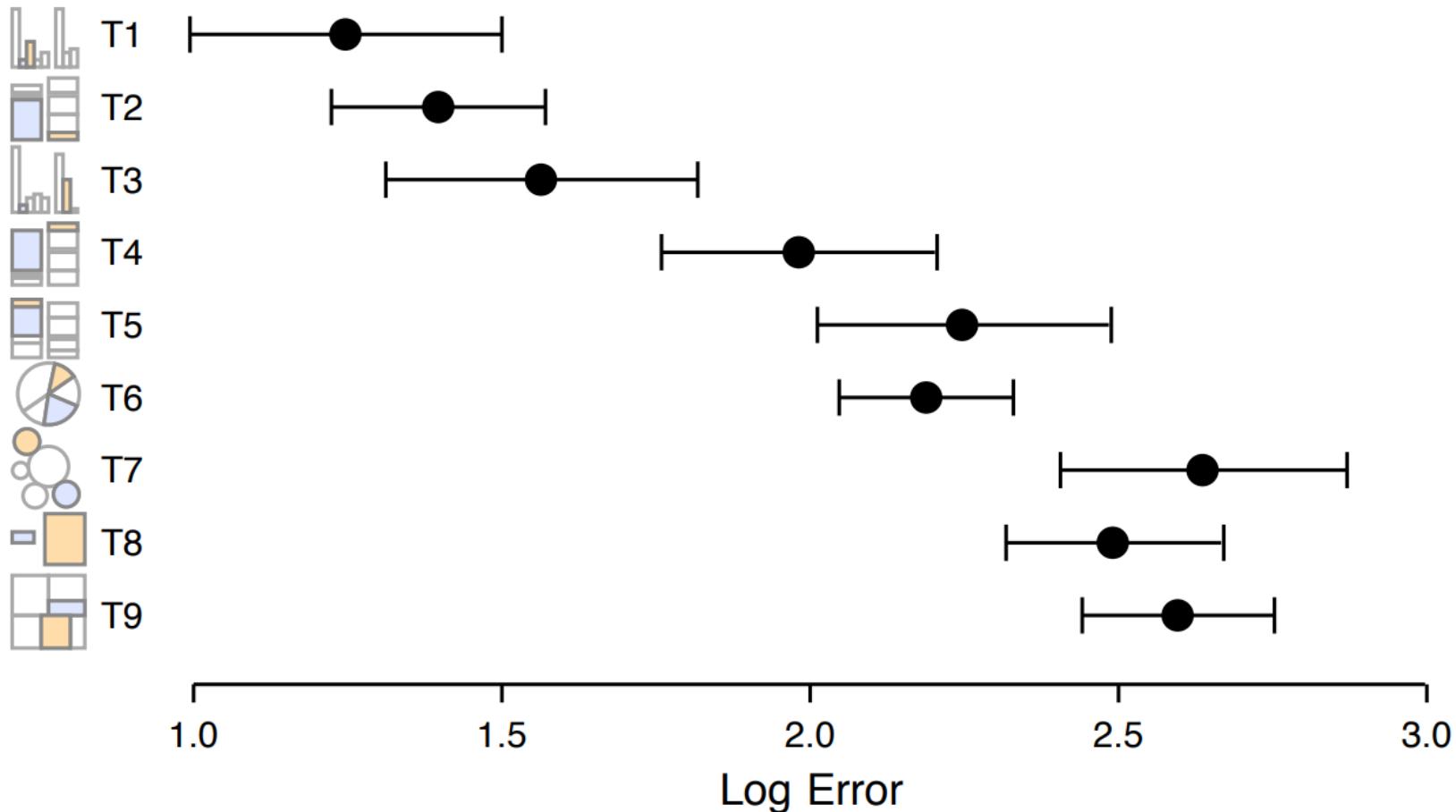
- What is the best way to visually encode the data ?
 - How the human visual system discriminate visual stimuli?
- Two major dimensions
 - Color
 - Shape

Steven's Psychophysical Power Law: $S = I^N$ 

Visual Encoding



Visual discrimination



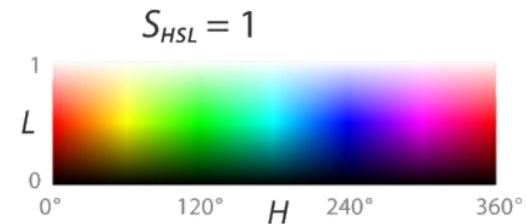
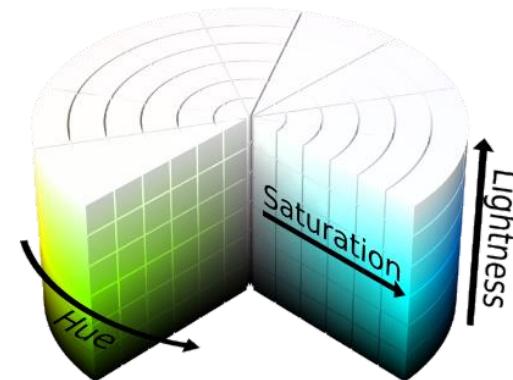
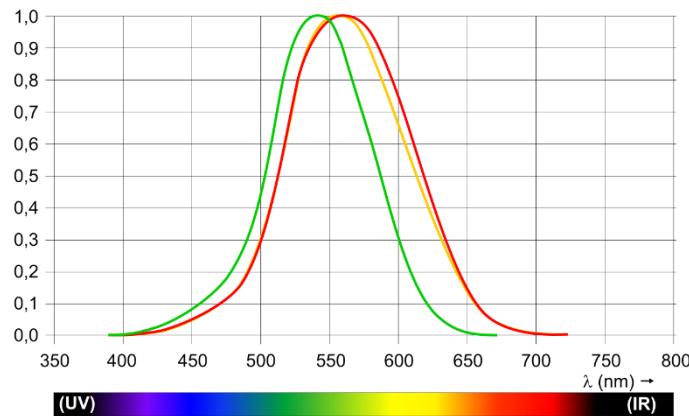
Crowdsourcing graphical perception: using mechanical turk to assess visualization design. Jeffrey Heer and Michael Bostock. 2010. ACM SIGCHI Conference on Human Factors in Computing Systems, p. 203-212

