A symbolic framework to analyse physical proximity in security protocols

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Symbolic model Reduction results

Applications

Introduction

Security protocols

Distributed programs that use cryptographic primitives to ensure security properties.



Authentication

Integrity



Untraceability

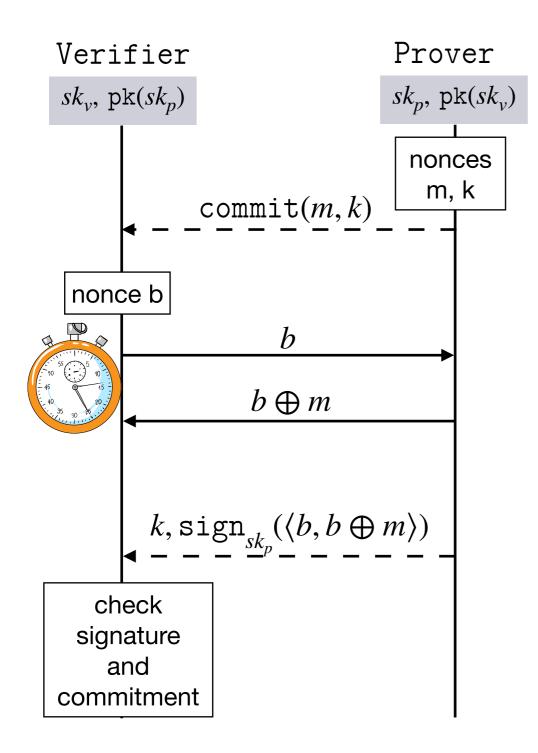
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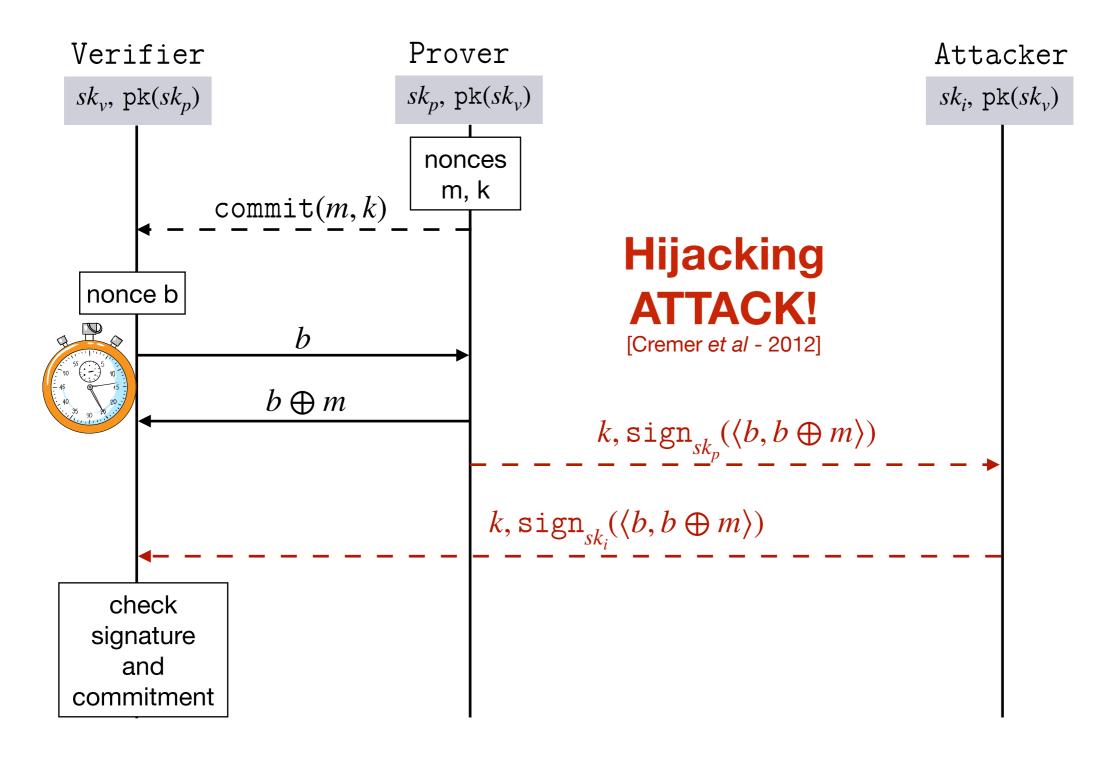
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Authentication with physical proximity





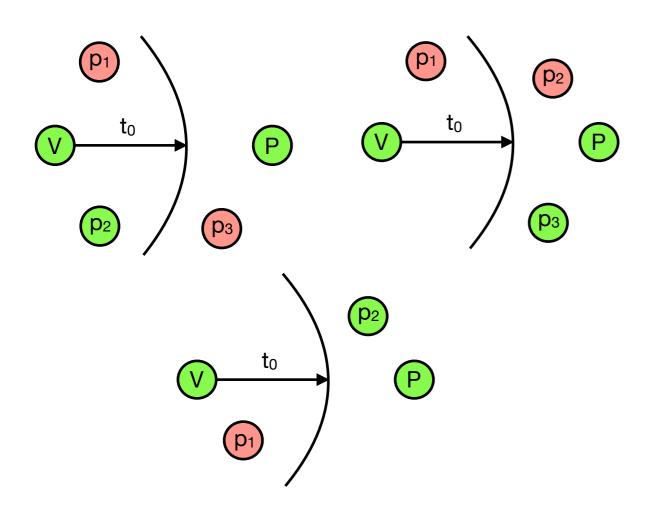
Classes of attacks

Mafia frauds

(or Man-in-the-Middle)

