# Symbolic Verification of Distance-bounding Protocols

Application to payments protocols

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## Scenario

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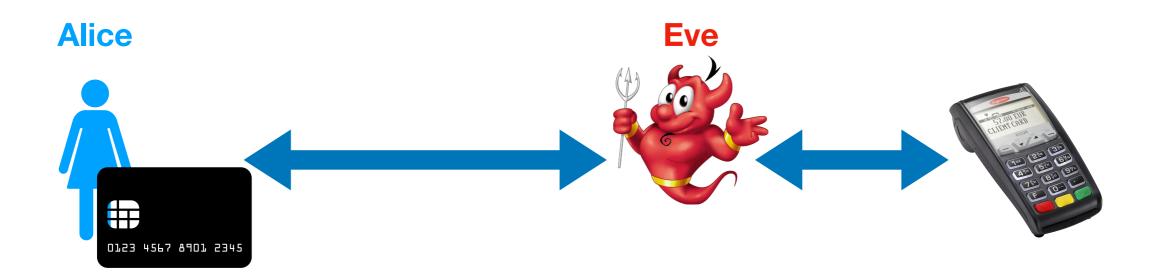
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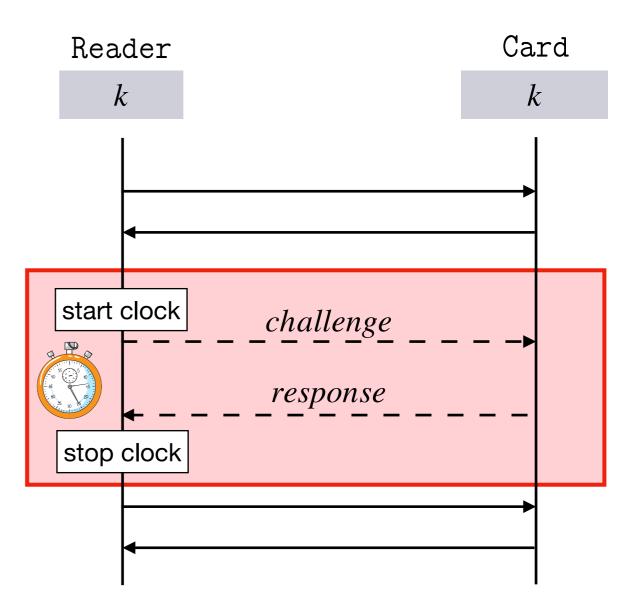
#### **Existing solutions**

- Steal the item...
- Steal a credit card: by-pass the PIN code, pay on the Internet, contactlessly...
- Abuse a victim by relaying messages using the contactless technology



#### **History of distance-bounding protocols**

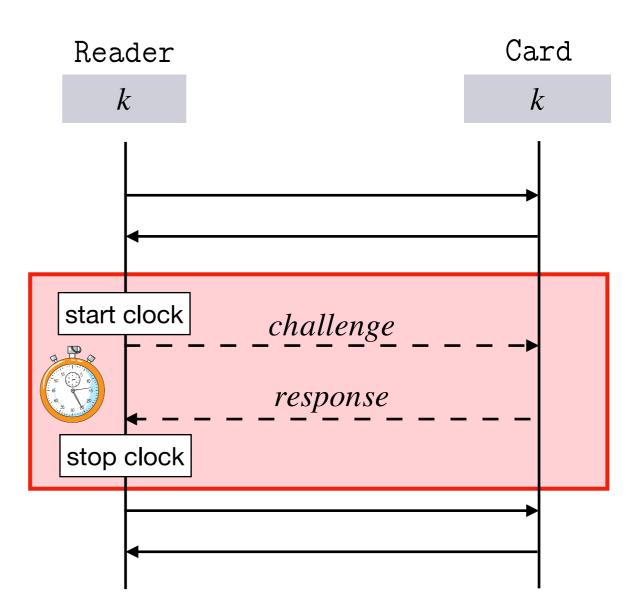
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Designing a good protocol is difficult!



# Many applications that are insecure....











# Two major families of models...

... with some advantages and some drawbacks.

## Computational models

- + messages are bitstrings, a general and powerful attacker
- tedious proofs, sometimes mechanized, but often for experts only



## Symbolic models

- Some simplifications/abstractions (messages, attacker...)
- + procedures and automated tools





Some results make a link between these two models [Abadi & Rogaway - 2000]

# Symbolic verification in a nutshell

#### Messages

- Function symbols: enc(x, k), sign(x, k), h(x),...

**Perfect cryptography** 

- Equations: dec(enc(x, k), k) = x

#### **Protocols**

- Process algebra, multiset rewriting rules, Horn clauses...

#### The attacker can...



read / overwrite messages



intercept / block messages

#### The attacker cannot...



break crypto



use side-channels

# **Existing verification tools**

#### Bounded number of sessions

- decidable for classes of protocols
- ► tools implement decision procedures



**AKiSs** 

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- efficient tools in practice but:
  - do some approximations
  - may not terminate

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5G-AKA

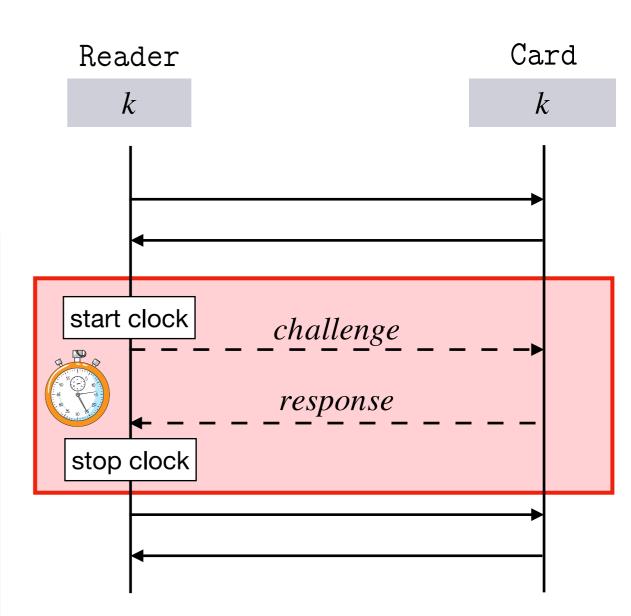


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- Standard models and tools: do not model time and locations!
- Main specific models:
  - Meadows et al. (2007),
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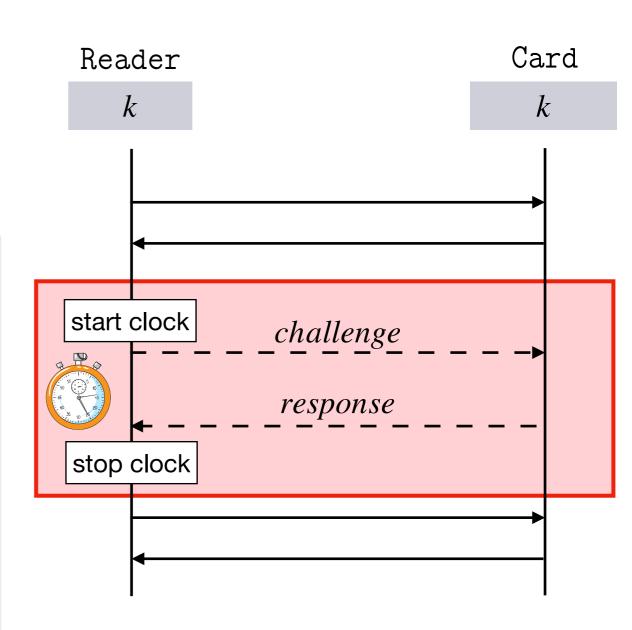