Color Encoding

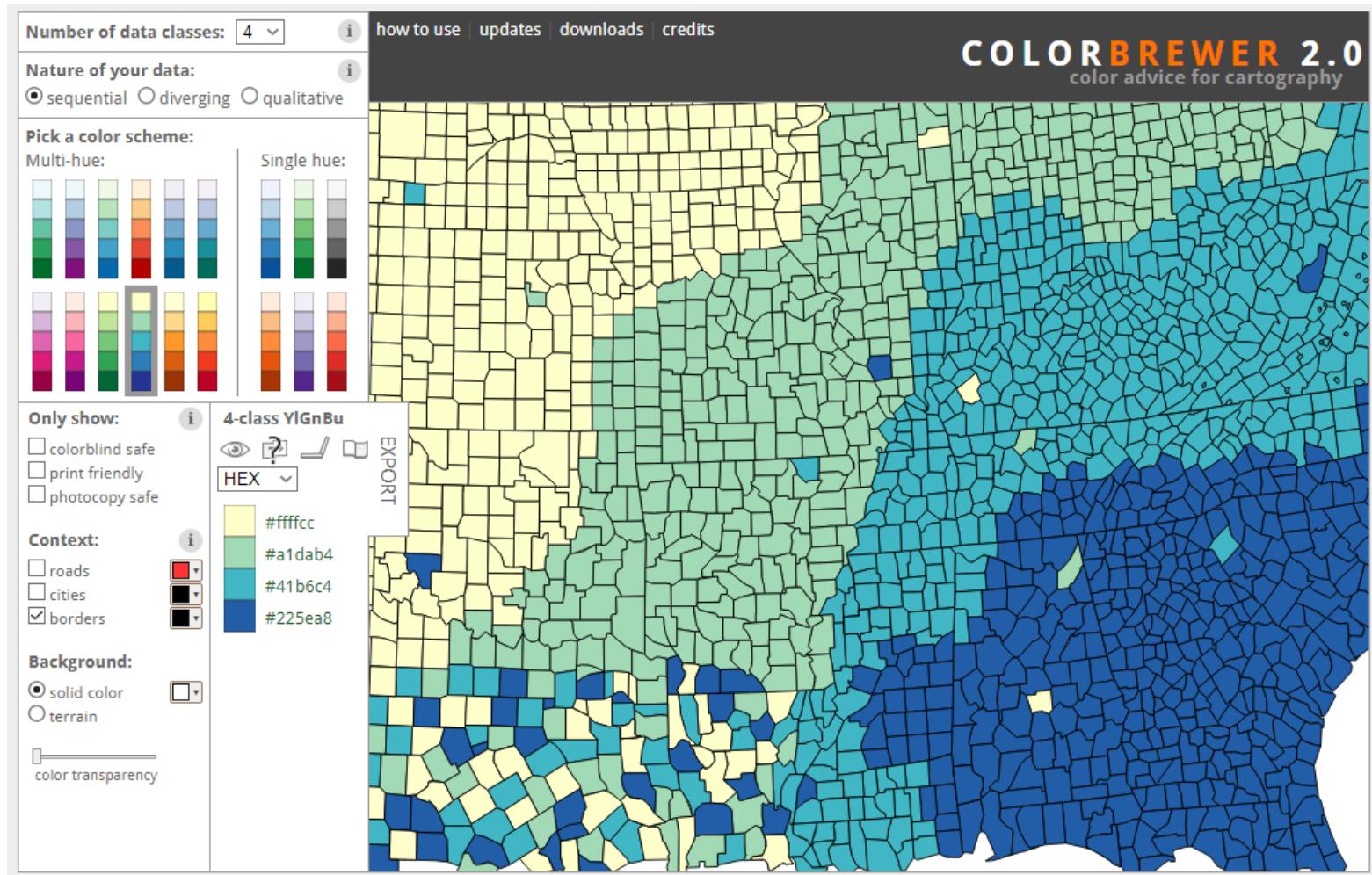
- Color Components



- Color sensitivity



Color Encoding



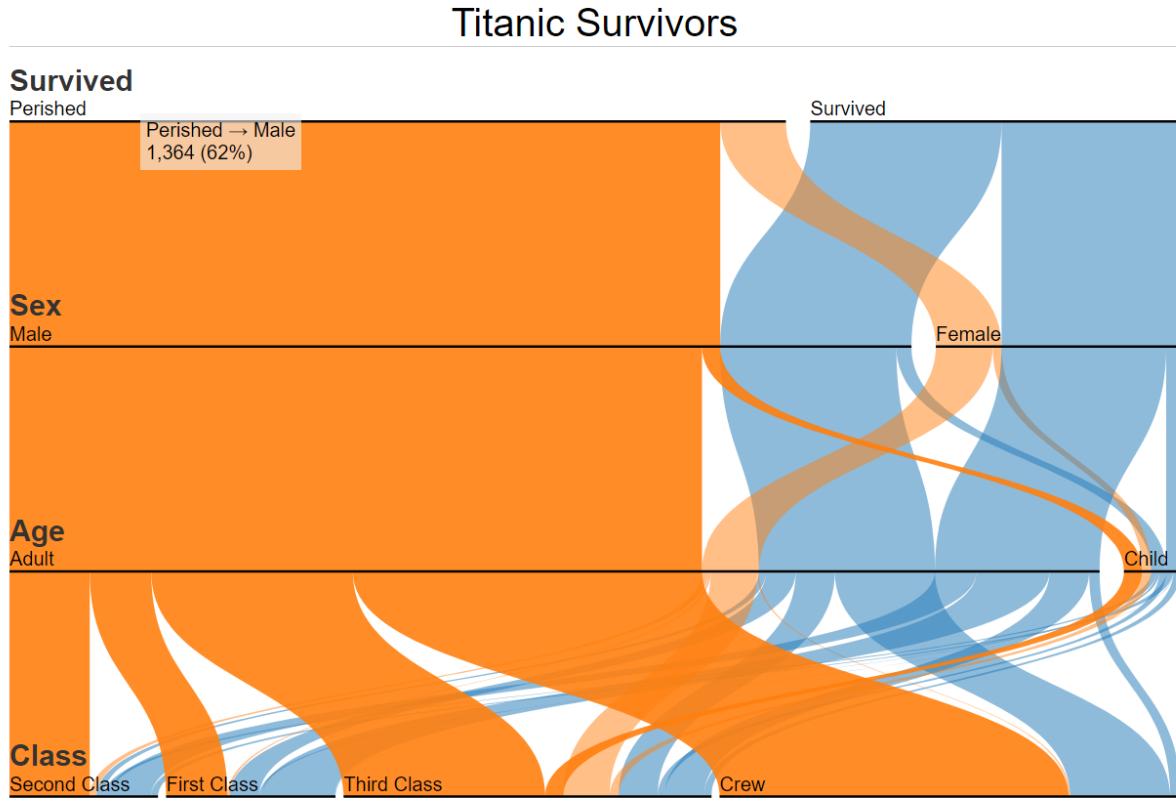
<http://colorbrewer2.org/>

Color Use Guidelines for Data Representation, Brewer, C. A. 1999. Proceedings of the Section on Statistical Graphics, American Statistical Association, Alexandria VA. pp. 55-60.

How to...

- ... **arrange** the data in the view spatially?
- ... **map** the data with all non-spatial channels?
- ... **manipulate** the data in the view?

Manipulate



→ Change



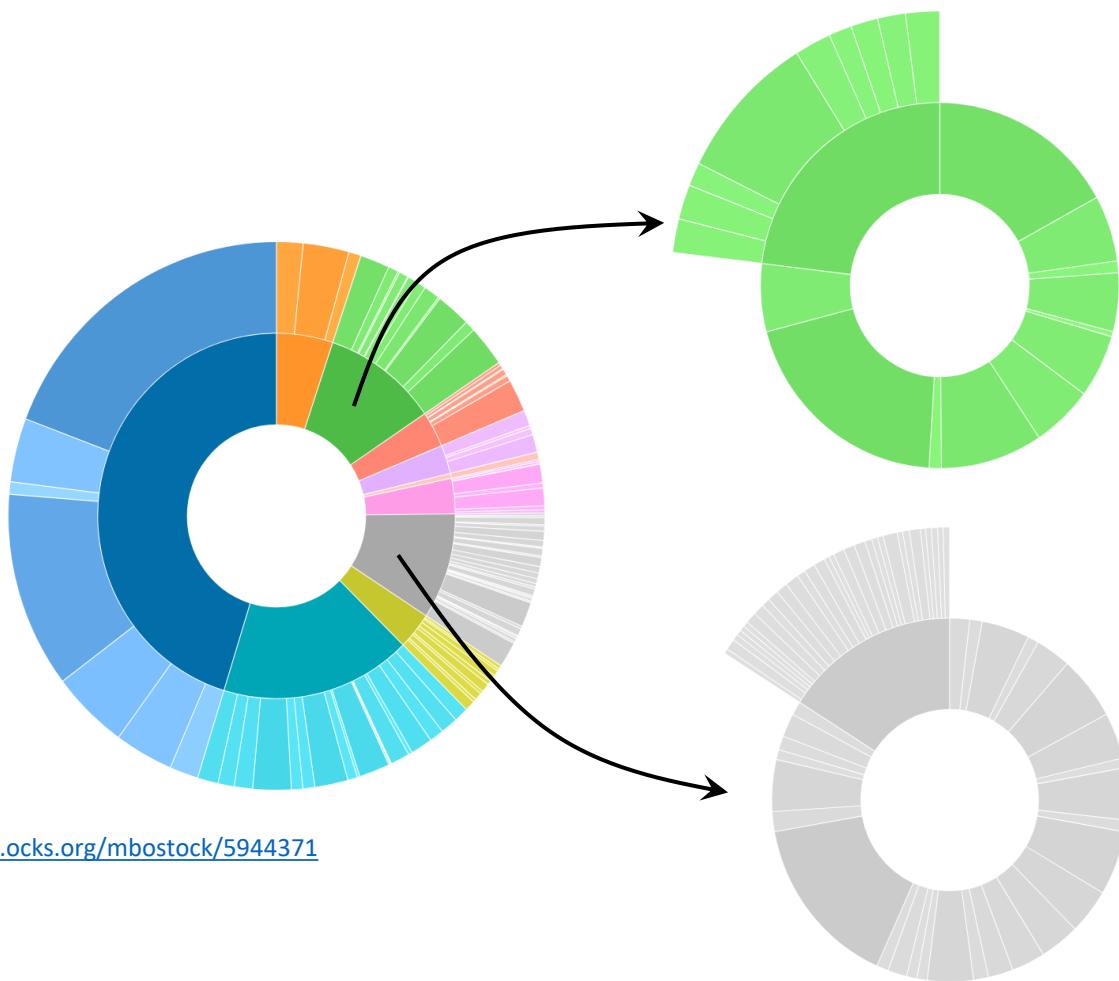
→ Select



→ Navigate



Manipulate



<https://bl.ocks.org/mbostock/5944371>

→ Change



→ Select



→ Navigate

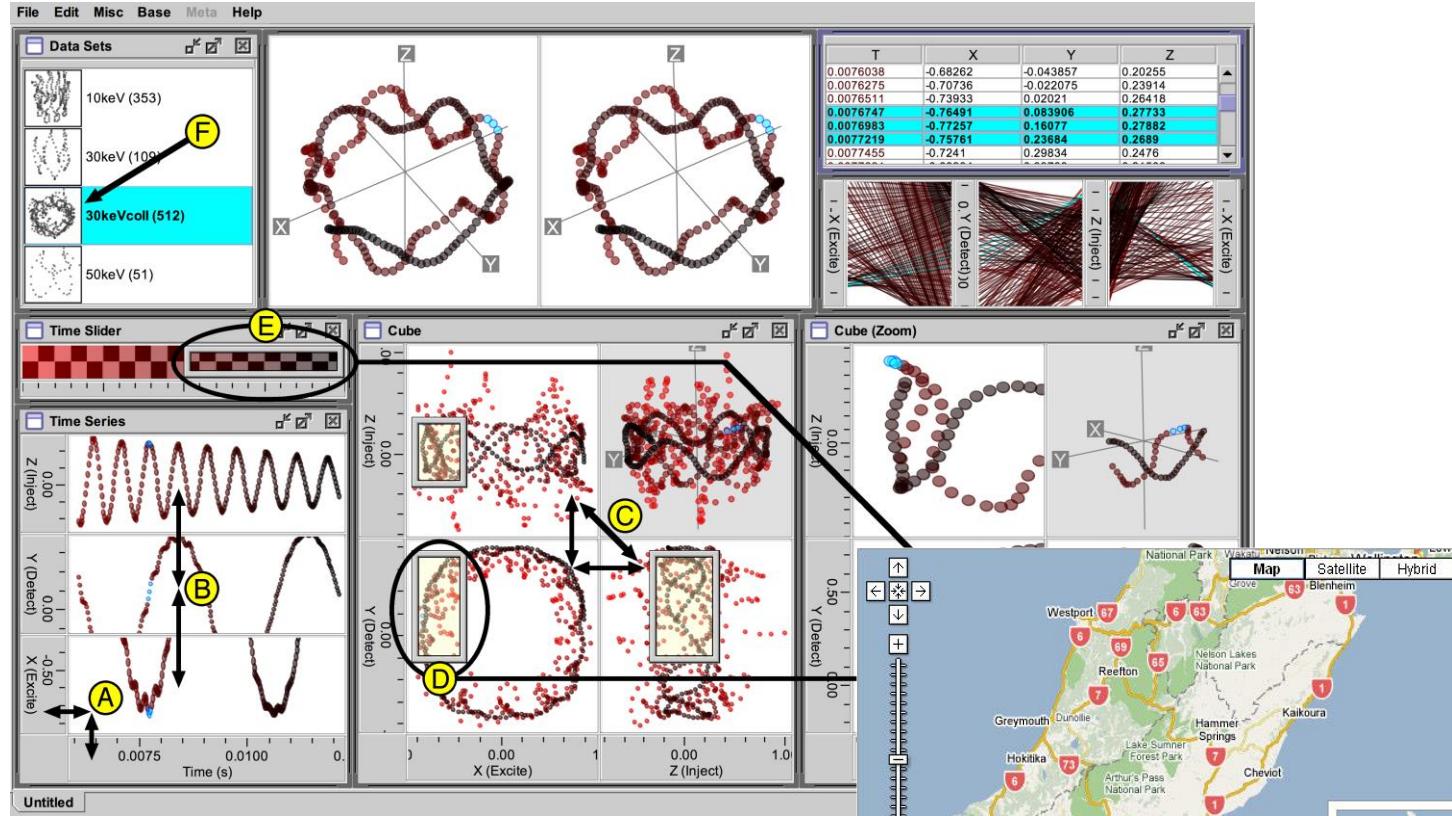


How to...

- ... **arrange** the data in the view spatially?
- ... **map** the data with all non-spatial channels?
- ... **manipulate** the data in the view?
- ... **facet** data between views?

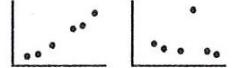
How?