An attack in a topology such that:

- ►V is honest
- ► P is honest



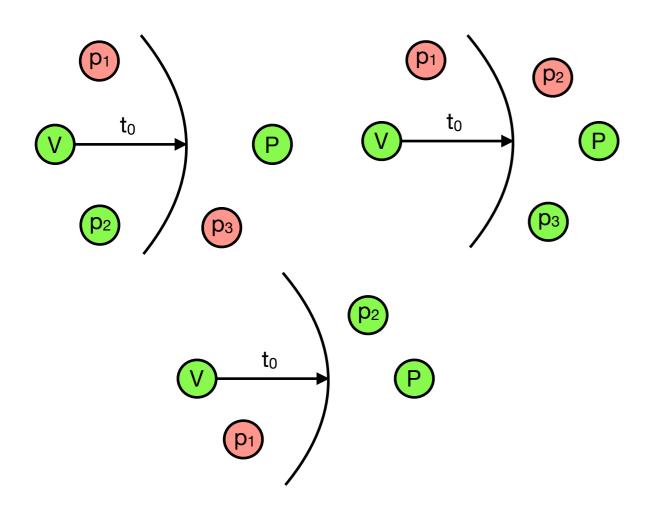
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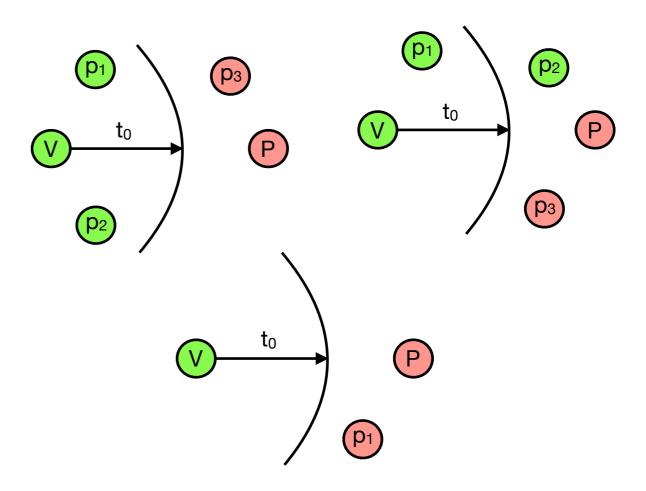


Distance hijacking

(or Man-in-the-Middle)

An attack in a topology such that:

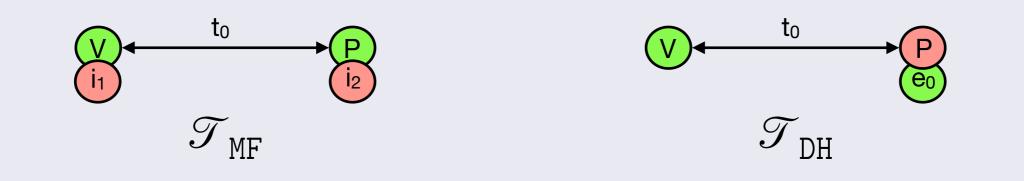
- ►V is honest
- ► P is **dishonest**
- ► No dishonest agents close to V



Contributions

Reduction results

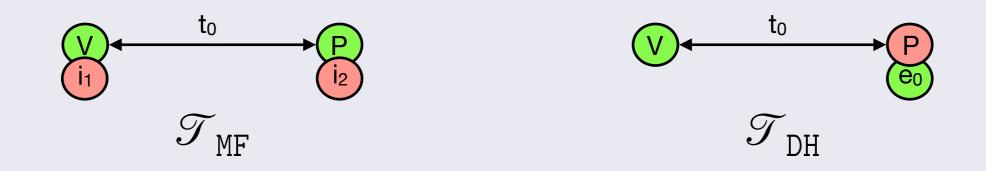
Consider 1 topology is enough to prove Mafia fraud or Distance hijacking resistance!



Contributions

Reduction results

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Getting rid of topologies and time

- Modeling in ProVerif using phases
- Application to well-know DB protocols

Reduction results

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Symbolic verification in a nutshell

Symbolic models:

- (i) <u>Terms</u>: abstracted with terms (e.g. $enc(\langle n_1, n_2 \rangle, k)$)
- (ii) <u>Protocols</u>: specific logics, process algebra, multiset rewriting rules
- (iii) Properties: trace property or equivalence property









Term algebra



Messages: terms but over a set of names \mathcal{N} and a signature Σ given with either an equational theory E or a rewriting system.