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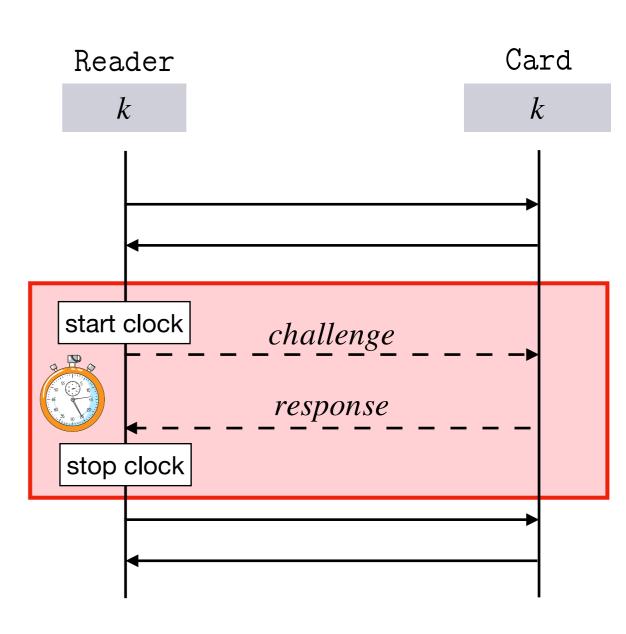
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- Recently: Mauw et. al. (2018, 2019)



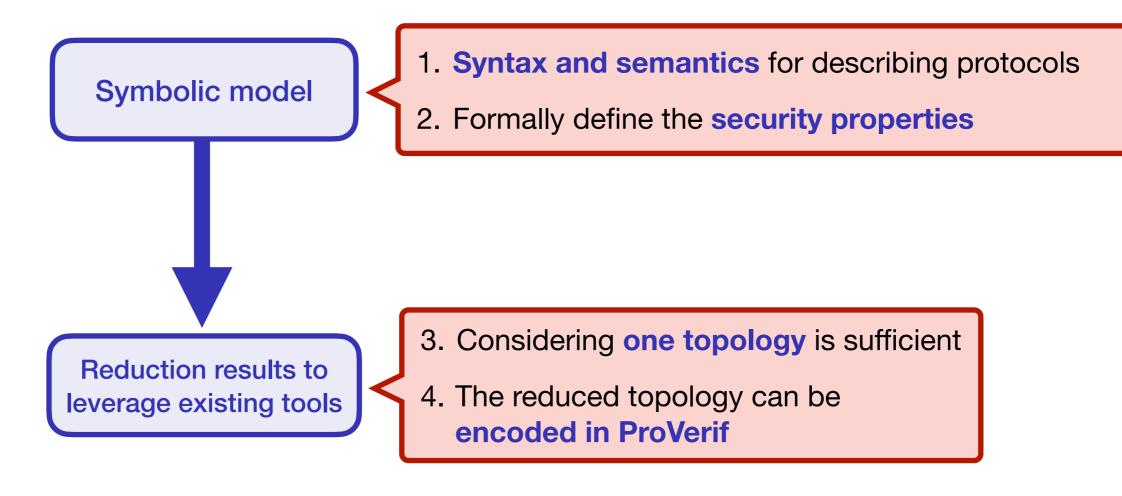
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# The story of verification

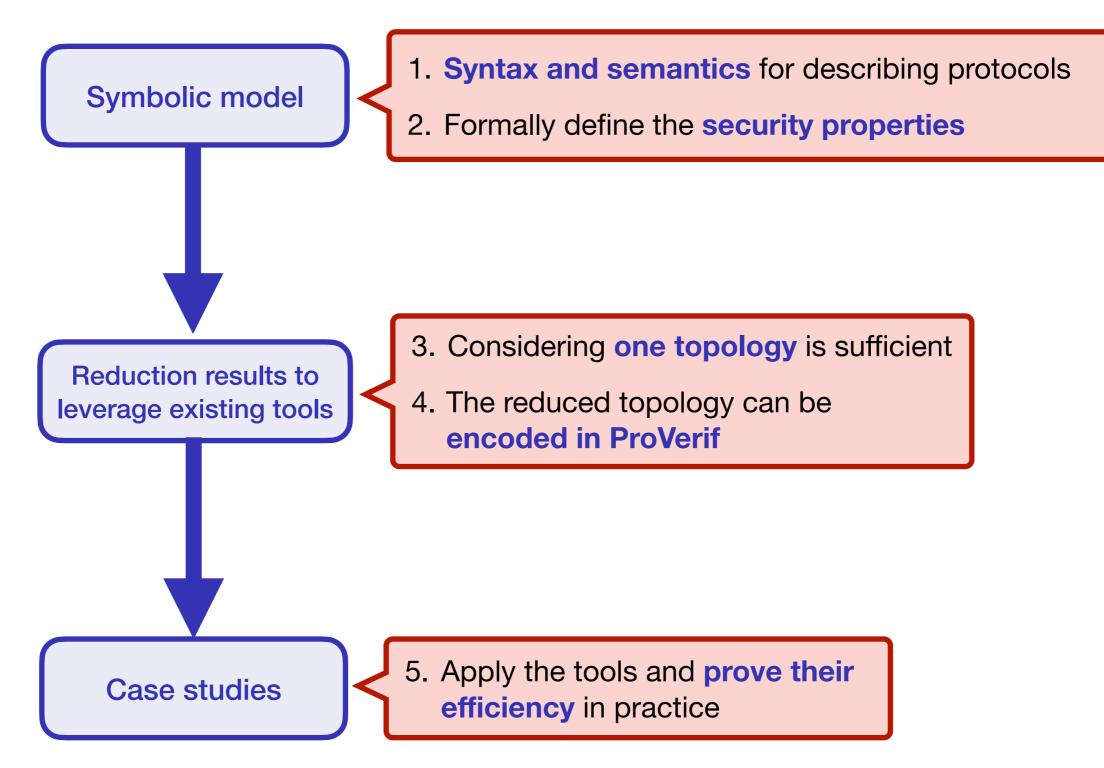
Symbolic model

- 1. Syntax and semantics for describing protocols
- 2. Formally define the security properties