Facet (multi-view)

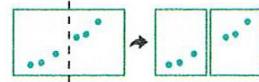


Weaver. Building Highly-Coordinated Visualizations In Improvise.
Proc. InfoVis 2004, p. 159-166

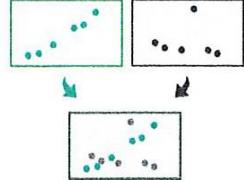
→ Juxtapose



→ Partition

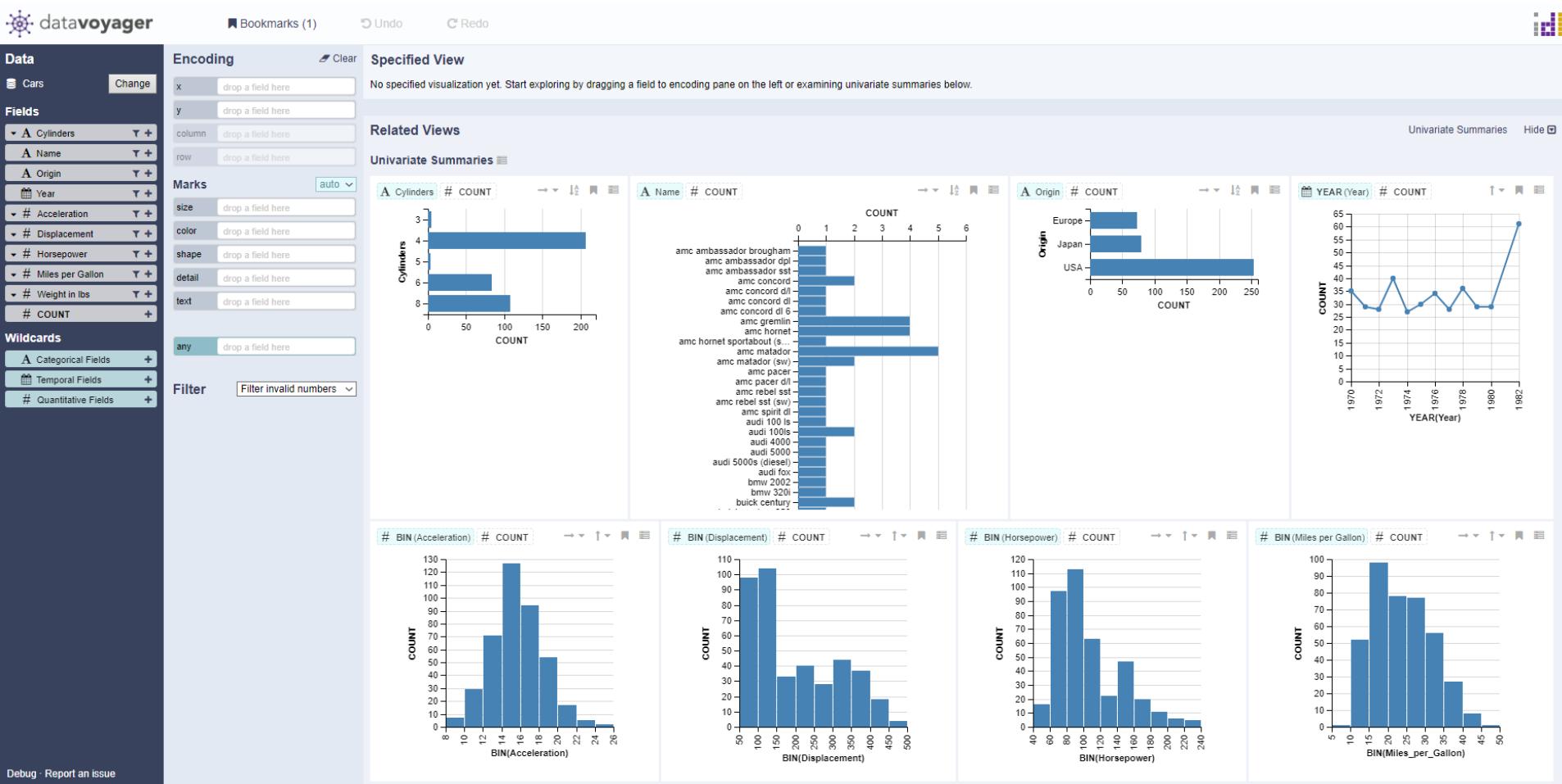


→ Superimpose



Overview + Detail

Facet (multi-view)



<https://vega.github.io/voyager2/>

How to...

- ... **arrange** the data in the view spatially?
- ... **map** the data with all non-spatial channels?
- ... **manipulate** the data in the view?
- ... **facet** data between views?
- ... **reduce** the data in the view?

Reduce

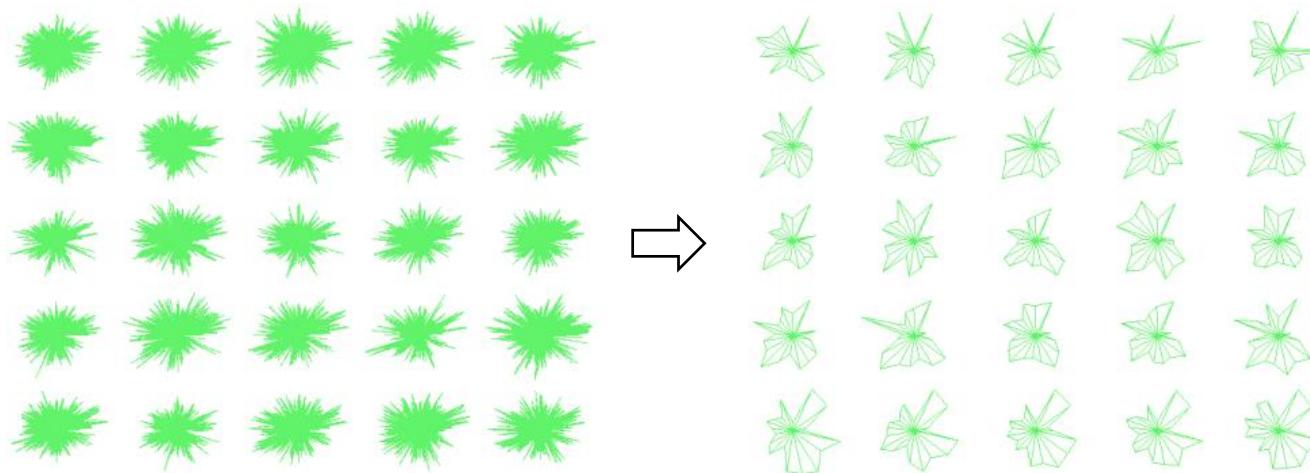
→ Filter



→ Aggregate

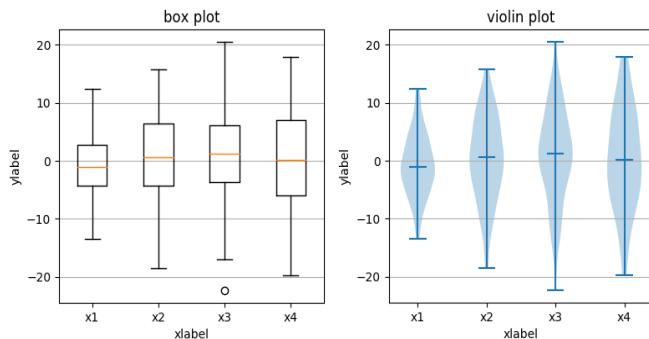


→ Embed

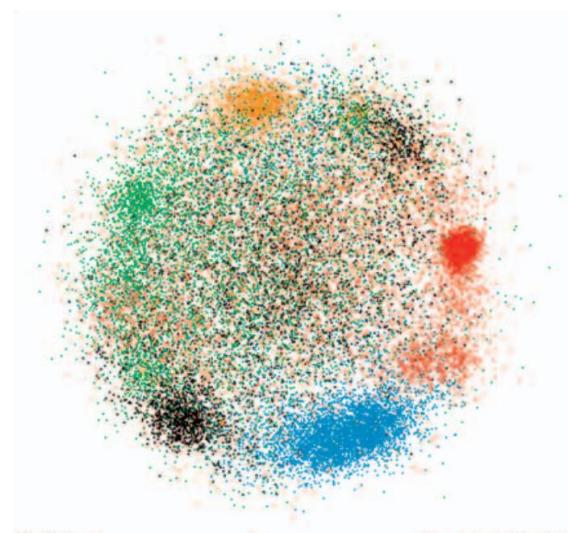


Yang, Jing, et al. "Interactive hierarchical dimension ordering, spacing and filtering for exploration of high dimensional datasets." *IEEE Symposium on Information Visualization*, 2003

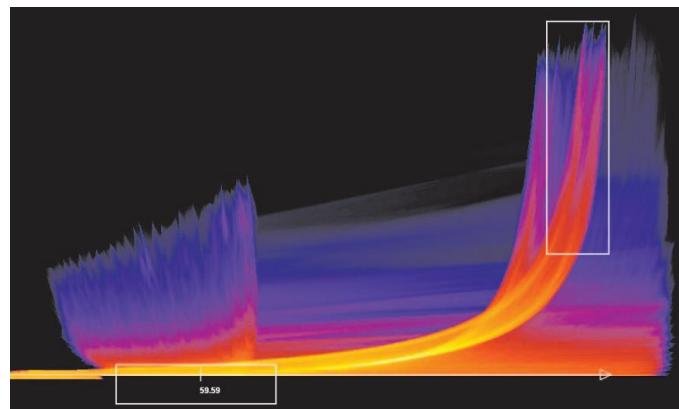
Reduce



<https://matplotlib.org/gallery.html>



S. Ingram, T. Munzner and M. Olano, "Glimmer: Multilevel MDS on the GPU," in *IEEE Transactions on Visualization and Computer Graphics*, vol. 15, no. 2, pp. 249-261, 2009.



S. Bachthaler and D. Weiskopf, "Continuous Scatterplots," in *IEEE Transactions on Visualization and Computer Graphics*, vol. 14, no. 6, pp. 1428-1435, 2008.