Example

- Names: $\mathcal{N} = \{a, n, k\}$
- ► Signature: $\Sigma = \{ \text{senc}, \text{sdec}, \text{pair}, \text{proj}_1, \text{proj}_2, \oplus \}$

$x \oplus 0 = x$	$(x \oplus y) \oplus z = x \oplus (y \oplus z)$
$x \oplus x = 0$	$x \oplus y = y \oplus x$

$$\begin{split} \texttt{sdec}(\texttt{senc}(x,y),y) \to x & \texttt{proj}_1(\texttt{pair}(x,y)) \to x \\ & \texttt{proj}_2(\texttt{pair}(x,y)) \to y \end{split}$$

For example: $sdec(senc(n \oplus 0), k), k)$ is "equal" to n

Process algebra

The role of an agent is described by a process following the grammar:

$$P := 0$$
null process $| new n.P$ name restriction $| let x = u in P$ conditional declaration $| out(u).P$ output $| in(x).P$ input

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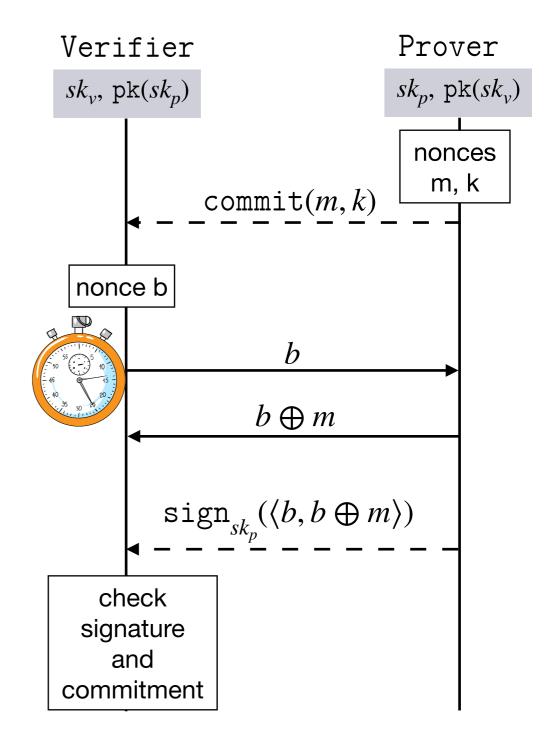
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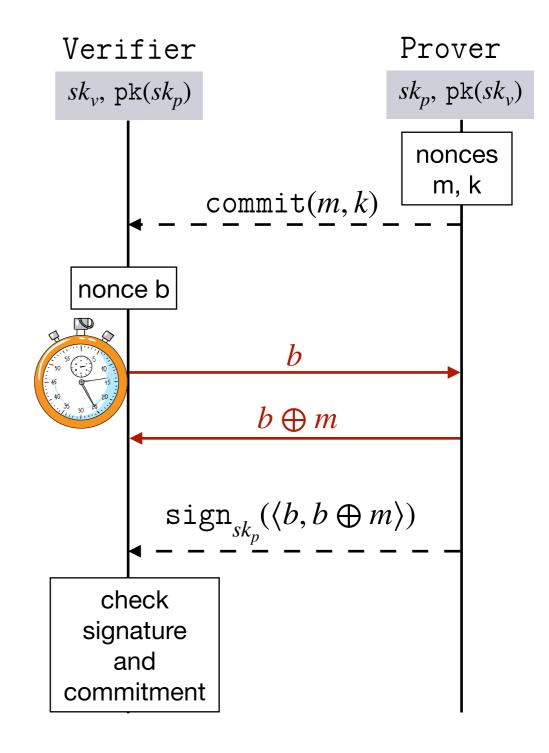
Protocol

A protocol is a set of roles $(\Pi_1, ..., \Pi_k)$ describing the behavior of each honest agents.

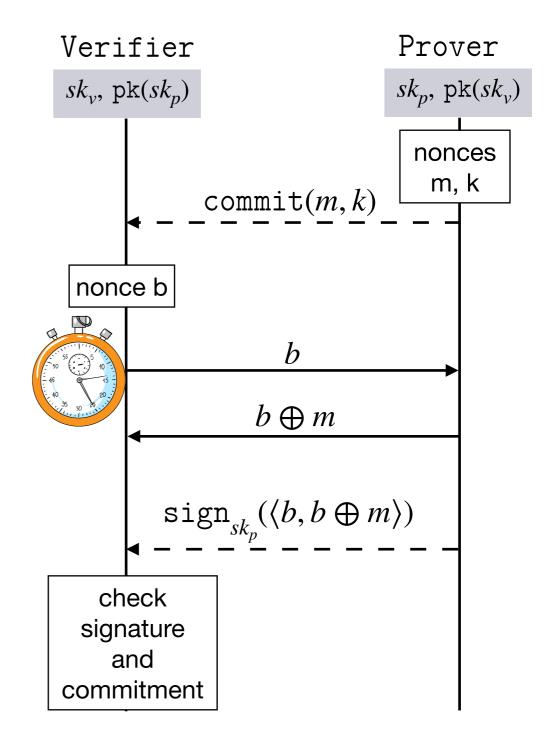
$$\begin{aligned} \forall (z_v, z_p) &\coloneqq \\ & \text{in}(y_c) \text{. new } b \text{.} \\ & \text{reset.out}(b) \text{. in}^{<2 \times t_0}(y_0) \text{.} \\ & \text{in}(y_k) \text{. in}(y_{\text{sign}}) \text{.} \\ & \text{let } y_m = \text{open}(y_c, y_k) \text{ in} \\ & \text{let } y_{\text{msg}} = \text{getmsg}(y_{\text{sign}}) \text{ in} \\ & \text{let } y_{\text{eq}} = \text{eq}(\langle b, b \oplus y_m \rangle, y_{\text{msg}}) \text{ in} \\ & \text{let } y_{\text{eq}'} = \text{eq}(b \oplus y_m, y_0) \text{ in} \\ & 0 \end{aligned}$$