# The story of verification



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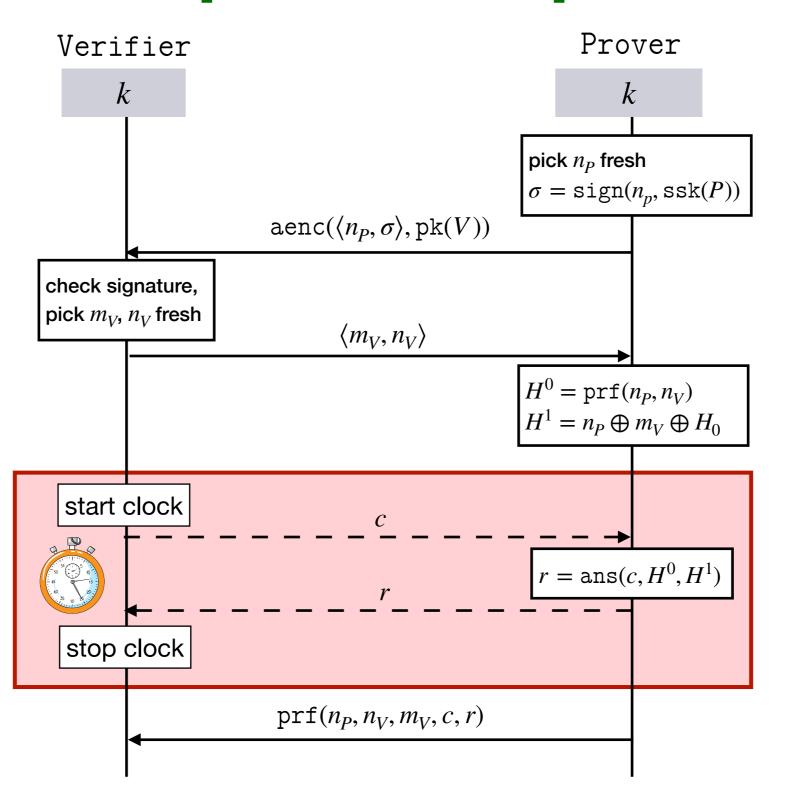


# A symbolic model with time and locations

syntax and semantics

# **SPADE**

## [Bultel et al. - 2016]



# Term algebra



Messages: terms built over a set of names  $\mathcal N$  and a signature  $\Sigma$  given with either an equational theory E or a rewriting system.

#### **Example**

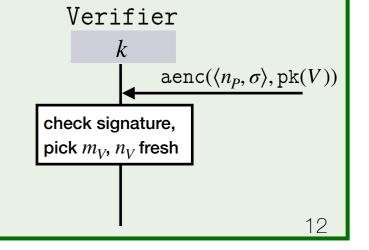
► Function symbols: aenc, adec, pk, sk, sign, get\_message, spk, ssk,  $\langle \cdot, \cdot \rangle$ , proj<sub>1</sub>, proj<sub>2</sub>

#### ► Rules:

$$\begin{split} \operatorname{adec}(\operatorname{aenc}(x,\operatorname{pk}(y)),\operatorname{sk}(y)) \to x & \operatorname{proj}_1(\langle x,y\rangle) \to x \\ \operatorname{get\_message}(\operatorname{sign}(x,\operatorname{ssk}(y)),\operatorname{spk}(y)) \to x & \operatorname{proj}_2(\langle x,y\rangle) \to y \\ \operatorname{eq}(x,x) \to ok & \end{split}$$

#### **Running example**

$$V(v,p) = \text{in}(x)\,.$$
 
$$\text{let } u = \text{adec}(x,\text{sk}(v)) \text{ in}$$
 
$$\text{let } x_{ok} = \text{eq}(\text{proj}_1(u),\text{get\_message}(\text{proj}_2(u),\text{spk}(P)) \text{ in}$$
 
$$\cdots$$



# Process algebra

The role of each agent is described by a process following the grammar:

$$P := 0$$
 null process 
$$| new \ n . P$$
 name restriction 
$$| let \ x = u \ in \ P$$
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# Running example $V(v,p) = \operatorname{in}(x).$ let $u = \operatorname{adec}(x,\operatorname{sk}(v))$ in let $x_{ok} = \operatorname{eq}(\operatorname{proj}_1(u),\operatorname{get_message}(\operatorname{proj}_2(u),\operatorname{spk}(P))$ in new $m_V$ . new $n_V$ . out( $\langle m_V,n_V\rangle$ ). reset.new c.out(c).inct(c)....

# **Semantics**

#### **Physical restrictions**

- ▶ locations: elements in  $\mathbb{R}^3$ , i.e. Loc :  $\mathscr{A} \to \mathbb{R}^3$
- distance: Euclidean norm between locations, i.e.  $\text{Dist}(a,b) = \frac{\|\text{Loc}(a) \text{Loc}(b)\|}{c}$
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#### System configuration $(\mathcal{P}, \Phi, t)$

- multiset of processes which remain to execute, i.e.
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#### **Execution rules**

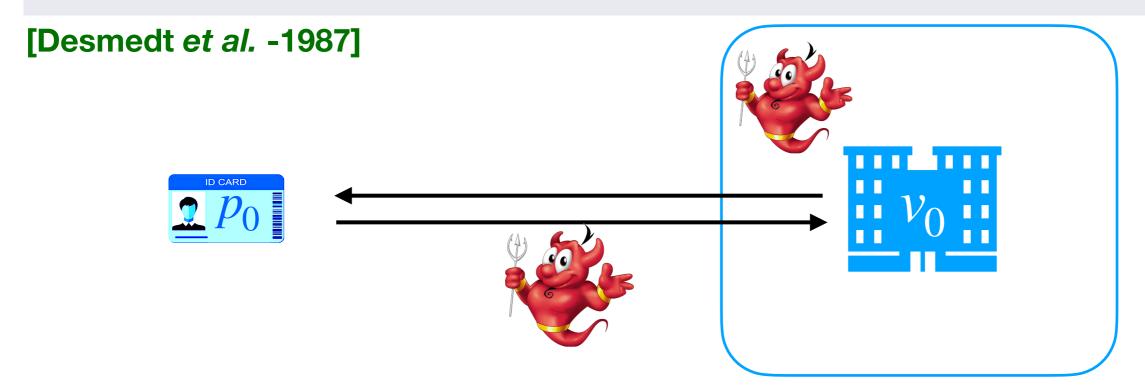
- ► TIM:  $(\mathcal{P}, \Phi, t) \longrightarrow (Shift(\mathcal{P}, \delta), \Phi, t + \delta)$  with  $\delta > 0$
- ► *IN*:  $([in(x).P]_a^{t_a} \uplus \mathscr{P}, \Phi, t) \xrightarrow{a, in(u)} ([P\{x \mapsto u\}]_a^{t_a} \uplus \mathscr{P}, \Phi, t)$