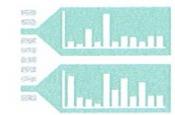
→ Filter



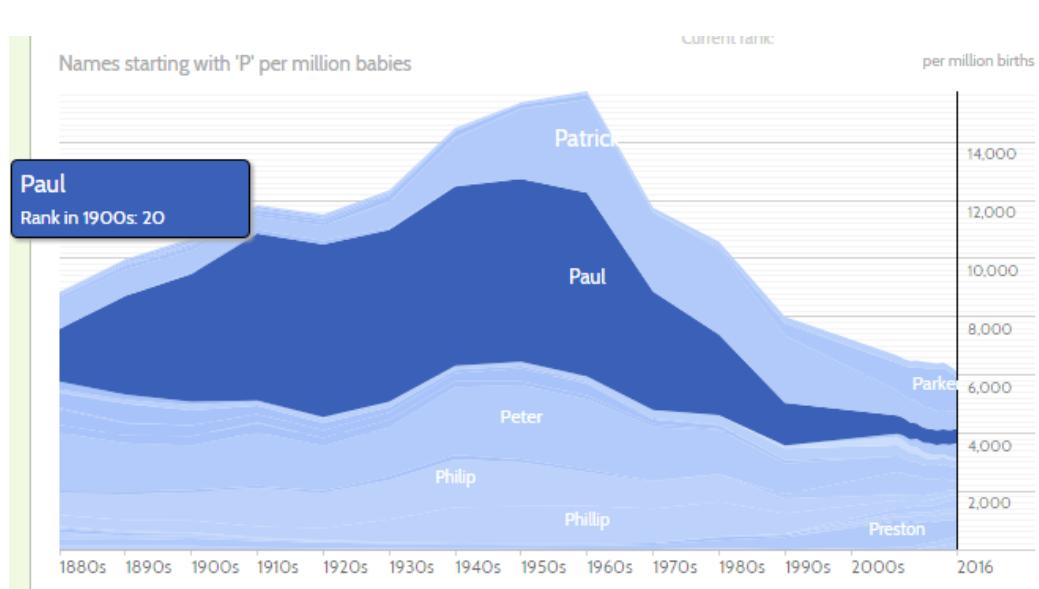
→ Aggregate



→ Embed



Reduce



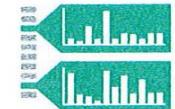
→ Filter



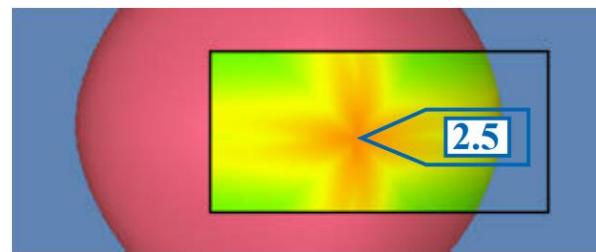
→ Aggregate



→ Embed

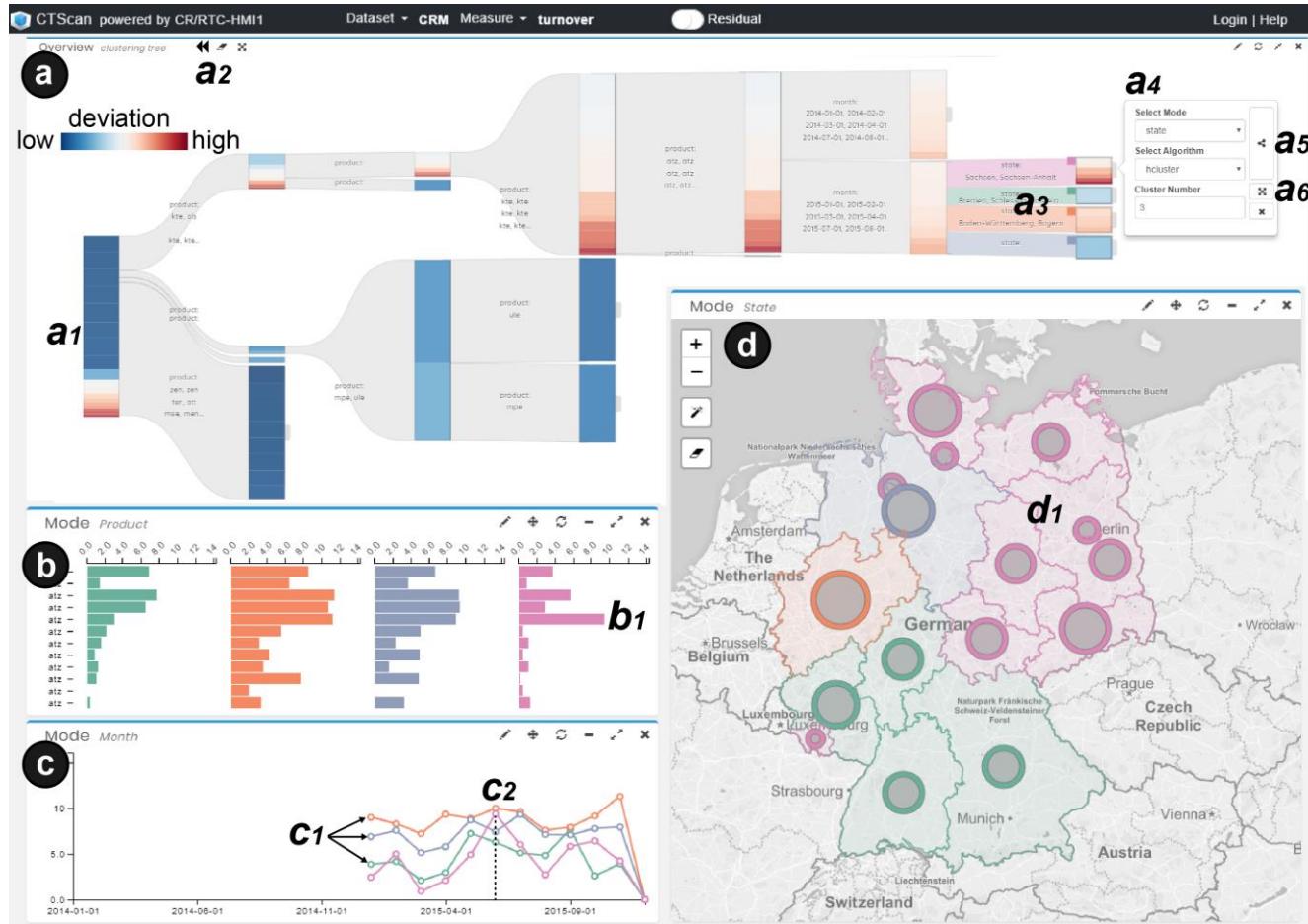


<http://www.babynamewizard.com/voyager>



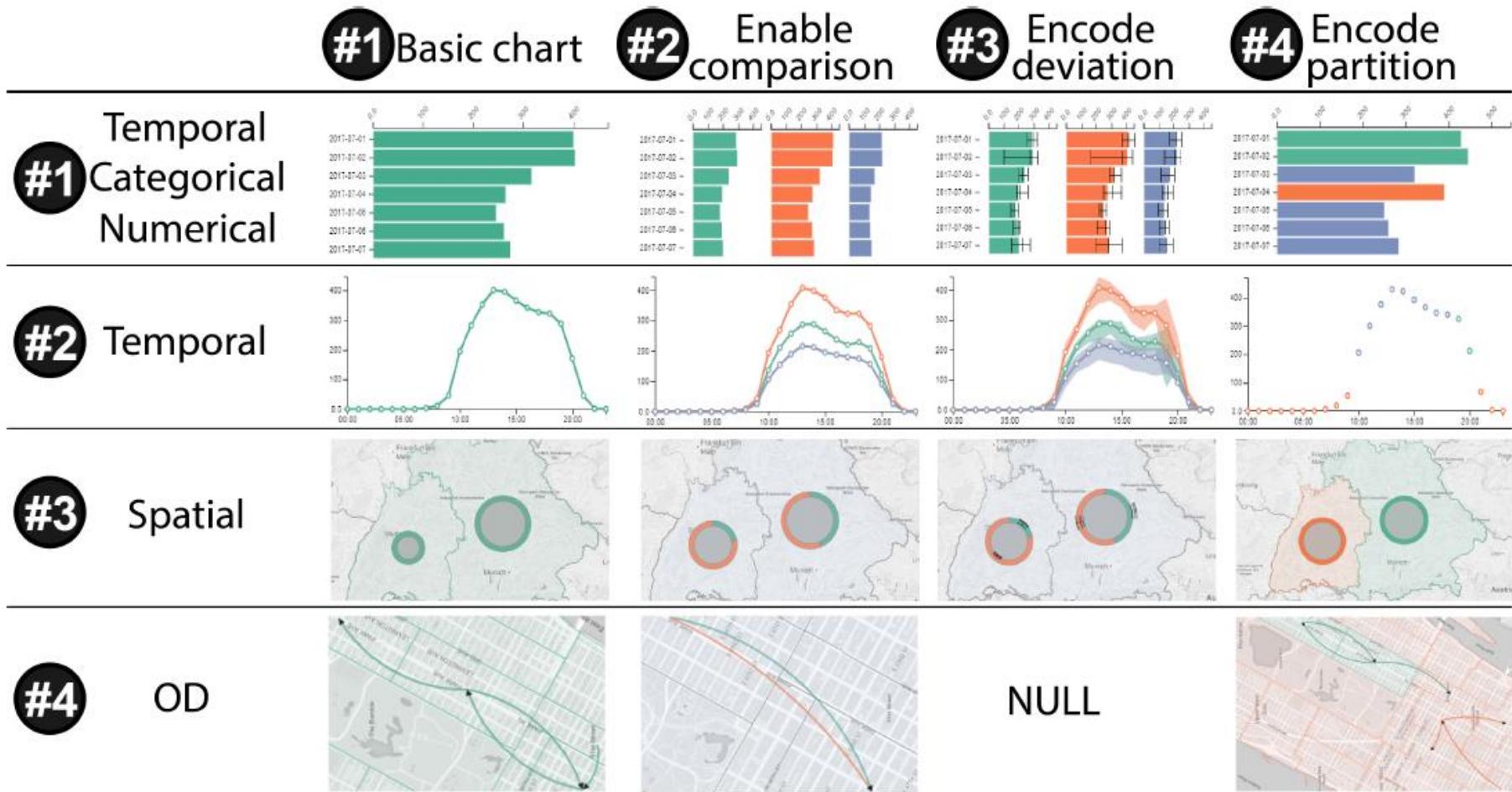
Eric A. Bier, Maureen C. Stone, Ken Pier, William Buxton, and Tony D. DeRose. 1993. **Toolglass and magic lenses: the see-through interface.** ACM SIGGRAPH '93

Example: Progressive Partition and Multidimensional Pattern Extraction for Large-Scale Spatio-Temporal Data Analysis