$$\begin{aligned} &\mathcal{V}(z_v, z_p) \coloneqq \\ & \text{in}(y_c) \text{.new } b \text{.} \\ & \text{reset.out}(b) \text{.in}^{<2 \times t_0}(y_0) \text{.} \\ & \text{in}(y_k) \text{.in}(y_{\text{sign}}) \text{.} \\ & \text{let } y_m = \text{open}(y_c, y_k) \text{ in} \\ & \text{let } y_{\text{msg}} = \text{getmsg}(y_{\text{sign}}) \text{ in} \\ & \text{let } y_{\text{eq}} = \text{eq}(\langle b, b \oplus y_m \rangle, y_{\text{msg}}) \text{ in} \\ & \text{let } y_{\text{eq}'} = \text{eq}(b \oplus y_m, y_0) \text{ in} \\ & 0 \end{aligned}$$

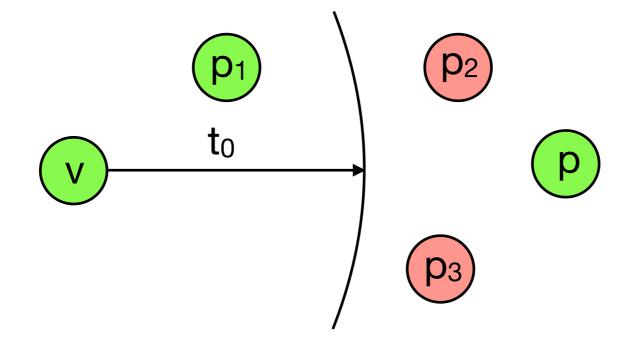


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Topology

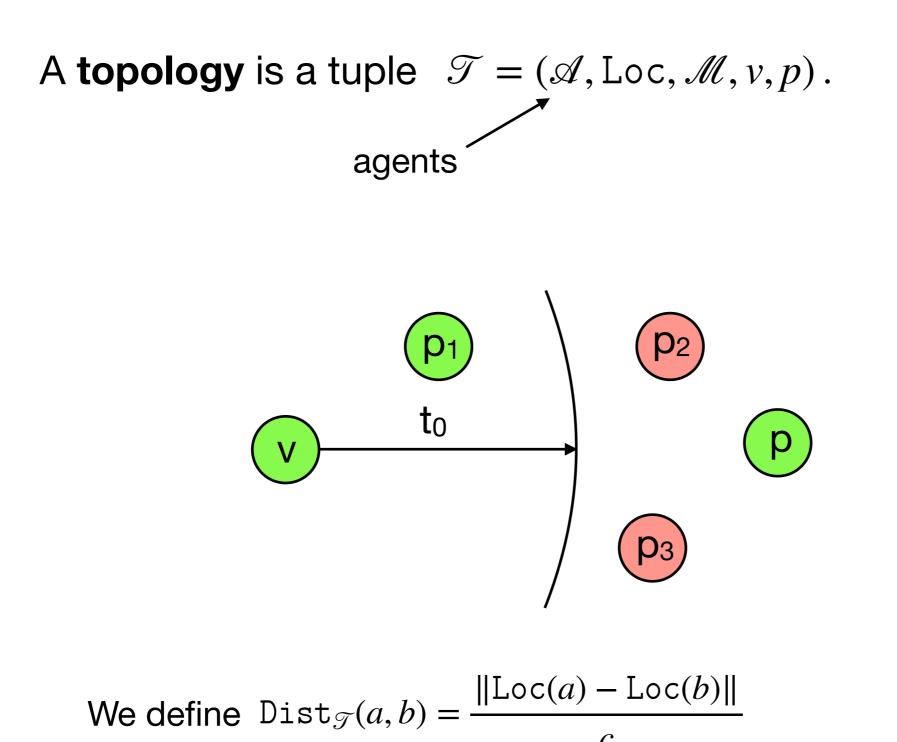
A **topology** is a tuple $\mathcal{T} = (\mathscr{A}, Loc, \mathscr{M}, v, p)$.



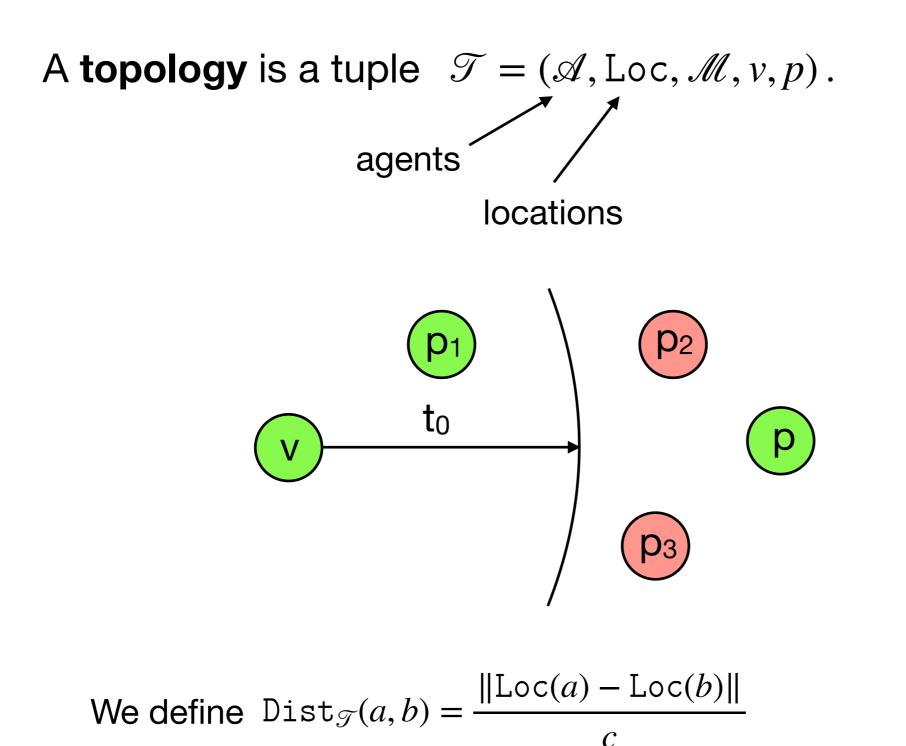
We define
$$\text{Dist}_{\mathcal{T}}(a,b) = \frac{\|\text{Loc}(a) - \text{Loc}(b)\|}{c}$$