if u is deducible from  $\Phi$  at time t

**•** ...

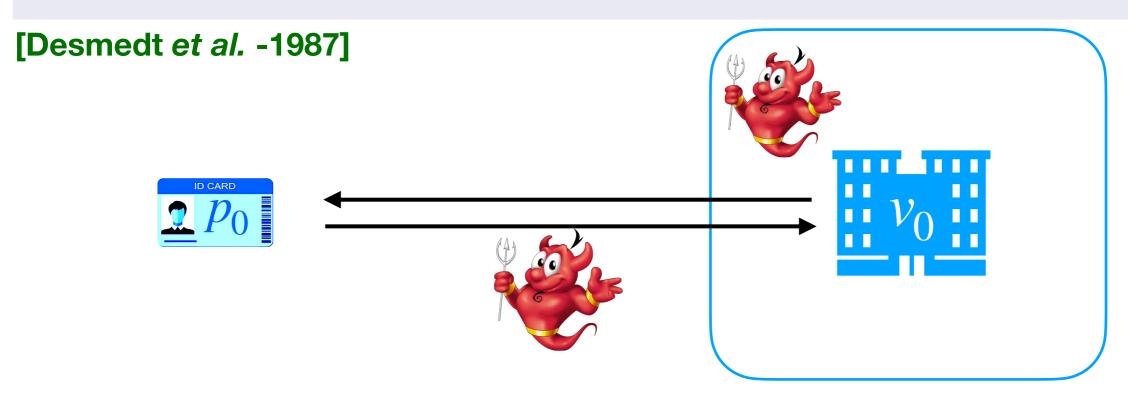
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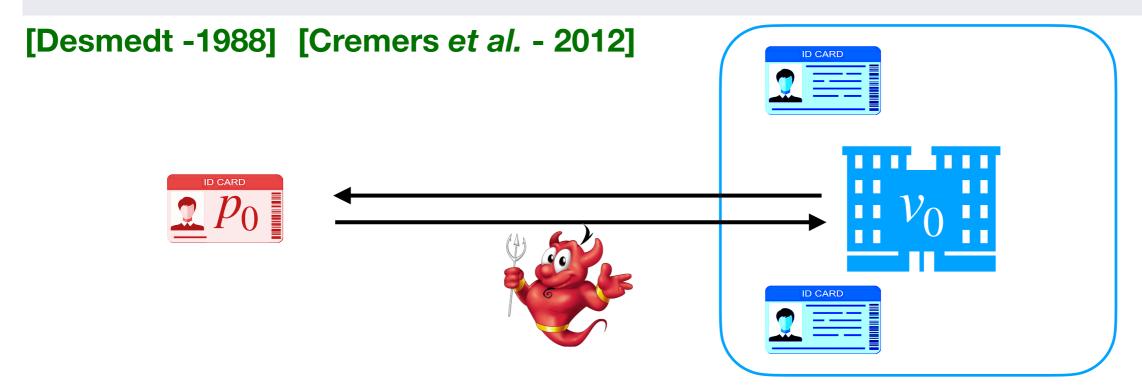
#### **Definition**

A protocol admits a mafia fraud if there exists a topology  $\mathcal{T} \in \mathcal{C}_{\mathrm{MF}}$  and an initial configuration K such that:

$$K \longrightarrow ([\operatorname{end}(v_0, p_0)]_{v_0}^{t_{v_0}}; \Phi; t)$$

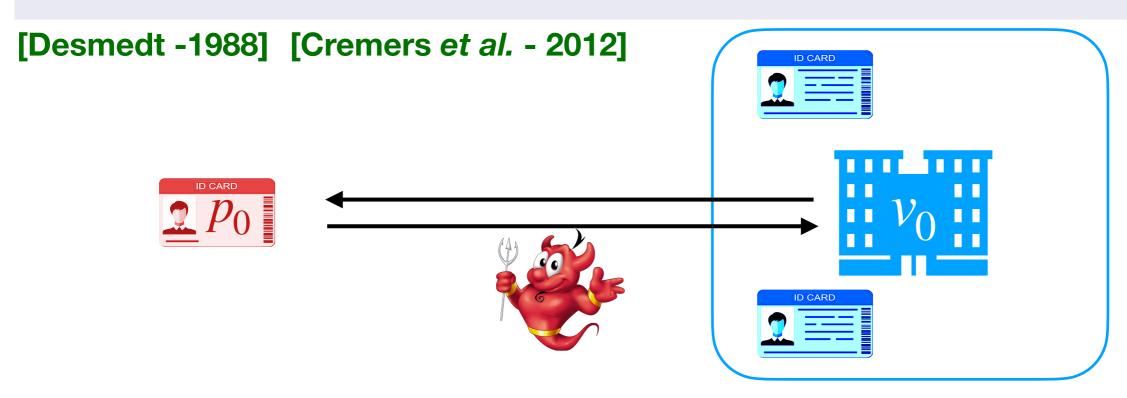
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# Some reduction results

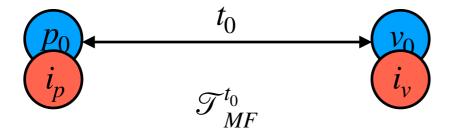
Topologies and time

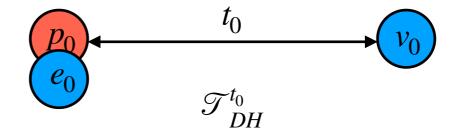
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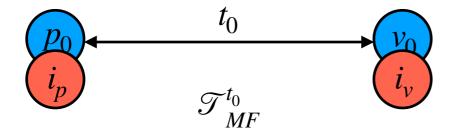
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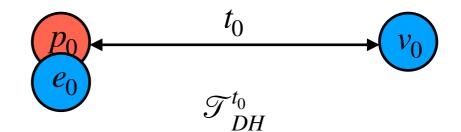


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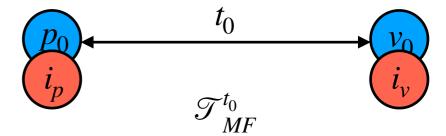




- 2. We must deal with time when conducting our analyses
  - -> we can use ProVerif's phases to encode the topologies!