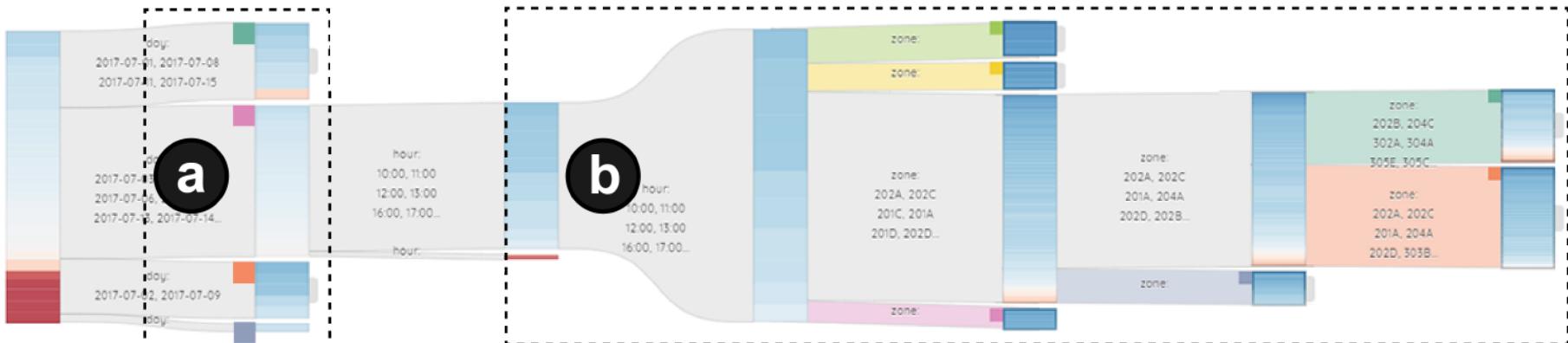
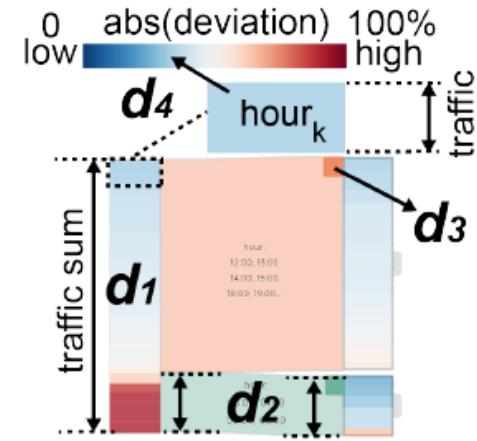
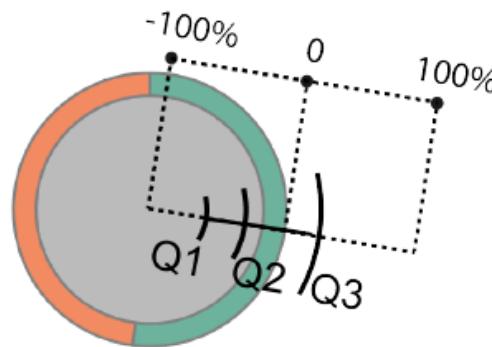
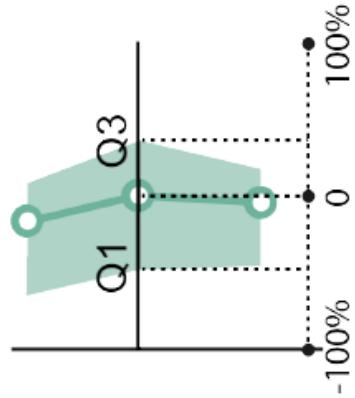
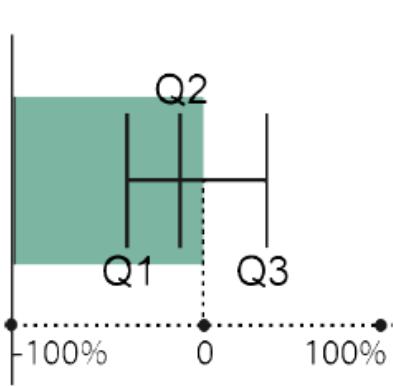


Liu, Dongyu, Panpan Xu, and Liu Ren. "TPFlow: Progressive partition and multidimensional pattern extraction for large-scale spatio-temporal data analysis." IEEE transactions on visualization and computer graphics 25.1 (2018): 1-11.

Pattern Comparison



Data Encoding



TPFlow: Progressive Partition and Multidimensional Pattern Extraction for Large-Scale Spatio-Temporal Data Analysis

IEEE VAST 2018 - Conference on Visual Analytics Science and Technology
(TVCG Track*)

Dongyu Liu

Hong Kong University of
Science and Technology, Hong Kong

Panpan Xu Liu Ren

Bosch Research North America
Sunnyvale, CA

(With Audio)

*Paper selected to IEEE Transactions on Visualization and Computer Graphics (TVCG)

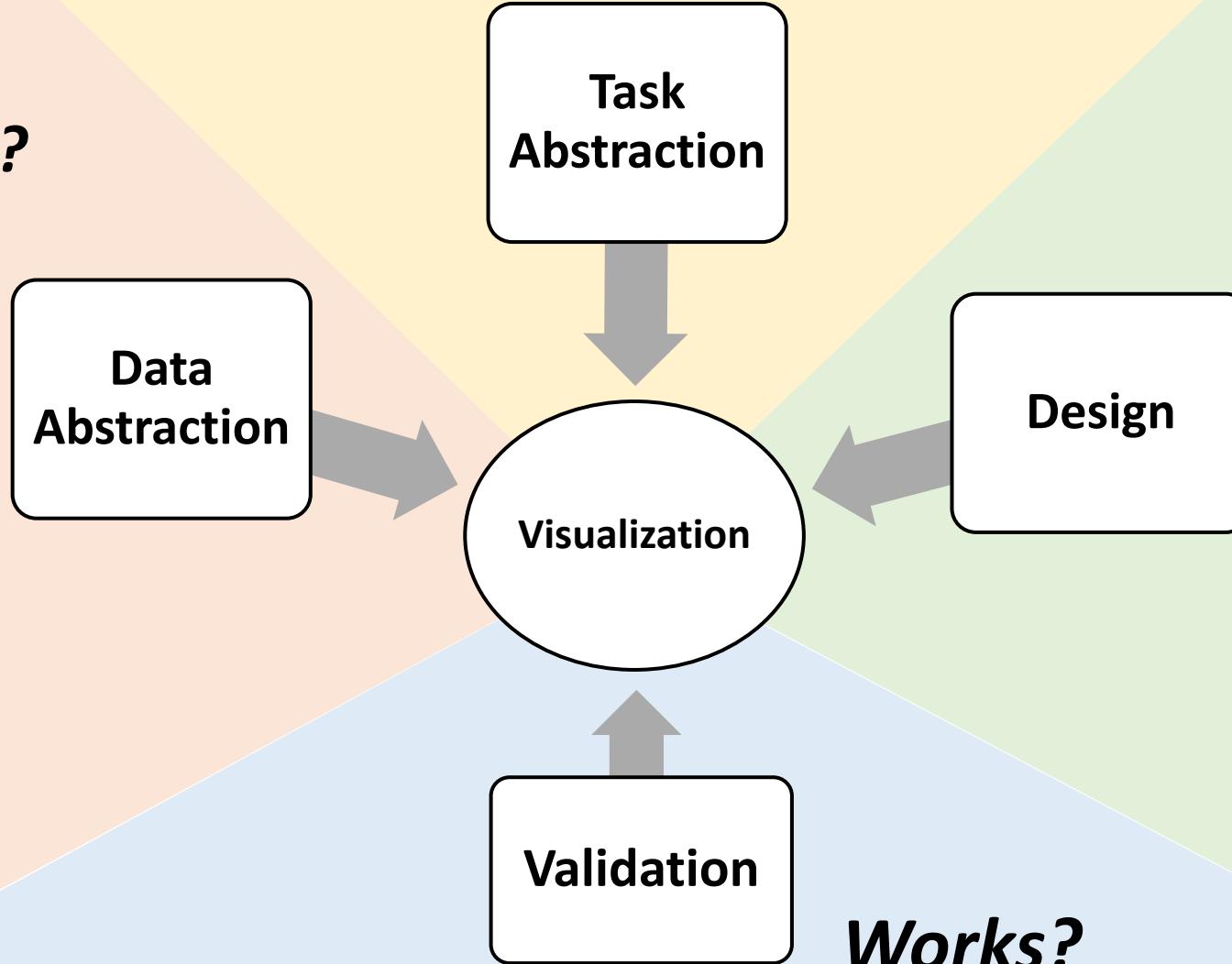


BOSCH
Invented for life

Why?

What?

How?



Works?

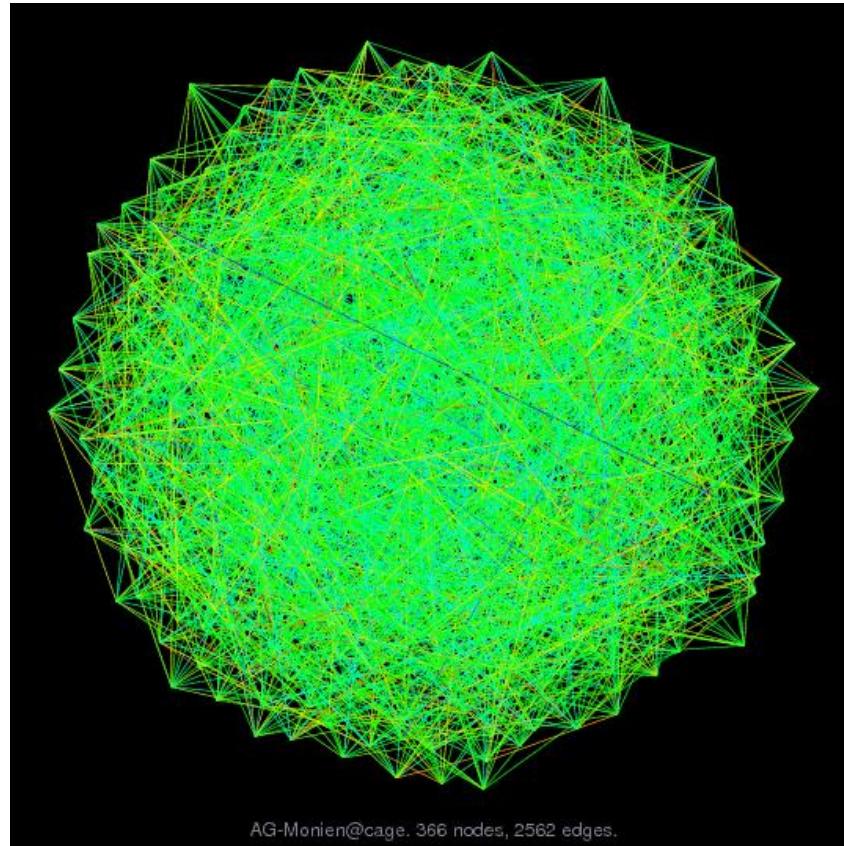
Validation

- How do you know if it works?
- How do you measure it?
 - How do you decide the benchmark data?
- How do you argue that one design is better or worse than another?
- What does it better mean?
 - Do user get something done faster?

Why it can go wrong?

- I do not understand
 - Poor match with the properties of the human perceptual and cognitive system
- Lack of context
 - Comprehensible by a human in some other setting
- Scalability problems

Why it can go wrong?



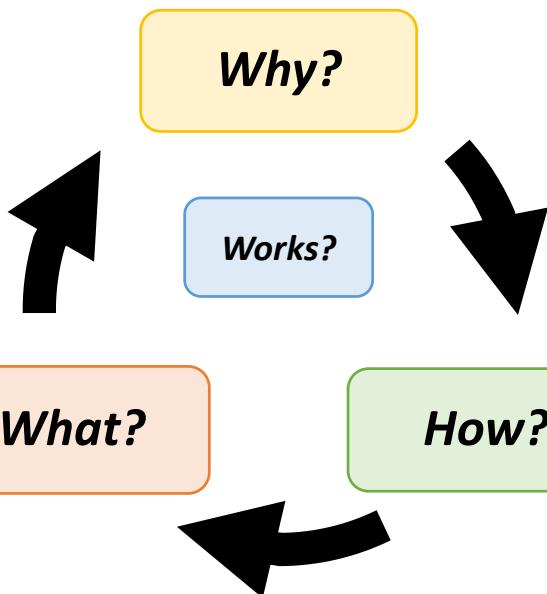
<http://yifanhu.net/GALLERY/GRAPHS>

Good Practices

- Do not optimize, satisfy
 - **The perfect visualization does not exist!!**
- Need to know a wide variety of vis techniques
 - Ease the design process using references
- Justification and Alternatives
 - 3D vs 2D?
- Eyes Beat Memory
 - Comparing views better than switch views
- Interactivity and Responsiveness

Life Cycle

- Follow the **life cycle** of a visualization tool
 - Profile of the user (expert, novice,...)