Topology

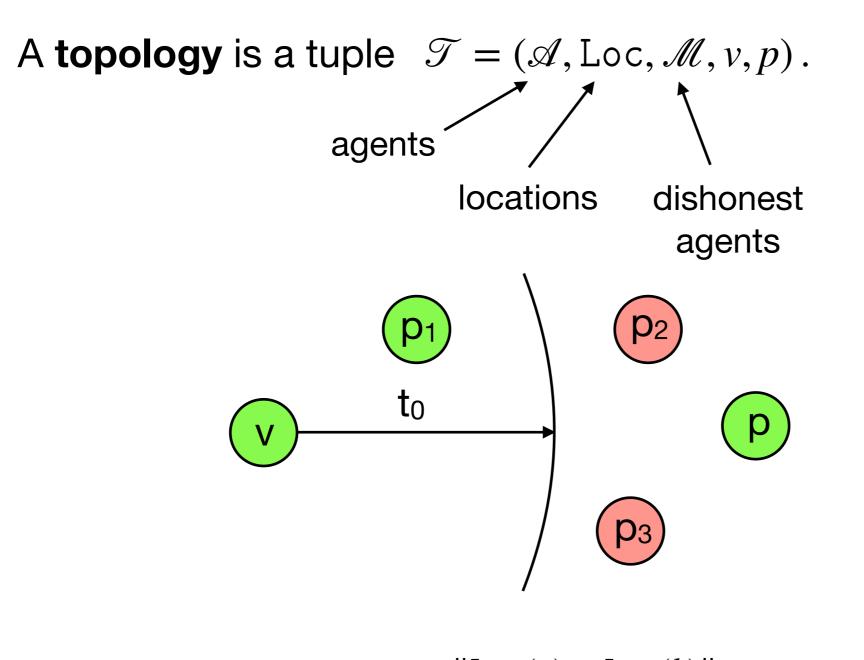
С



Topology

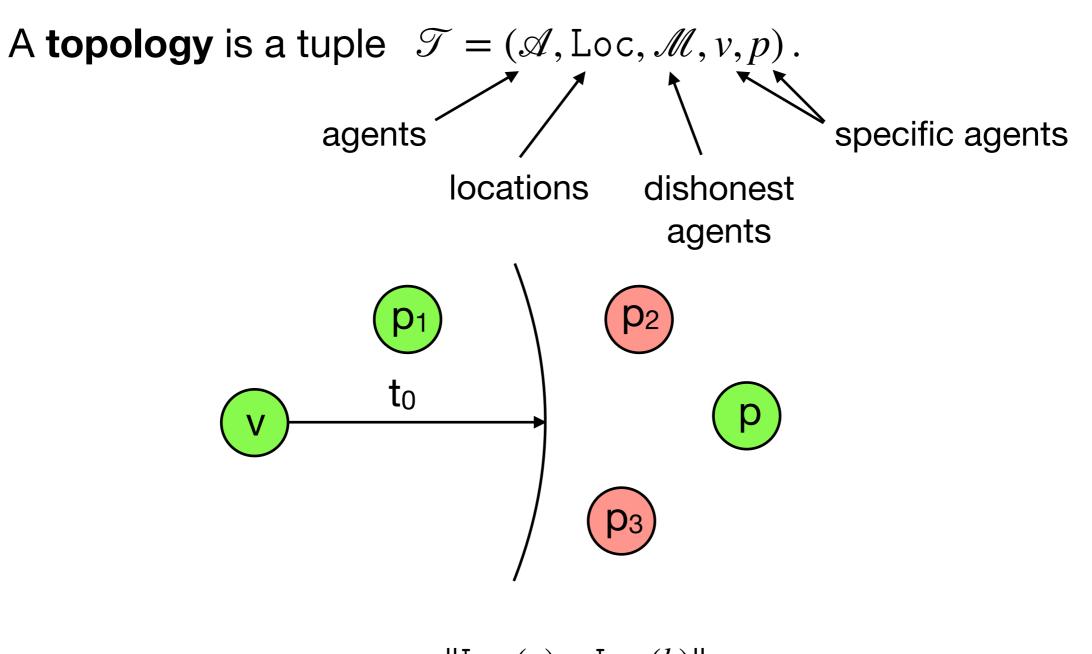


Topology



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Topology



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Configuration and semantics

A configuration is a tuple $(\mathscr{P}; \Phi; t)$ where:

- \mathscr{P} is a multiset of $[P]_a^{t_a}$ with $a \in \mathscr{A}$ and $t_a \in \mathscr{R}_+$
- $\Phi = \{ w_1 \xrightarrow{a_1, t_1} m_1, \dots, w_n \xrightarrow{a_n, t_n} m_n \}$ is a frame
- ▶ $t \in \mathcal{R}_+$ is the global time

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TIME $(\mathscr{P}; \Phi; t) \longrightarrow_{\mathscr{T}_0} (\mathscr{P}'; \Phi; t')$

t' > t

 $\blacktriangleright \mathscr{P}' = \{ |P|_a^{t_a + (t'-t)} | |P| \in \mathscr{P} \}$

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OUT
$$([\operatorname{out}(u) \cdot P]_a^{t_a} \uplus \mathscr{P}; \Phi; t) \xrightarrow{a, \operatorname{out}(u)} \mathscr{T}_0 ([P]_a^{t_a} \uplus \mathscr{P}; \Phi'; t)$$

with $\Phi' = \Phi \cup \{w \xrightarrow{a, t} u\}$

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$$\mathsf{IN} \qquad ([\operatorname{in}^*(x) \, P]_a^{t_a} \uplus \, \mathscr{P}; \Phi; t) \xrightarrow{a, \operatorname{in}^*(u)} \mathscr{T}_0 ([P\{x \mapsto u\}]_a^{t_a} \uplus \, \mathscr{P}; \Phi; t)$$

if u is deducible from Φ

Configuration and semantics

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$$[\mathsf{N} \quad ([\operatorname{in}^*(x) \, P]_a^{t_a} \uplus \, \mathscr{P}; \Phi; t) \xrightarrow{a, \operatorname{in}^*(u)} \mathscr{T}_0 ([P\{x \mapsto u\}]_a^{t_a} \uplus \, \mathscr{P}; \Phi; t)$$

if $\exists b \in \mathscr{A}, t_b \in \mathscr{R}_+$ such that $t_b \leq t - \text{Dist}_{\mathscr{T}_0}(b, a)$ and:

• if
$$b \notin \mathcal{M}$$
 then $u \in img(\lfloor \Phi \rfloor_{h}^{t_{b}})$

• if $b \in \mathcal{M}$ then u is deducible from $\bigcup \lfloor \Phi \rfloor_{c}^{t_{b}-\text{Dist}_{\mathcal{T}_{0}}(c,b)}$ $c \in \mathscr{A}$

Configuration and semantics

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- ▶ $t \in \mathcal{R}_+$ is the global time

NEW, LET, RESET...

Security property: physical proximity

Mafia frauds (resp. Distance hijacking attacks)

A protocol \mathcal{P}_{prox} is resistant against Mafia frauds (resp. Distance hijacking attacks) if for all topologies $\mathcal{T} \in \mathscr{C}_{MF}$ (resp. \mathscr{C}_{DH}) and initial configuration *K*:

$$K \xrightarrow{tr} (\lfloor \operatorname{end}(v_0, p_0) \rfloor_{v_0}^{t_{v_0}}; \Phi; t) \Rightarrow \operatorname{Dist}_{\mathcal{T}}(v_0, p_0) < t_0$$

Reduction results

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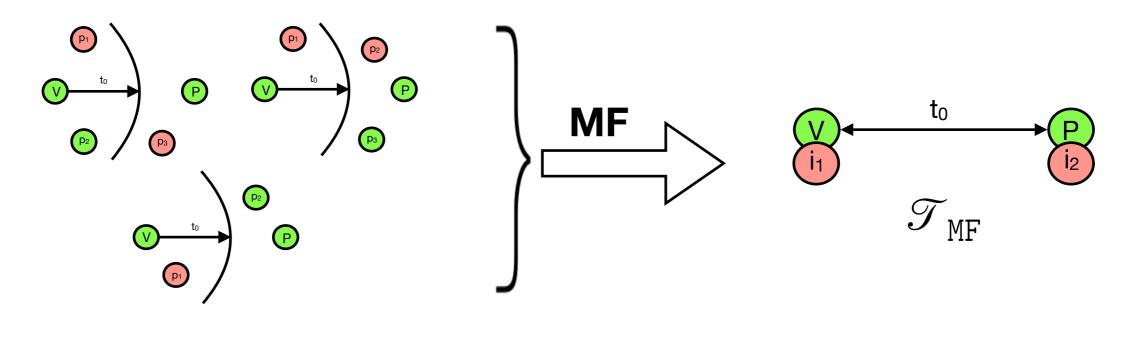
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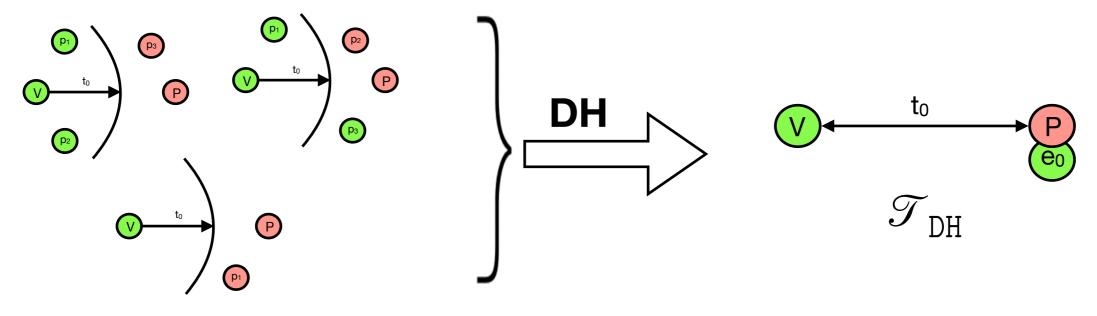
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Reduction results

Only one topology is sufficient!