## Theorem

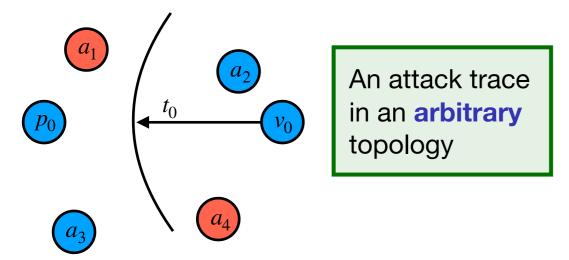
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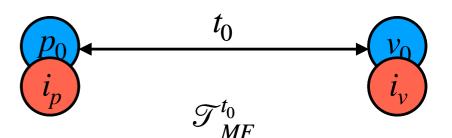


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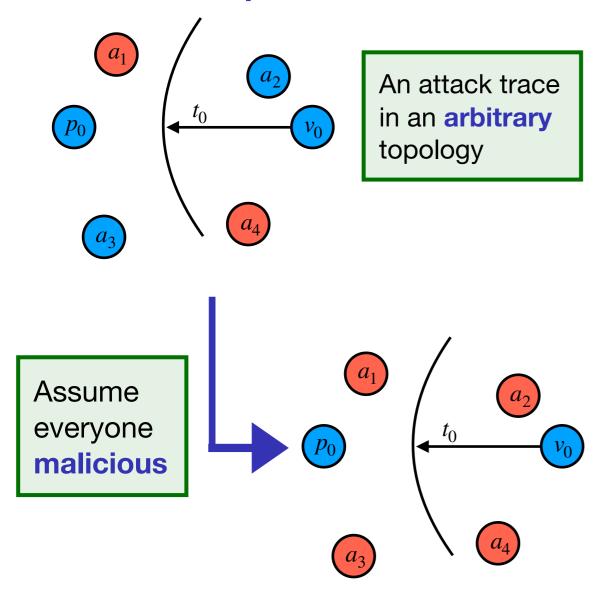