Prototype!

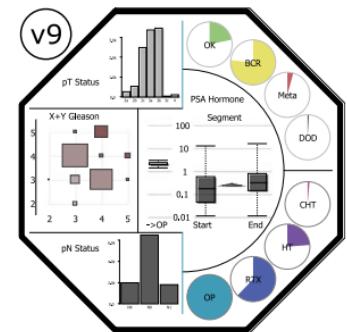
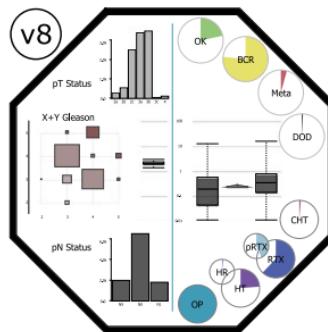
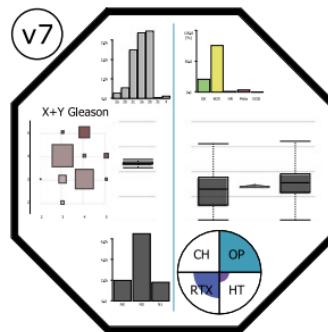
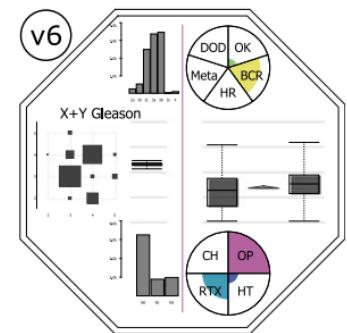
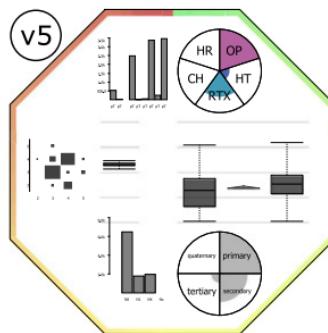
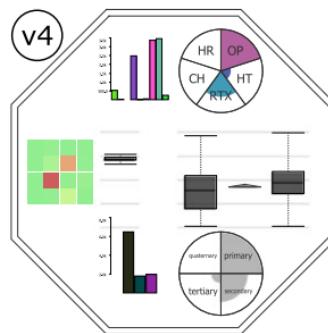
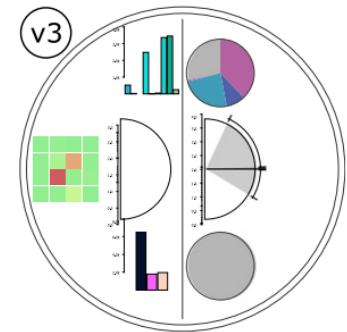
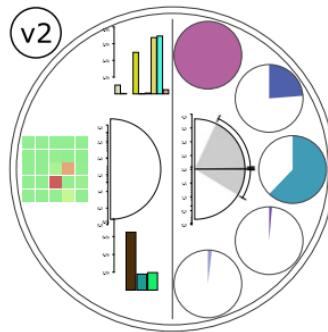
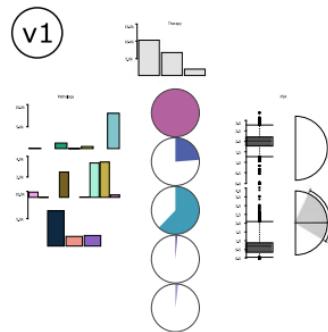


Trust the experts!



Evaluate!

Example: Using Dashboard Networks to Visualize Multiple Patient Histories



Overview of 15 Most Relevant Attributes Describing the Condition of a Patient

Attribute	Description	Att. Type	Value Domain	Visual Enc.
PSA Pre-OP	The value of the PSA hormone is a most important biological indicator for prostate cancer. Last measurement of the PSA hormone before OP (surgery).	Numerical	$[0;200.0[\frac{ng}{ml}]$ median : 8.7	
PSA at segment start	Value of the PSA hormone at start of the visualized temporal segment.	Numerical	$[0;4,472.0[\frac{ng}{ml}]$ median : 0.21	
PSA at segment end	Value of the PSA hormone at the end of the visualized temporal segment. Used to assess the progression of the PSA value within the segment interval.	Numerical	$[0;4,472.0[\frac{ng}{ml}]$ median : 0.26	
PSA trend in segment	Trend of the PSA hormone value within the duration of a temporal segment. Depicts the delta between the PSA values in a relative way.	Numerical	$] - 70.3;4381.68[\frac{ng}{ml}]$ median : 0.0	
pT-status	Histopathological status of the tumor, obtained by pathology report (pT - pathological tumor). Used for prognoses about the progress of the disease.	Ordinal	<i>pt2a, pt2b, pt2c, pt3a pt2b, pt3c, pt4</i>	
pN-status	Histopathological characteristics of the tumor, obtained by pathology report. Used for prognoses about the progress of the disease.	Ordinal	<i>NX, N0, N1</i>	
Gleason Score	Histopathological characteristics of the tumor, obtained by pathology report. Used for prognoses about the progress of the disease.	Ordinal	$2+3, 3+2, 3+3, 3+4, 3+5,$ $4+3, 4+4, 4+5, 5+3, 5+4$	
OK after OP	Outcome variable (biological condition) reflecting a good condition after OP. Is active until relapse or metastases.	Boolean	<i>[false, true]</i>	
BCR	Outcome variable (biological condition) describing the biochemical recurrence (relapse) of the tumor. Used for prognoses about the progress of the disease.	Boolean	<i>[false, true]</i>	
Metastases	Outcome variable (biological condition) describing whether a patient got metastases. Metastases are the most severe biological indicator in the dataset.	Boolean	<i>[false, true]</i>	
DOD	Biological end point when a patient died of disease. Often used for cause-effect analyses.	Boolean	<i>[false, true]</i>	
OP	Treatment attribute reflecting whether a patient had surgery. In the dataset all patients received OP.	Boolean	<i>[false, true]</i>	
RTX	Treatment attribute reflecting whether a patient got radiation therapy. Local treatment, only affecting the prostate area.	Boolean	<i>[false, true]</i>	
HT	Treatment attribute reflecting whether a patient had hormone therapy. Systemic treatment, affecting the whole human body.	Boolean	<i>[false, true]</i>	
CHT	Treatment attribute reflecting whether a patient got chemotherapy. Often applied in severe situations, e.g., when metastases are detected.	Boolean	<i>[false, true]</i>	

Immersive Analytics

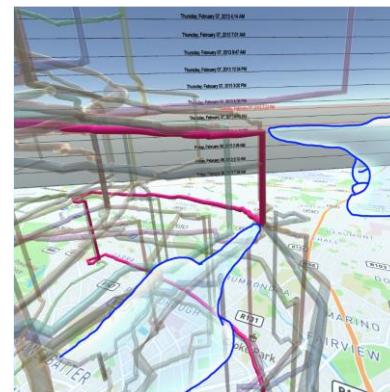
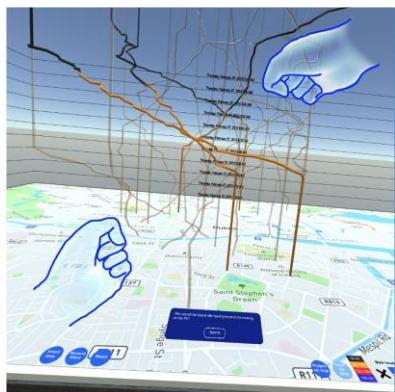
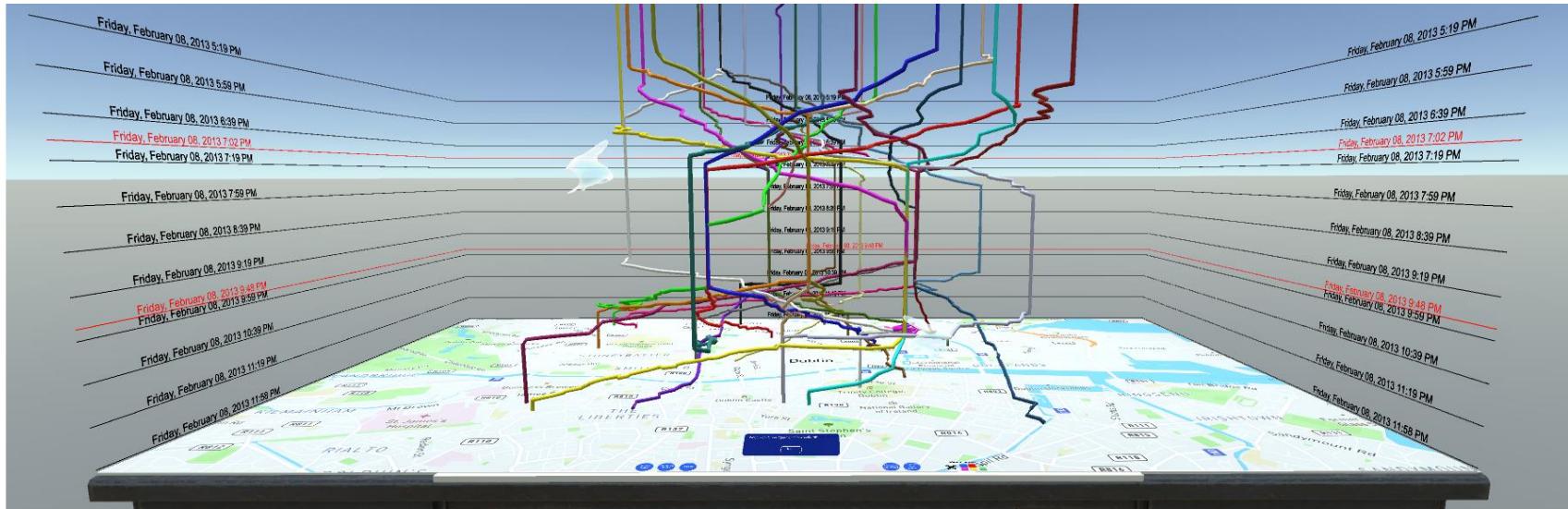
Focus

Immersive Analytics

*“Science of analytical reasoning facilitated by
immersive human-computer interfaces”*



Space-Time Cube Geovisualization



INFOVIS PAPER

Evaluating an Immersive Space-Time Cube Geovisualization for Intuitive Trajectory Data Exploration