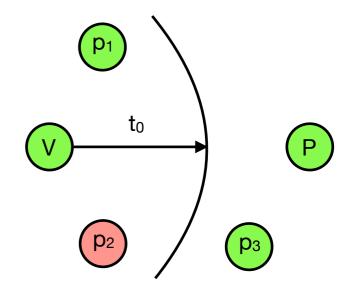




Theorem

Let $\mathscr{P}_{\text{prox}}$ be an executable protocol. $\mathscr{P}_{\text{prox}}$ admits a Mafia fraud attack w.r.t. t_0 -proximity, if and only if, there is an attack against t_0 -proximity in the topology \mathscr{T}_{MF} .

Sketch of proof:

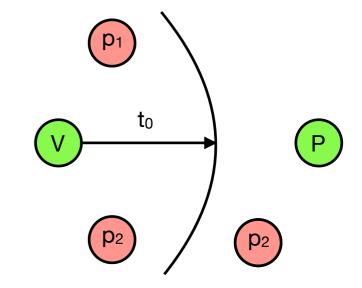


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Sketch of proof:

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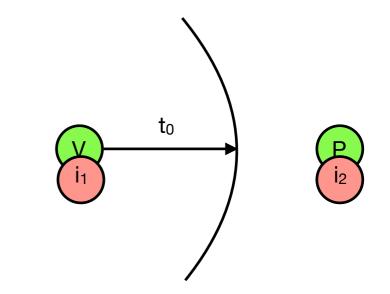
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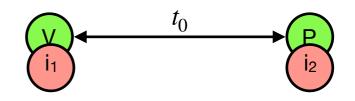


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- 3. We shorten the distance



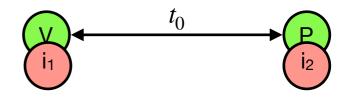
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Sketch of proof:

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Remark. This proof cannot be adapted for distance hijacking attacks!



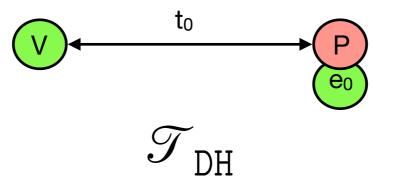
Distance hijacking attacks

Theorem

Let \mathscr{P}_{prox} be a protocol such that the Verifier role respects the following grammar:

> $P, Q := \text{end}(z_0, z_1) \mid \text{in}(x) \cdot P \mid \text{let } x = v \text{ in } P$ $| \text{ new } n \cdot P | \text{ out}(u) \cdot P | \text{ reset.out}(u') \cdot \text{in}^{< t}(x) \cdot P$

If \mathscr{P}_{prox} admits a Distance hijacking attack w.r.t. t_0 -proximity, then $\overline{\mathscr{P}_{prox}}$ admits an attack against t_0 -proximity in the topology \mathcal{T}_{DH} .



In \mathscr{P}_{prox} we only keel guards computed by v_0 .

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Getting rid of topologies and time

Up to now: we have reduced the number of topologies to only one

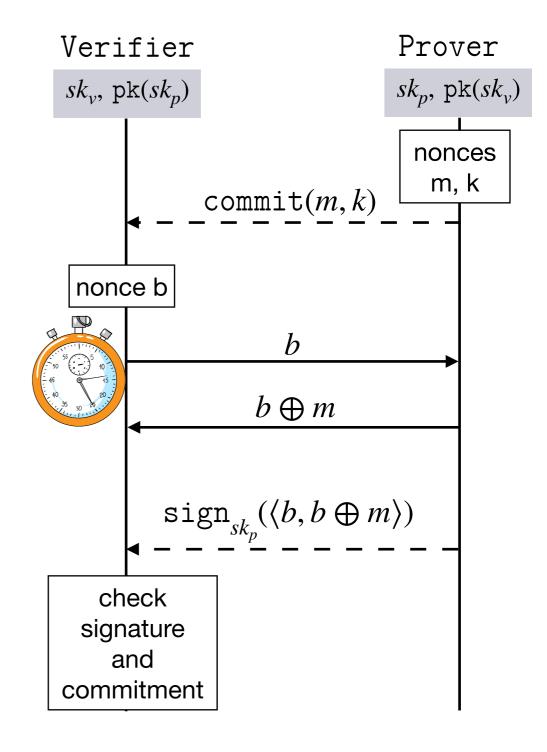
But: even a single topology cannot be modeled into existing tools

We propose a methodology to encode the two reduced topology in the ProVerif tool.