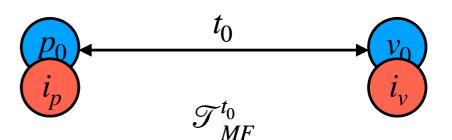


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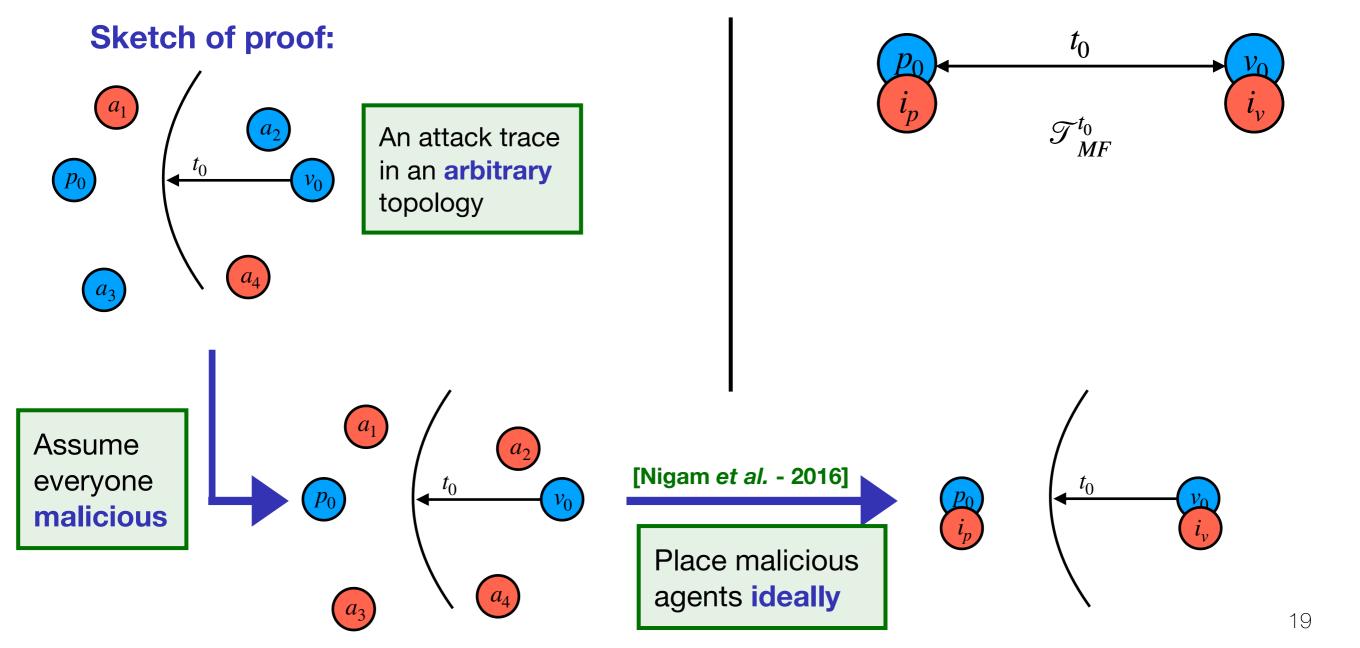
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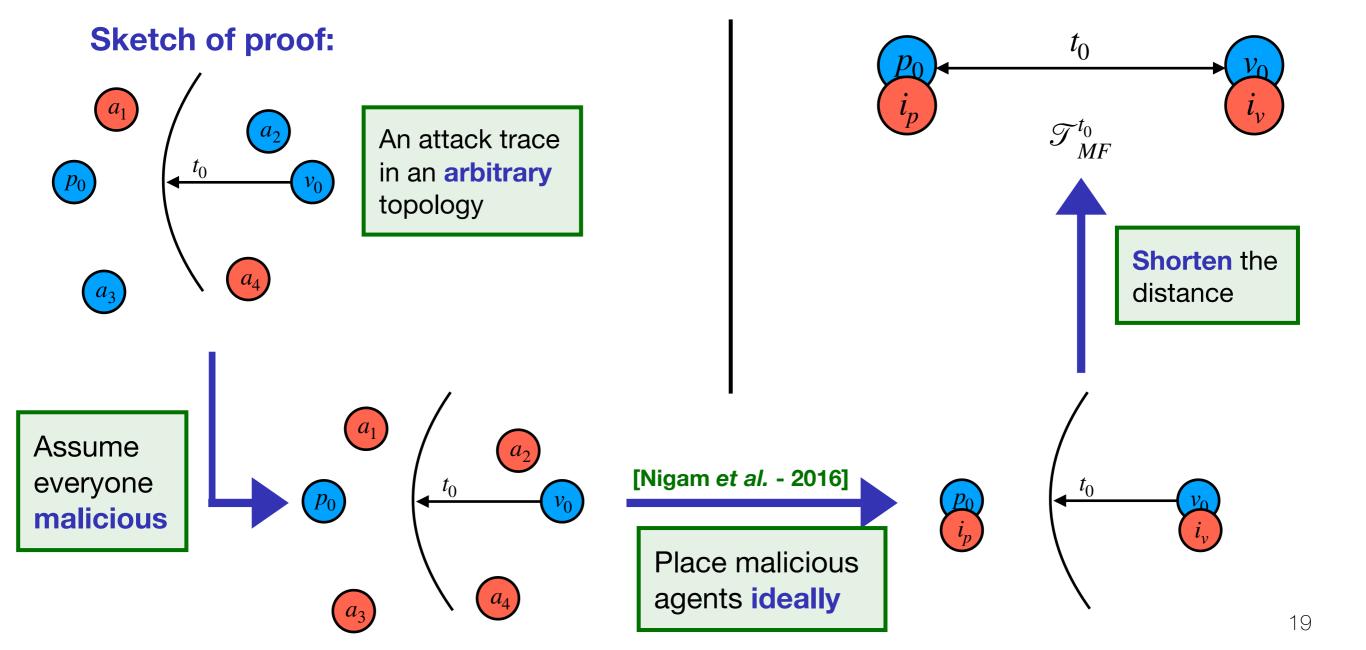
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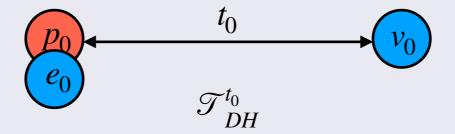
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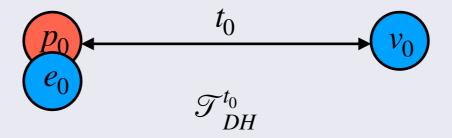
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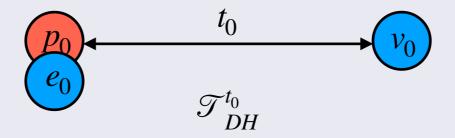
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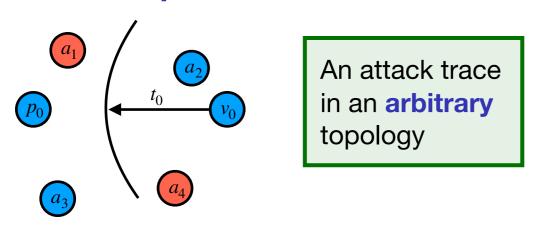
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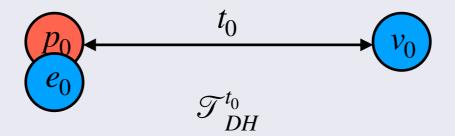
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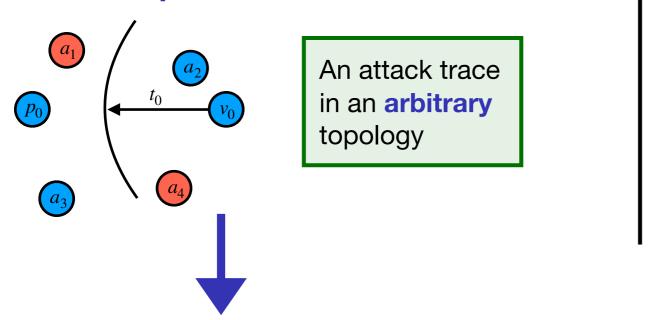
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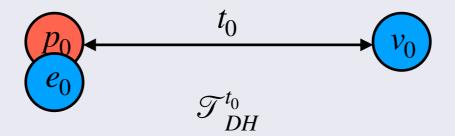
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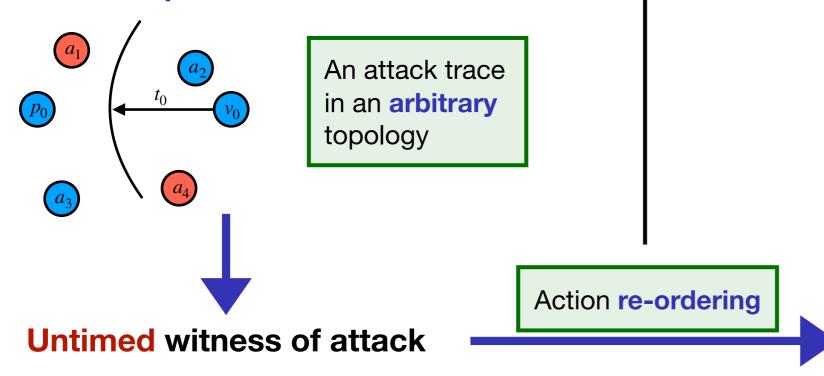
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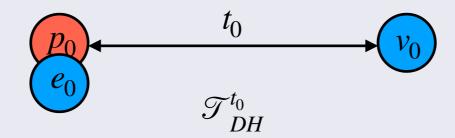
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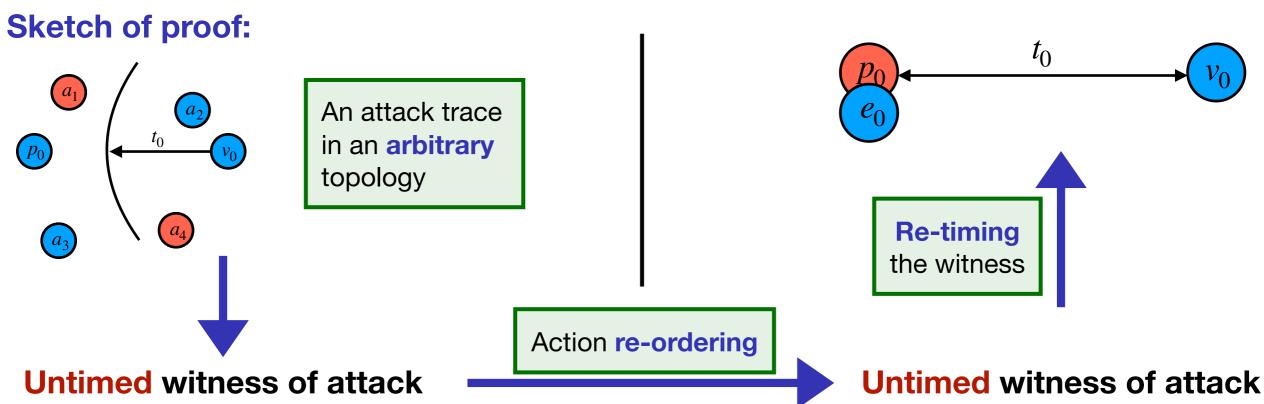
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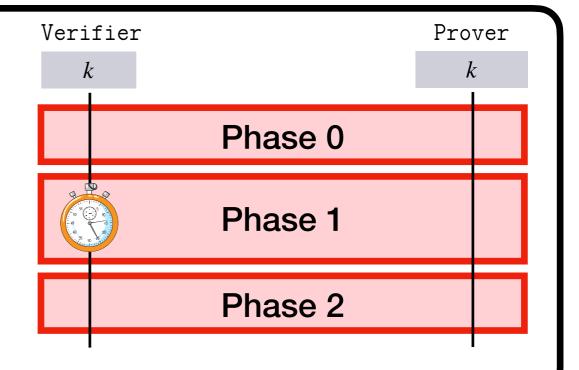
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# Encoding the two topologies with phases [Chothia et al. - 2015]