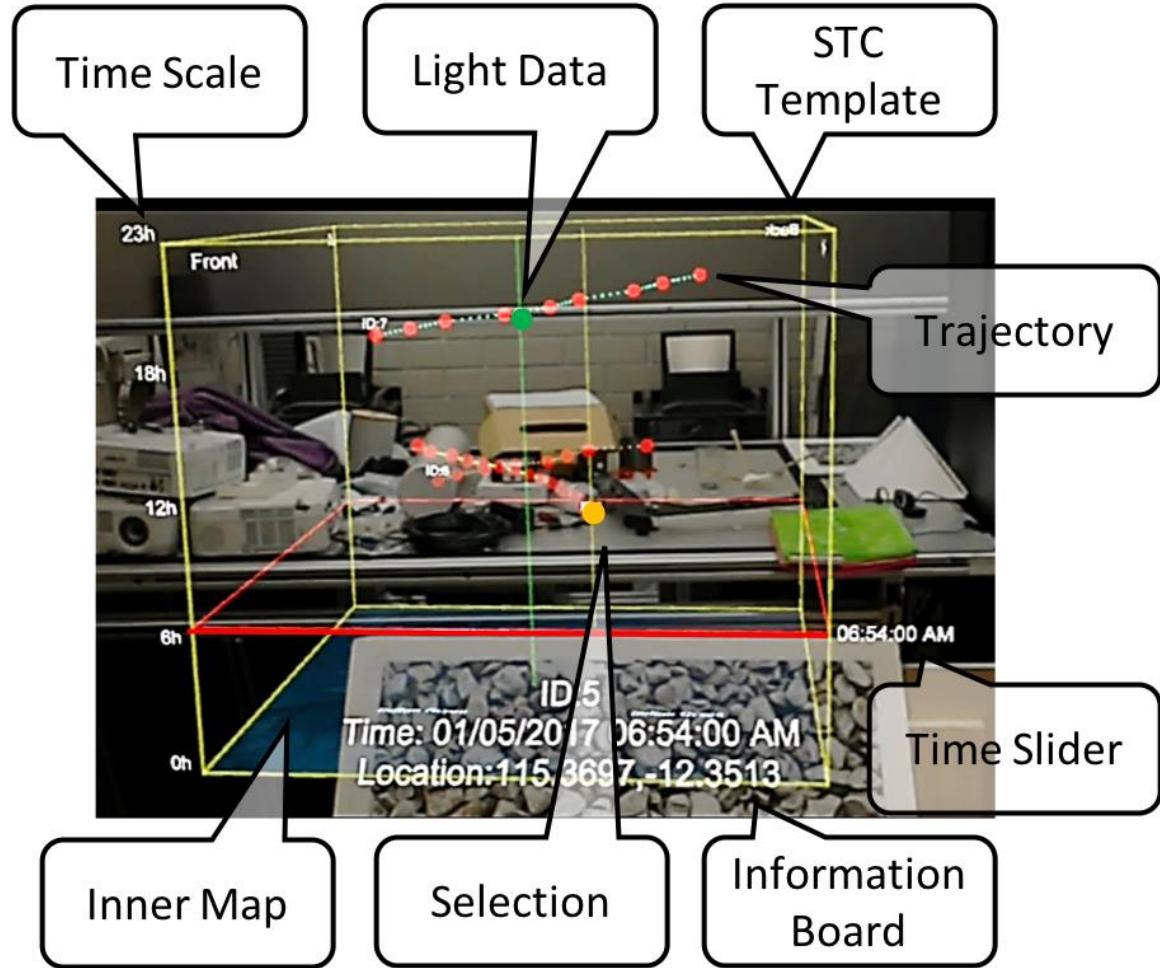
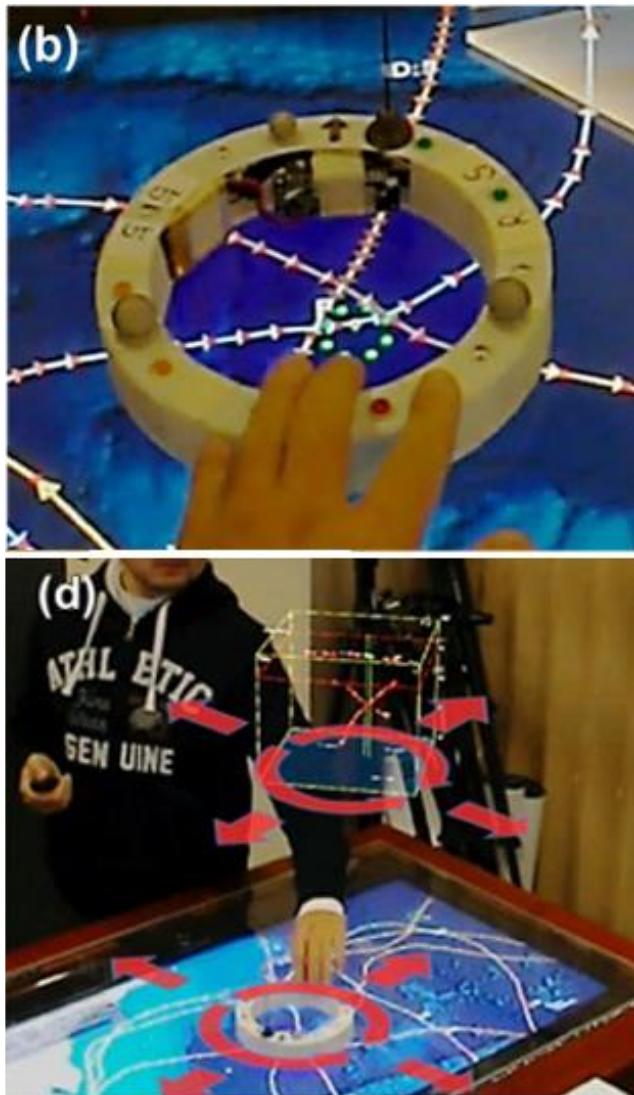
Jorge Wagner, Wolfgang Stuerzlinger, Luciana Nedel