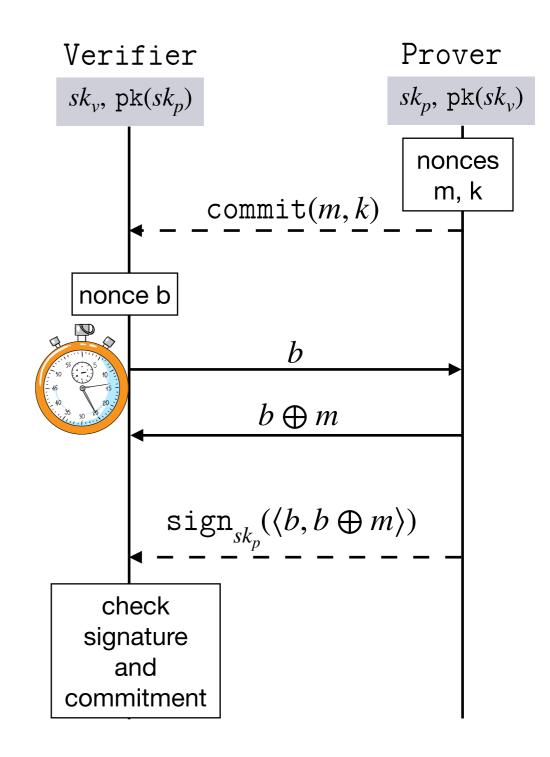
Overview of the encoding

- few assumptions on the protocol
- it relies on the phases of ProVerif
 - e.g. in DB protocols:
 - ► Phase 0 → slow initialization phase
 - ► Phase 1 \longrightarrow rapid phase
 - ► Phase 2 → slow verification phase

$$\begin{split} V(z_v, z_p) &\coloneqq \\ & \text{in}(y_c) \text{.new } b \text{.} \\ & \text{reset.out}(b) \text{.in}^{<2 \times t_0}(y_0) \text{.} \\ & \text{in}(y_k) \text{.in}(y_{\text{sign}}) \text{.} \\ & \text{let } y_m = \text{open}(y_c, y_k) \text{ in} \\ & \text{let } y_{\text{msg}} = \text{getmsg}(y_{\text{sign}}) \text{ in} \\ & \text{let } y_{\text{eq}} = \text{eq}(\langle b, b \oplus y_m \rangle, y_{\text{msg}}) \text{ in} \\ & \text{let } y_{\text{eq}'} = \text{eq}(b \oplus y_m, y_0) \text{ in} \\ & 0 \end{split}$$



```
\overline{V_0}(z_v, z_p) :=
        in(y_c).new b.
         phase 1.
         \operatorname{out}(b).\operatorname{in}(y_0).
        phase 2.
        in(y_k).in(y_{sign}).
        let y_m = \operatorname{open}(y_c, y_k) in
        let y_{msg} = getmsg(y_{sign}) in
        let y_{eq} = eq(\langle b, b \oplus y_m \rangle, y_{msg}) in
        let y_{eq'} = eq(b \oplus y_m, y_0) in
         0
```



Translation into ProVerif $Transf(\mathcal{T}, \mathcal{P}_{prox}, t_0)$

Given a process *P* we define:

- $P^{<}$: all the possible ways of splitting P in the phases 0, 1 and 2
- P^{\geq} : all the possible ways of splitting P in the phases 0, and 2

 $Transf(\mathcal{T}, \mathscr{P}_{prox}, t_0)$ is the multiset of processes derived from \mathscr{P} when applying:

- .< for all instantiated roles of \mathscr{P} executed by agents close to v_0
- ▶ .≥ for all instantiated roles of \mathscr{P} executed by agents far from v_0

Proposition

If $(\mathscr{P}_{prox} \cup V_0)$ admits an attack w.r.t. t_0 – proximity in \mathscr{T} then $(Transf(\mathcal{T}, \mathcal{P}, t_0) \uplus \overline{V_0}(v_0, p_0); \Phi_{\text{init}})$ admits an attack in ProVerif.

Inspired by [Chothia et al. - FC'15]

Case analysis - DB protocols

Protocols	MF	DH
Brands and Chaum		X
Meadows <i>et al.</i> $(n_V \oplus n_P, P)$		\checkmark
Meadows <i>et al.</i> $(n_V, n_P \oplus P)$		×
TREAD-Asymmetric	×	×
TREAD-Symmetric		×
MAD (One-Way)		×
Swiss-Knife		\checkmark
Munilla et al.		\checkmark
CRCS		×
Hancke and Kuhn		\checkmark

(\times : attack found, \checkmark : proved secure)

- Coherent with the recent analysis done in [Mauw et al. S&P'18] using Tamarin
- We never obtained false attacks

Conclusion

We have adapted an existing symbolic model to take time into account.

We obtained **two reductions results** that reduce the number of relevant topologies that need to be studied from infinitely many to only 2.



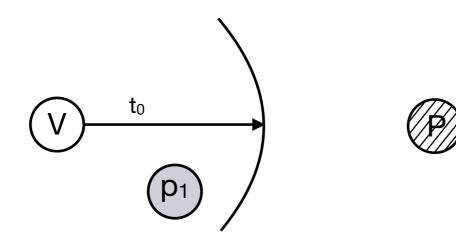
We provide a methodology to encode these reduced topologies into an **existing verification tool**, ProVerif, to be able to analyse well-known protocols w.r.t. authentication with physical proximity.

Future work

Goal: Establish reduction results to enable the verification for Terrorist frauds reusing existing tools.

Terrorist fraud

A remote dishonest prover cooperates with another dishonest agent, close to the verifier, to authenticates himself to the prover without giving any advantages for future attacks.



Challenge:

Formally define the notion of semi-dishonest agents