- → it relies on the phases of ProVerif
  - ► Phase 0 slow initialization phase
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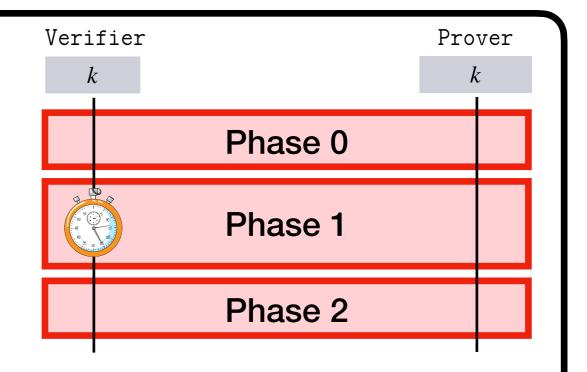


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## **Proposition**

If a protocol  $\mathscr{P}_{db}$  admits a mafia fraud (resp. distance hijacking, terrorist fraud) then  $\operatorname{end}(v_0,p_0)$  is reachable in  $\mathscr{F}(\mathscr{P}_{db})$ .

# A comprehensive case studies analysis

Application to distance-bounding protocols

# Case studies analyses

Corpus +25 protocols

**Tool** ProVerif (slightly modified for distance hijacking attacks)

**Abstractions** ► rapid phase collapsed in a single round-trip

weak exclusive-OR

tool limitation