20-25 October 2019
Vancouver, Canada

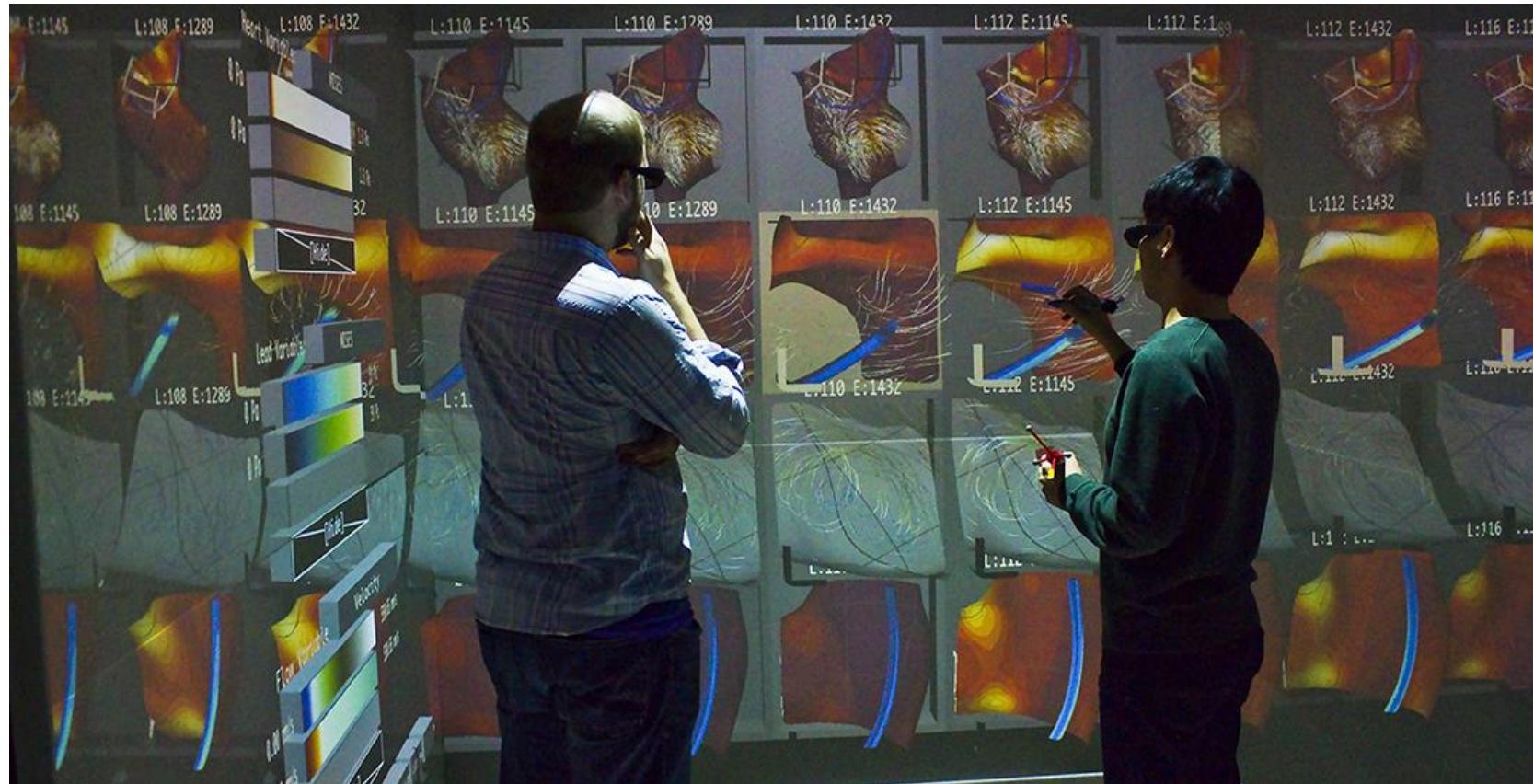
ieeevis.org

GeoGate

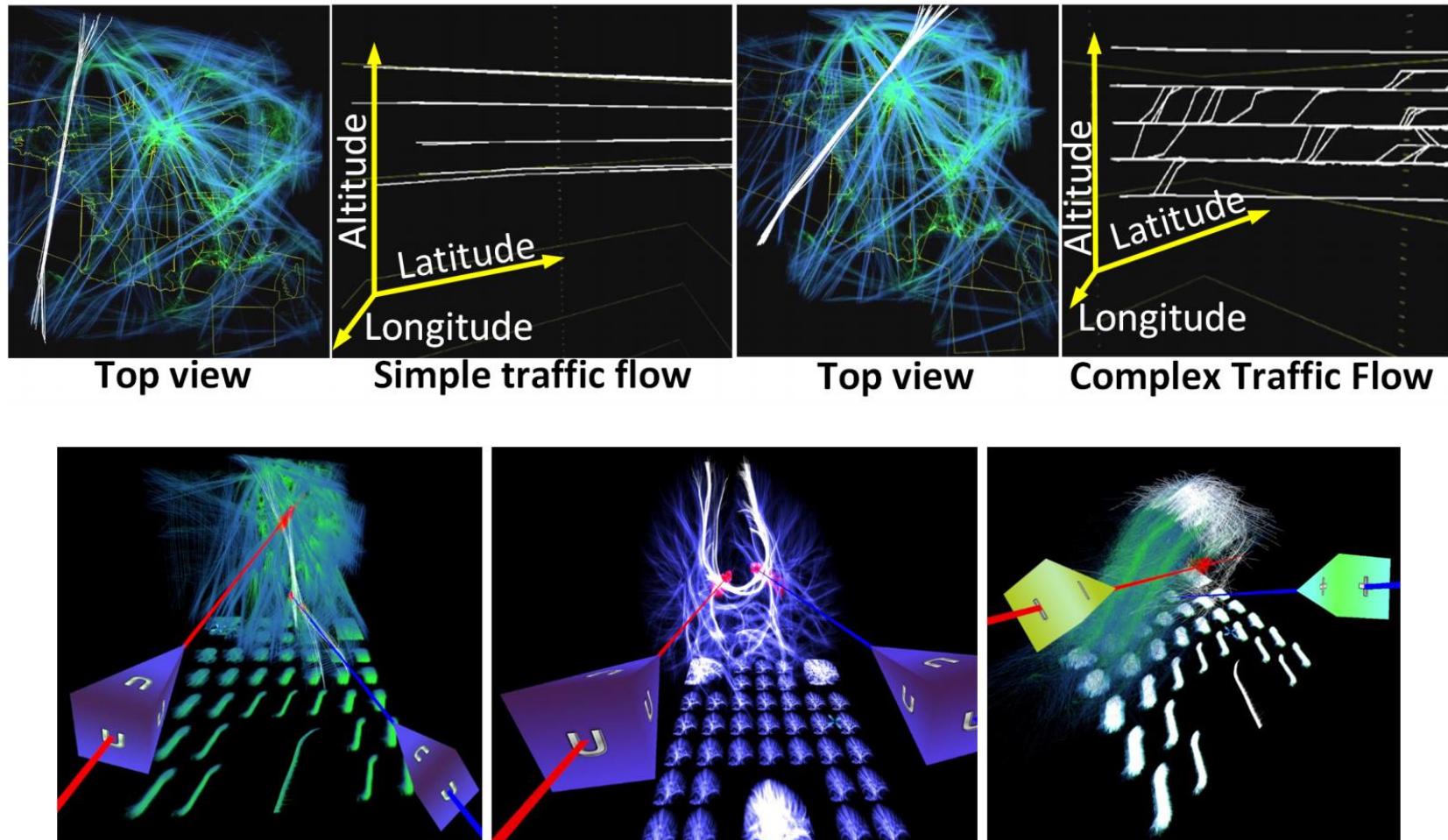


S. Y. Ssin, J. A. Walsh, R. T. Smith, A. Cunningham and B. H. Thomas, "GeoGate: Correlating Geo-Temporal Datasets Using an Augmented Reality Space-Time Cube and Tangible Interactions," 2019 IEEE Conference on Virtual Reality and 3D User Interfaces (VR), Osaka, Japan, 2019, pp. 210-219, doi: 10.1109/VR.2019.8797812.

Bento Box



FiberClay



INFOVIS PAPER

FiberClay: Sculpting Three Dimensional Trajectories to Reveal Structural Insights

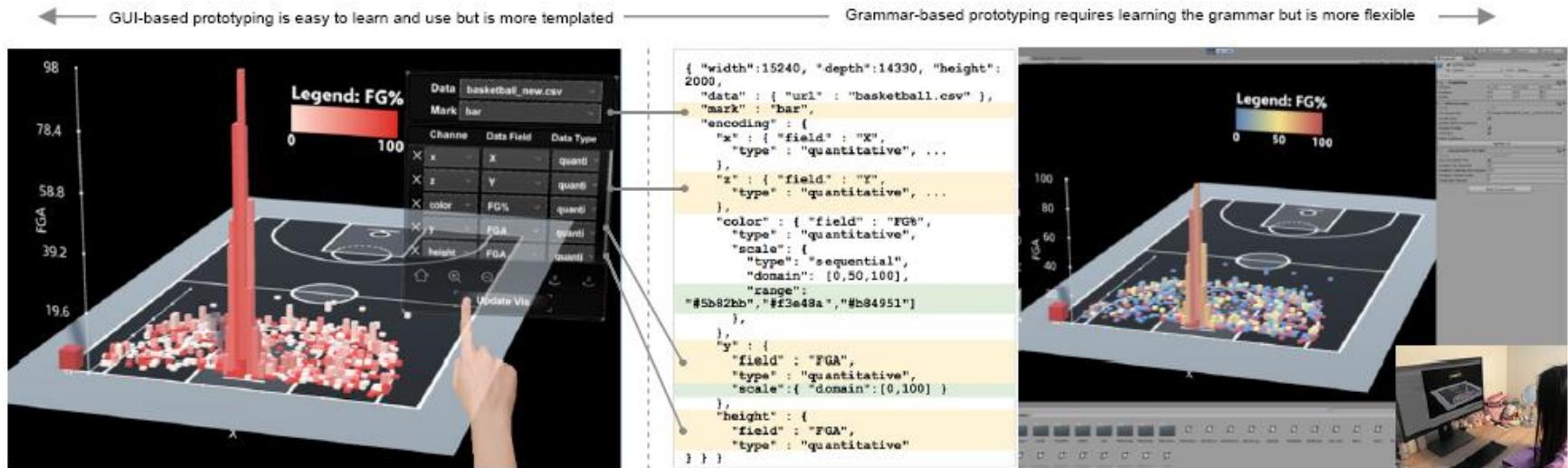
Christophe Hurter, Nathalie Henry Riche, Steven Drucker, Maxime Cordeil,
Richard Alligier, Romain Vuillemot



21–26 October 2018
Berlin, Germany

ieeevis.org

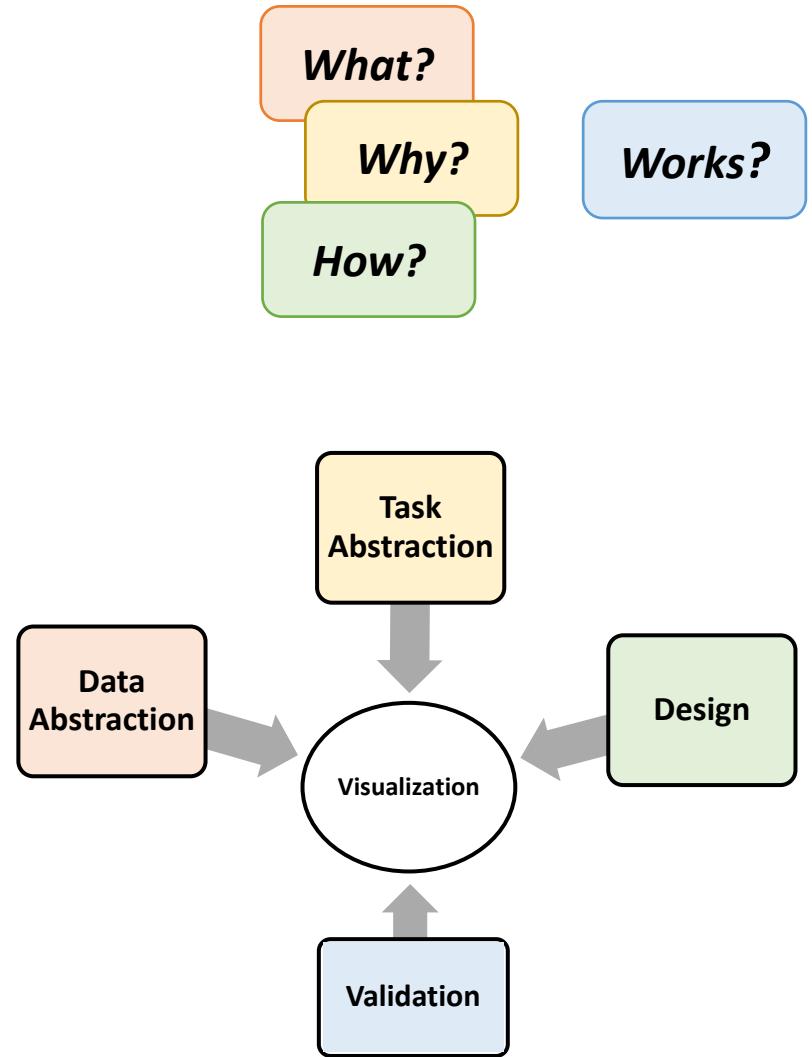
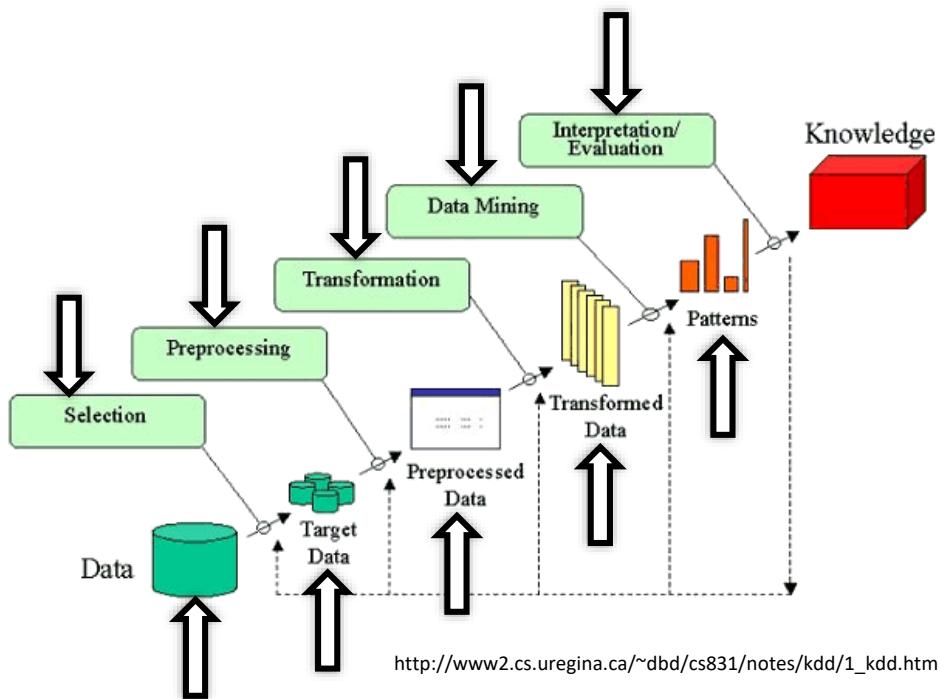
Toolkits for Immersive Analytics



Research Challenges in Immersive Analytics

- Combining Human and Computer Intelligence
- The Utility of Immersion
- Designing Immersive Analytics Systems
- Facilitating Collaboration through Immersion
- Changing the Process of Analysis with Immersion

Wrap Up



Further reading

- Remy Dautriche. Multi-scale Interaction Techniques for the Interactive Visualization of Execution Traces. Chapter 3.3, Pattern Visualization, 2016
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 - <http://www.cs.ubc.ca/labs/imager/tr/2009/VisChapter/akp-vischapter.pdf>
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Further reading

- **Visualization Analysis and Design**
- **Design for Information: An Introduction to the Histories, Theories, and Best Practices Behind Effective Information Visualizations**
- **The Functional Art: An introduction to information graphics and visualization**