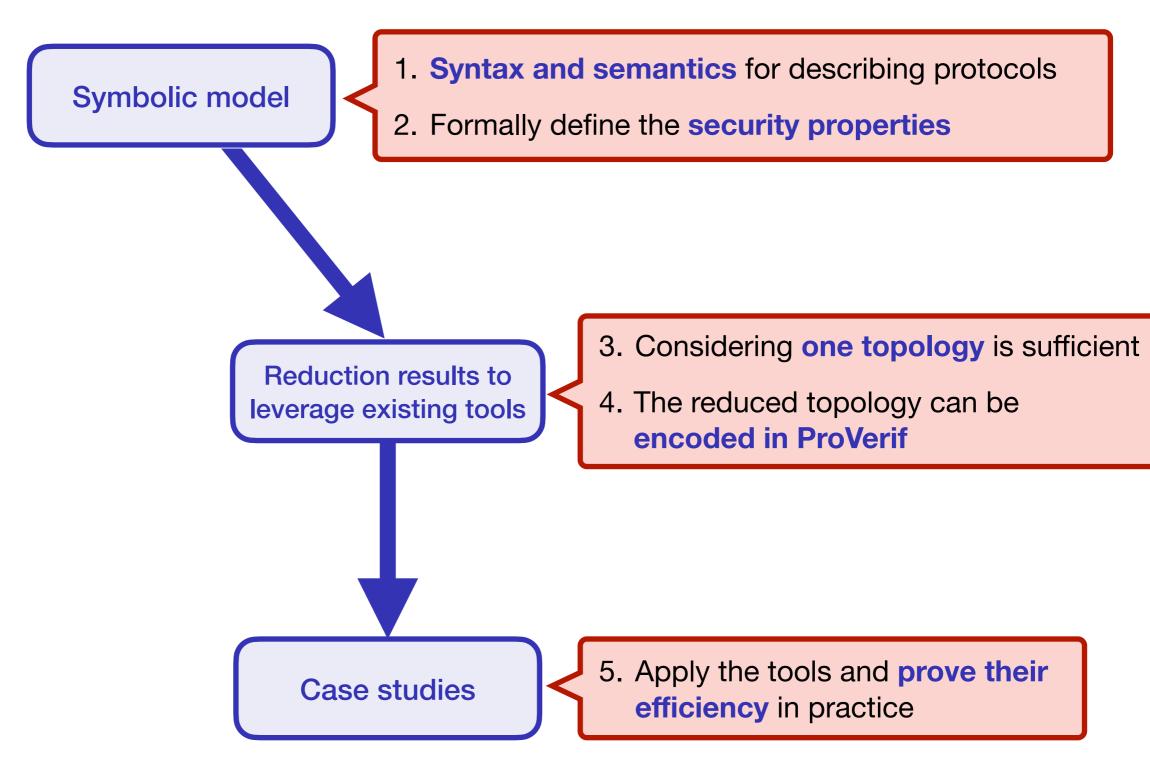
model limitation

#### **Application to real-world protocols**

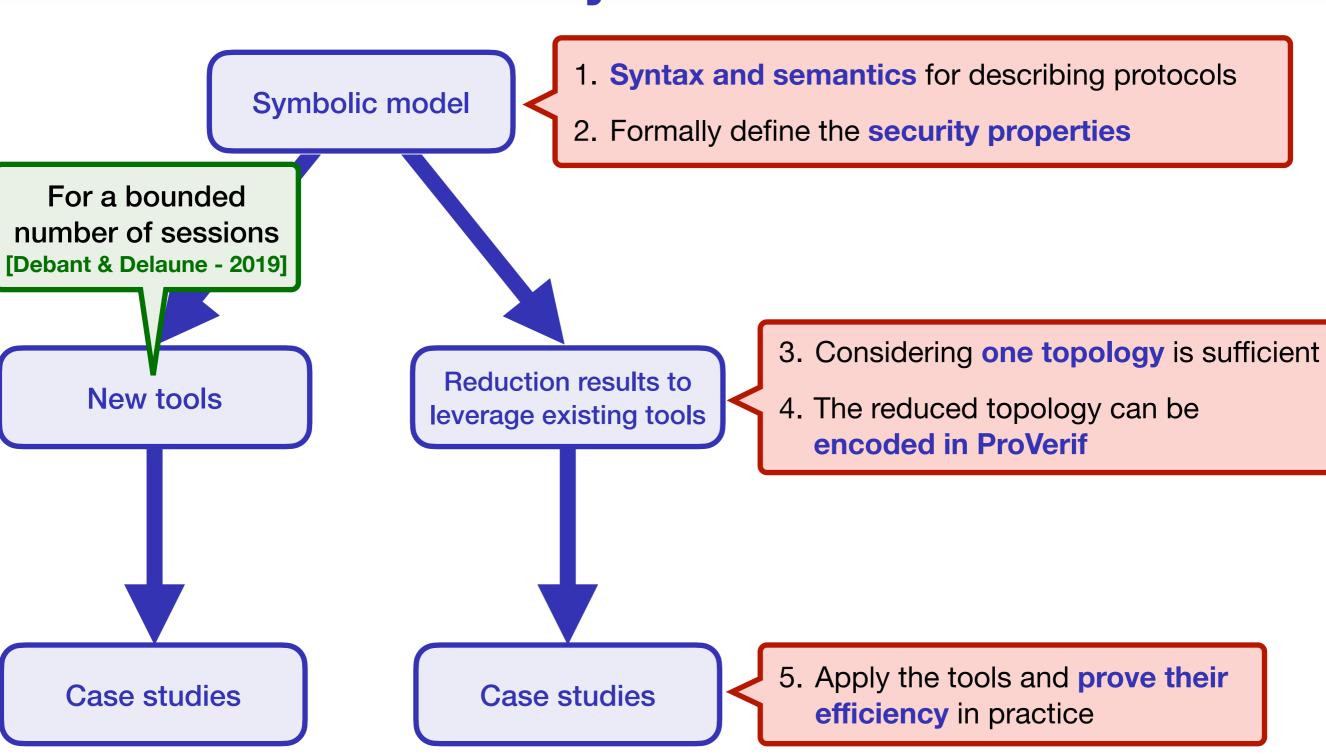
Protocols	Mafia fraud	Distance hijacking	Terrorist fraud
MasterCard RRP	✓	X	X
PaySafe	✓	X	X
MIFARE Plus	✓	X	X

# Conclusion

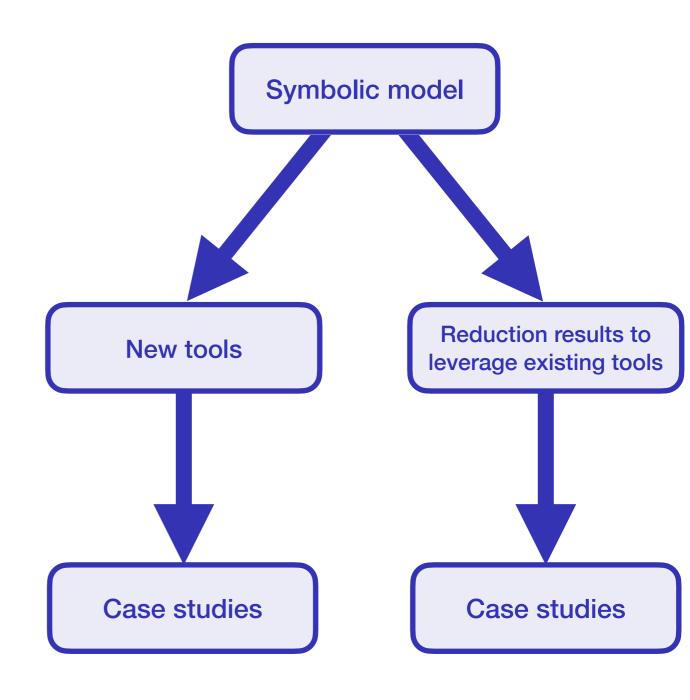
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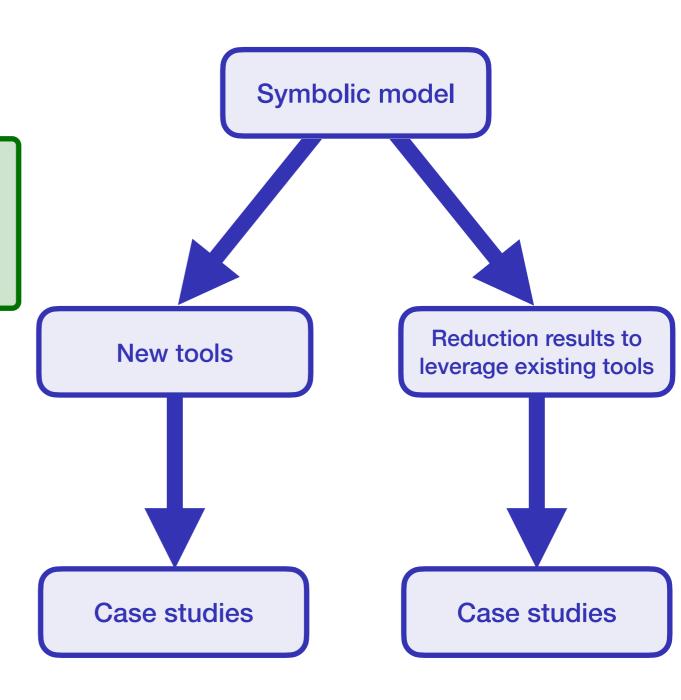
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- extend ProVerif's procedure
- improve automation for Tamarin



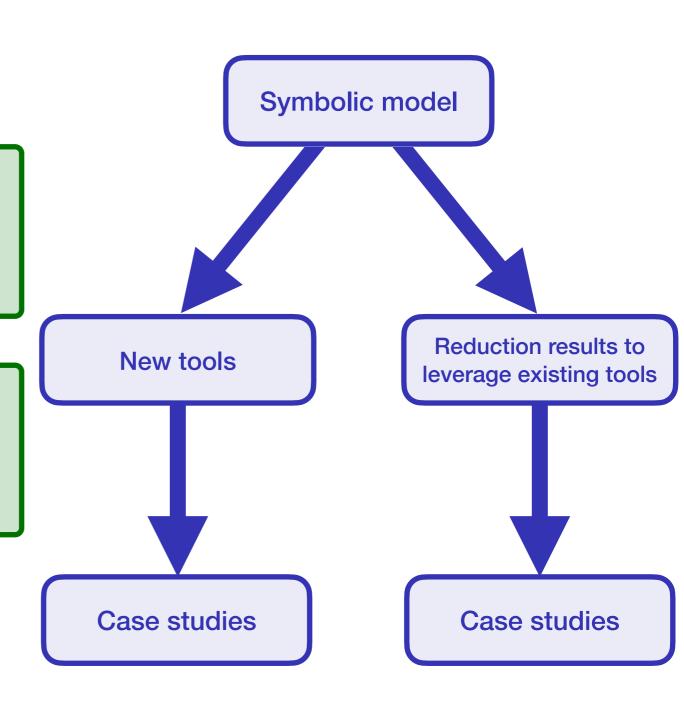
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#### **Model bit-level operations**

- consider probabilistic processes and properties
- model messages with bitstrings

